



## GWTC-4.0: Population Properties of Merging Compact Binaries

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## Abstract

We detail the population properties of binary neutron star, neutron star–black hole binary, and binary black hole mergers using 158 events from the cumulative Gravitational-Wave Transient Catalog 4.0. The black hole primary mass distribution consists of a power-law-like continuum that steepens above  $35 M_{\odot}$  with overdensities at  $10 M_{\odot}$  and  $35 M_{\odot}$ . Binary black holes with primary masses near  $10 M_{\odot}$  are more likely to have less massive secondaries, with a mass ratio distribution peaking at  $q = 0.71^{+0.12}_{-0.11}$ , potentially a signature of stable mass transfer during binary evolution. Black hole spins are inferred to be nonextremal, with 90% of black holes having  $\chi < 0.6$ , and preferentially aligned with binary orbits, implying many merging binaries form in isolation. However, we find that a significant fraction, 0.23–0.41, of binaries have negative effective inspiral spins, suggesting many could be formed dynamically in gas-free environments. We find evidence for correlation between effective inspiral spin and mass ratio, driven either by variation in the mode of the distribution or the width. The binary black hole merger rate increases with redshift, consistent with the cosmic star formation density. While there is no evidence of the mass spectrum evolving with redshift, the distribution of effective inspiral spin is found to broaden as redshift increases out to  $z \approx 1$ . We infer the local merger rates (at  $z = 0$ ) to be  $8.8\text{--}250 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for binary neutron stars,  $9.3\text{--}86 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for neutron star–black hole binaries, and  $13\text{--}26 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for binary black holes; all values reflect central 90% credible intervals.

*Unified Astronomy Thesaurus concepts:* [Gravitational waves \(678\)](#); [Astrophysical black holes \(98\)](#); [Neutron stars \(1108\)](#); [Compact binary stars \(283\)](#)

## 1. Introduction

Gravitational waves (GWs) have revolutionized the study of compact objects and their populations (B. P. Abbott et al. 2016a, 2019a; R. Abbott et al. 2021a, 2023a), with observations now extending beyond redshift  $z = 1$ . Searches for GWs from compact binary mergers have robustly quantifiable selection effects, which enable detailed inference of population properties with few sources of potential bias (I. Mandel et al. 2019; S. Vitale et al. 2020; R. Essick & M. Fishbach 2024). By studying the growing catalog of compact binary mergers, we aim to uncover both where these systems form and how they evolve toward merger. For example, are they formed from stars that are gravitationally bound at birth, possibly as the products of chemically homogeneous evolution (S. E. de Mink & I. Mandel 2016; I. Mandel & S. E. de Mink 2016; P. Marchant et al. 2016), or brought close enough together for GW-driven inspiral through phases of common envelope evolution (H. A. Bethe & G. E. Brown 1998; S. F. Portegies Zwart & L. R. Yungelson 1998; K. Belczynski et al. 2001; M. Dominik et al. 2015) or stable mass transfer (J. R. Hurley et al. 2002; C. J. Neijssel et al. 2019; L. A. C. van Son et al. 2022b)? Could binaries be assisted in assembly and hardening in the gaseous disks of active galactic nuclei (AGN; B. McKernan et al. 2012; I. Bartos et al. 2017; N. C. Stone et al. 2017; G. Fragione et al. 2019) or through dynamical interactions in dense stellar environments (S. F. Kulkarni et al. 1993; S. Sigurdsson & L. Hernquist 1993; S. F. Portegies Zwart & S. McMillan 2000; B. M. Ziosi et al. 2014)?

From the first three observing runs of the LIGO–Virgo–KAGRA Collaboration (LVK), we established that stellar-mass black holes (BHs) in merging binaries have a broad distribution of masses, with peaks at primary masses of  $\sim 10 M_{\odot}$  and  $\sim 35 M_{\odot}$ , that falls off steeply above  $\sim 45 M_{\odot}$  (R. Abbott et al. 2023a). Despite the steep decline, the rate of mergers in the expected pair-instability supernova gap, predicted to begin at  $\sim 45\text{--}50 M_{\odot}$  (S. E. Woosley 2017; R. Farmer et al. 2019), was found to be nonzero (R. Abbott et al. 2020a, 2020b). Likewise, the rate of mergers in the purported lower mass gap between  $\sim 3$  and  $5 M_{\odot}$  (C. D. Bailyn et al. 1998; F. Ozel et al. 2010; W. M. Farr et al. 2011) was

found to be small but nonzero (R. Abbott et al. 2020c; A. G. Abac et al. 2024). The neutron star (NS) mass distribution does not require a peak in the distribution at  $\sim 1.33 M_{\odot}$ , as is seen in the galactic binary neutron star (BNS) population (F. Özel & P. Freire 2016; N. Farrow et al. 2019). The binary black hole (BBH) merger rate was found to definitively increase with redshift. Spins were found to be small in magnitude, with a nonzero fraction of systems with spin components antialigned with the binary orbit.

Advanced LIGO (J. Aasi et al. 2015), Advanced Virgo ; (F. Acernese et al. 2015), and the Kamioka Gravitational Wave Detector (KAGRA; T. Akutsu et al. 2021) began their fourth observing run (O4) on 2023 May 24 at 15:00 UTC. The first part of the fourth observing run (O4a) ended on 2024 January 16 at 16:00 UTC. The accompanying Gravitational Wave Transient Catalog (GWTC) version 4.0 (hereafter, GWTC-4.0; A. G. Abac et al. 2025a, 2026a, 2026b) contains those events observed in previous observing runs, O1 (B. P. Abbott et al. 2016a), O2 (B. P. Abbott et al. 2019b), and O3 (R. Abbott et al. 2021b, 2023b, 2024), together with the newest observations from first part of the fourth observing run (O4a). We use the updated catalog to infer the population properties of BNS, neutron star–black hole binary (NSBH), and BBH systems in the local Universe.

GWTC-3.0 included 76 candidates with false alarm rate (FAR)  $< 1 \text{ yr}^{-1}$ : 69 BBHs, 4 NSBHs, 2 BNSs, and 1 event GW190814\_211039 (henceforth, GW190814) that is either an NSBH or BBH. A. G. Abac et al. (2026b) identifies 128 candidate signals in O4a with a probability of astrophysical compact binary origin (W. M. Farr et al. 2015; B. P. Abbott et al. 2016b; S. J. Kapadia et al. 2020; A. G. Abac et al. 2026a) of  $p_{\text{astro}} \geq 0.5$ , of which 85 (84 BBHs and 1 NSBH) have FAR  $< 1 \text{ yr}^{-1}$ . Selecting BBHs from the catalog using this threshold yields a cumulative BBH count of 153. With fewer signal candidates from binaries containing at least one NS, maintaining a comparable contamination fraction to that of BBH mergers ( $\sim 5\%$ ) requires a more conservative threshold (see Section 3 for more details). We adopt the same threshold used for similar analyses of GWTC-3.0, FAR  $< 0.25 \text{ yr}^{-1}$ , for analyses that include NS-containing populations (R. Abbott et al. 2023a). This yields two NSBH candidates from O3 and one new candidate, GW230529\_181500 (henceforth, GW230529), detected above

this threshold in designated observing time during O4a (A. G. Abac et al. 2024). Section 3 provides further details and discussion of threshold choices and candidate inclusion. Adopting the more conservative  $\text{FAR} < 0.25 \text{ yr}^{-1}$  threshold reduces the O4a BBH count to 76, resulting in a catalog of 2 BNSs, 3 NSBHs, and 138 BBHs for analyses that include BNS and NSBH populations in this work.

The remainder of the paper is structured as follows. In Section 2, we provide a brief description of our inference techniques (with remaining details in Appendix A) and the classes of models used (with full descriptions of the models in Appendices B and C, and how they were chosen in Appendix D). Section 3 describes our dataset and sample selection, including brief descriptions of search techniques, threshold choices, and waveform models used. In Section 4, we present measurements of the complete compact-binary mass spectrum (NSs and BHs). In Section 5, we study the properties of the NS-containing population in detail, and in Section 6 focus on the ensemble properties of BBHs, including their masses, spins, redshifts, and associated correlations. Section 7 concludes by summarizing the key results of this work. Associated data releases provide analysis results and figure generation scripts (LIGO Scientific Collaboration et al. 2025) and data products for estimating sensitivity (R. Essick 2025a, 2025b).

## 2. Methods

We determine the population properties of merging compact binaries using hierarchical Bayesian inference as has been done in previous studies (B. P. Abbott et al. 2019a; R. Abbott et al. 2021a, 2023a). Our aim here is to estimate the posterior distribution  $p(\Lambda|d)$  on population-level model parameters  $\Lambda$  (also referred to as *hyperparameters*) in light of new data  $d$  representing the observed GW data from individual merger events. These model-dependent hyperparameters describe the population-level properties of GW source parameters  $\theta$  (masses, spins, redshifts, etc.). According to Bayes' theorem,

$$p(\Lambda|d) = \frac{\mathcal{L}(d|\Lambda)\pi(\Lambda)}{p(d)}, \quad (1)$$

where  $\pi(\Lambda)$  is the prior probability distribution and  $\mathcal{L}(d|\Lambda)$  is the likelihood—the probability of obtaining the data  $d$  given some  $\Lambda$ . The Bayesian *evidence*  $p(d)$  ensures that  $p(\Lambda|d)$  is properly normalized.

In order to use Bayes' theorem to infer the posterior probability distribution of hyperparameters, we need the likelihood of obtaining the observed catalog of events given a set of hyperparameters and a population model. Because GW detectors are not equally sensitive to different astrophysical sources, the likelihood must account for selection biases. Various groups have developed independent frameworks to account for selection effects and infer population properties (e.g., D. Wysocki et al. 2019; J. Roulet et al. 2021), providing a crucial cross-check to the standard approach used by collaboration analyses, detailed below. Assuming (i) a Poisson process generates realizations from the source population of which a subset is detected and (ii) the observed data associated are statistically independent (e.g., no overlapping signals), the likelihood is given by (T. J. Loredo 2004; D. W. Hogg et al. 2010; W. M. Farr et al. 2015; S. R. Taylor & D. Gerosa 2018; I. Mandel et al. 2019; E. Thrane & C. Talbot 2019;

S. Vitale et al. 2020)

$$\mathcal{L}(\{d_i\}, N_{\text{det}}|\Lambda) \propto N(\Lambda)^{N_{\text{det}}} e^{-N_{\text{exp}}(\Lambda)} \prod_{i=1}^{N_{\text{det}}} \int d\theta \mathcal{L}(d_i|\theta) \pi(\theta|\Lambda), \quad (2)$$

where  $N(\Lambda)$  is the total number of mergers (detected and undetected) incident on the detectors within the observing period,  $N_{\text{det}}$  is the number of detections,  $d_i$  are the strain data corresponding to the  $i$ th detection, and  $\mathcal{L}(d_i|\theta)$  is the likelihood of the data  $d_i$  given the GW source parameters  $\theta$  (A. G. Abac et al. 2026a). The expected number of detections is  $N_{\text{exp}}(\Lambda) = N \xi(\Lambda)$ , with  $\xi(\Lambda)$  being the expected fraction of the population parameterized by  $\Lambda$  that is detectable. Formally, we impose a detection criterion on the data, e.g., a FAR threshold, by the selection function  $x(d)$  acting on a data segment  $d$ . A GW event is detectable in  $d$  if  $x(d) > x_{\text{thr}}$ , where  $x_{\text{thr}}$  is the chosen detectability threshold. Then,

$$\xi(\Lambda) = \int_{x(d) > x_{\text{thr}}} dd d\theta p(d|\theta) \pi(\theta|\Lambda). \quad (3)$$

In Equation (3), the domain of integration is over all data  $d$ , which surpasses the detection threshold  $x_{\text{thr}}$  (R. Essick et al. 2025). When a prior  $\pi(N) \propto 1/N$  is assumed, Equation (2) can be analytically marginalized over  $N$  leaving the rate-marginalized hierarchical likelihood

$$\mathcal{L}(\{d_i\}, N_{\text{det}}|\Lambda) \propto \prod_{i=1}^{N_{\text{det}}} \frac{\int d\theta \mathcal{L}(d_i|\theta) \pi(\theta|\Lambda)}{\xi(\Lambda)}. \quad (4)$$

This likelihood may also be obtained by marginalizing over a prior on the expected number of detections,  $N_{\text{exp}} = N\xi(\Lambda)$ , rather than on  $N$  (R. Essick & M. Fishbach 2024).

Having described the hierarchical likelihood in Equation (2) and Equation (4) we have one of the two ingredients necessary for sampling the posterior in Equation (1). We also must choose a prior over the space of hyperparameters. This depends on the population model, which we describe in more detail below. We specify the priors for each model in Appendix B.

Equation (2) is the exact form of the likelihood. However, calculating  $\xi(\Lambda)$  and integrating over  $\theta$  is analytically intractable. Therefore, we approximate the likelihood via Monte Carlo reweighting using importance sampling. Our Monte Carlo approximation for the likelihood carries some uncertainty and may not be converged appropriately for some hyperparameter values. Therefore, we discard hyperparameters whose likelihood uncertainty exceeds a chosen threshold a posteriori (C. Talbot & J. Golomb 2023). For more description of this problem and our approach for mitigating it, see Appendix A.

The Bayesian inference problem is stated here in terms of the population probability density  $\pi(\theta|\Lambda)$  and the overall number of merging binaries  $N$ . This can be converted to another astrophysical quantity of interest, the comoving source-frame merger rate density

$$\mathcal{R}(z) = \frac{dN}{dV_c dt_s}(z) = \frac{dN}{dt_d dz} \left( \frac{dV_c}{dz} \frac{1}{1+z} \right)^{-1}, \quad (5)$$

where  $t_s$  is the time measured in the comoving source frame,  $t_d$  is the time at the detector (redshift  $z = 0$ ) and  $dV_c/dz$  is the

differential comoving volume with respect to redshift  $z$  (see, e.g., R. Essick et al. 2025). The comoving source frame merger rate represents the number of mergers in a unit of comoving volume and source-frame time, conventionally measured in units of  $\text{Gpc}^{-3} \text{yr}^{-1}$ .

To construct models for the population distribution of astrophysical GW sources, we take one of two approaches. The first approach—which we call the *strongly modeled approach* (sometimes called the parametric approach)—assumes a specific functional form  $\pi(\theta|\Lambda)$  for the astrophysical distribution a priori, e.g., a Gaussian distribution or a power law. A second approach—which we call the *weakly modeled approach* (elsewhere data-driven, flexible, or non-parametric)—attempts to make minimal a priori assumptions about the underlying astrophysical population, e.g., a spline model. We elaborate on each approach in the following two subsections and provide details for the models presented in this work falling into each category.

### 2.1. Strongly Modeled Approach

The strongly modeled approach assumes that the underlying astrophysical distribution of binary properties can be described by a fixed functional form and associated hyperparameters. Consequently, this approach has far fewer hyperparameters as compared to the weakly modeled approach. The parameterization may be motivated by theoretical expectations about the astrophysical population and/or could be selected because it seems to fit the observed data well. This has the benefit of being simple and interpretable, as hyperparameters can be designed to correspond directly to physical features of interest. Examples of such features are a distribution’s minimum or maximum, the location parameter for an overdensity corresponding to, e.g., pulsational pair-instability supernovae, etc. On the other hand, these approaches can be overly restrictive: features present in the true astrophysical distribution that are not captured by our parameterization cannot be easily discovered. Additionally, the inferred parameters can be biased due to a misspecified model (e.g., I. M. Romero-Shaw et al. 2022).

The parameterized models selected for this work are generally simple extensions to those employed in the previous LVK astrophysical population studies paper from GWTC-3.0 (R. Abbott et al. 2023a). Updates to these models are motivated by features that have emerged due to new data in GWTC-4.0 and improved interpretations since GWTC-3.0.

Table 1 lists the strongly modeled approaches used in this paper, with details in Appendix B. We also describe the parameterizations and priors for these models in Appendix B and our procedure for selecting the default strongly modeled approach in Appendix D. For most models, we assume that masses, spins, and redshifts are all uncorrelated. We also study a selection of pairwise correlations between parameters in Section 6.5.

### 2.2. Weakly Modeled Approach

The weakly modeled approach adopts models that deliberately make few assumptions about the nature of the underlying compact-binary population. Such approaches typically require a larger number of hyperparameters in order to effectively approximate a wide variety of distributions. The philosophy of a weakly modeled approach is to discover unexpected features

in the population, which may be unforeseen or difficult to parameterize. However, they could yield results that are more difficult to interpret astrophysically. The difference between the strongly modeled and weakly modeled approaches can be understood in terms of the bias–variance tradeoff; the former has low variance with a risk of bias, whereas the latter has low bias but elevated variance.

Weakly modeled approaches must make some assumptions, however, and must be designed with different features in mind. For example, different approaches have sensitivity to astrophysical correlations, narrow structures, or gaps in the population. While a unified Bayesian approach to capture generic population features is still an open problem (I. Mandel et al. 2017; V. Tiwari 2021; S. Rinaldi & W. Del Pozzo 2021; B. Edelman et al. 2023; J. Golomb & C. Talbot 2023; E. Payne & E. Thrane 2023; A. Ray et al. 2023a; A. Toubiana et al. 2023; T. A. Callister & W. M. Farr 2024; A. M. Farah et al. 2025; J. Heinzl et al. 2025a), we use two different weakly modeled approaches—B-SPLINE and binned Gaussian process (BGP)—to verify results from our strongly modeled approaches (see Table 1). We describe two additional weakly modeled approaches—Autoregressive Process (AR) and Flexible Mixtures (FM)—in Appendix C, and compare these approaches in Appendix D.4.

## 3. Dataset

### 3.1. Data Collection Duration

Analyses presented in this paper use selected data products from GWTC-4.0 (A. G. Abac et al. 2025a, 2026a, 2026b, 2026c). This section and Section 3.2 provide details on the selection criteria for events analyzed for this paper. GWTC-4.0 includes GW candidates and data from the first observing run (O1) through the end of O4a, as well as a GW candidate and data collected during an engineering run (ER; B. P. Abbott et al. 2020a) directly preceding the start of O4a. ERs are periods dedicated to final commissioning and configuration of the instruments prior to an observing run; the instruments may be in locked and low-noise configurations, but are not generally intended to perform astrophysical observations. The ER data included in GWTC-4.0 is deliberately chosen to contain a few days of data around a GW event potentially originating from an NSBH binary merger, GW230518\_125908 (henceforth, GW230518). The analyses and results quoted in this paper exclude data obtained during the ER; the inclusion of this data would introduce human selection effects that cannot be easily incorporated into  $\xi(\Lambda)$  and hence may bias our inferences.

### 3.2. Event Selection Criteria

#### 3.2.1. Significance Thresholds

To ensure that the dataset we use in this paper has reduced contamination from noise events, we adopt a significance threshold of  $\text{FAR} < 1 \text{ yr}^{-1}$  in at least one GW search pipeline, which is consistent with the criterion adopted in R. Abbott et al. (2023a). Based on the FAR threshold, a total of 161 CBC candidates have been detected from O1 through O4a (B. P. Abbott et al. 2019b; R. Abbott et al. 2021b, 2023b, 2024) by the GW search pipelines (A. G. Abac et al. 2026b), of which 85 were from O4a. This is a noteworthy increase in the number of observations reported

**Table 1**  
Summary of Models

| Model Type                          | Model Name                          | Description                                                                                                                                                                                                                                                                        |
|-------------------------------------|-------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Strongly Modeled:<br>Mass           | FULLPOP-4.0                         | Models the mass spectrum of all CBCs simultaneously with appropriate power-law and peak components. Also allows for a gap between the most massive NS and the least massive BH.                                                                                                    |
|                                     | BROKEN POWER LAW + 2 PEAKS $\star$  | The primary mass distribution has a broken power-law continuum between a minimum and maximum mass, plus two Gaussian peaks around $\sim 10 M_{\odot}$ and $\sim 35 M_{\odot}$ . The distribution of mass ratio $q$ is a power law between some minimum value and 1.                |
|                                     | EXTENDED BROKEN POWER LAW + 2 PEAKS | The mass-ratio power law is allowed to differ between primary masses in the continuum and in the $35 M_{\odot}$ peak.                                                                                                                                                              |
| Strongly Modeled:<br>Component Spin | GAUSSIAN COMPONENT SPINS $\star$    | The spin magnitude population is a Gaussian truncated over the physical range $\chi \in [0, 1)$ . The distribution of cosine spin tilts relative to the orbital angular momentum includes an isotropic (i.e., uniform) component and a truncated Gaussian component.               |
| Strongly Modeled:<br>Effective Spin | GAUSSIAN EFFECTIVE SPINS            | The joint $\chi_{\text{eff}}\text{--}\chi_p$ effective spin distribution is a bivariate Gaussian allowing for correlations.                                                                                                                                                        |
|                                     | SKEW-NORMAL EFFECTIVE SPIN          | The $\chi_{\text{eff}}$ marginal effective spin distribution is skew normal, truncated to $[-1, 1]$ .                                                                                                                                                                              |
| Strongly Modeled:<br>Redshift       | POWER LAW REDSHIFT $\star$          | The merger rate per unit comoving volume and source-frame time evolves with redshift $z$ as a power law, i.e., $\propto (1+z)^{\kappa}$ .                                                                                                                                          |
| Strongly Modeled:<br>Correlations   | COPULA                              | Truncated Gaussian distributions are assumed for $\chi_{\text{eff}}$ and $\chi_p$ . A Frank copula density function correlates two variables. Separate copula models correlate $(q, \chi_{\text{eff}})$ , $(z, \chi_{\text{eff}})$ , $(m_1, \chi_{\text{eff}})$ , and $(m_1, z)$ . |
|                                     | LINEAR                              | A truncated Gaussian distribution is assumed for $\chi_{\text{eff}}$ with the mean and width linearly dependent on either $q$ or $z$ .                                                                                                                                             |
|                                     | SPLINE                              | A truncated Gaussian distribution is assumed for $\chi_{\text{eff}}$ with the mean and width dependent on either $q$ or $z$ . This dependence is flexibly modeled with a cubic spline.                                                                                             |
| Weakly Modeled:<br>All Parameters   | B-SPLINE                            | Fits the astrophysical distribution as a separable joint distribution with one-dimensional B-splines. Large numbers of basis functions allow for flexibility, with difference-based priors imposing smooth evolution a priori.                                                     |
|                                     | BINNED GAUSSIAN PROCESS             | Assumes a fixed binning scheme and infers the event rate under the assumption of a constant rate within each bin, and a Gaussian process prior imposing smooth covariance across bins.                                                                                             |

**Note.** Strongly modeled and weakly modeled approaches used to study the mass, spin, and redshift distributions of merging compact binaries. We provide a brief description of each model here, with detailed descriptions in Appendices B and C. Models marked with a  $\star$  are treated as defaults and are used whenever no model is explicitly indicated for a certain parameter. All strongly modeled approaches mentioned below target BBHs, with the exception of FULLPOP-4.0, which is used to model the entire compact binary coalescence (CBC) population.

in R. Abbott et al. (2023b), which contained 76 events meeting the  $\text{FAR} < 1 \text{ yr}^{-1}$  threshold. With this FAR threshold and assuming noise signals are produced independently, we expect  $\sum_k \text{FAR} \times T_k \simeq 6.7$  contaminant noise events in our results, where  $T_k$  is an estimate of the time examined by the  $k$ th search. The list of GW events included in the analyses of this paper contains GW231123\_135430 (henceforth, GW231123), which has high probability for being the most massive BBH with  $\text{FAR} < 1 \text{ yr}^{-1}$  detected to date by the GWs with both component masses possibly in the upper mass gap ; (S. E. Woosley 2017; R. Farmer et al. 2019, 2020; M. Mapelli et al. 2020; S. E. Woosley & A. Heger 2021; D. D. Hendriks et al. 2023; A. G. Abac et al. 2025b). Not all events reported in the GWTC papers (B. P. Abbott et al. 2019b; R. Abbott et al. 2021b, 2023b, 2024; A. G. Abac et al. 2026b) are included in our analyses, as previous GWTC papers thresholded event candidates using  $p_{\text{astro}} \geq 0.5$  or  $\text{FAR} < 2 \text{ yr}^{-1}$ , whereas the

analyses presented in our paper select events with a significance of  $\text{FAR} < 1 \text{ yr}^{-1}$ . Here,  $p_{\text{astro}}$  is the estimate of the probability of astrophysical origin of the event candidates (A. G. Abac et al. 2026a, 2026b). In addition, GW230630\_070659 is excluded from the analyses and the number of events reported in this paper, due to concerns of the data quality around the time of this event (A. G. Abac et al. 2026b).

### 3.2.2. Mass and Significance Thresholds for Events with NSs

To distinguish NS-containing events from events containing only BHs, we first threshold events by checking whether the 1% lower limit on the component mass is smaller or larger than  $3 M_{\odot}$ . As far fewer GW candidates with NSs have been observed compared to BBHs, this paper adopts a stricter FAR threshold of  $< 0.25 \text{ yr}^{-1}$  in at least one GW search pipeline for GW candidates with NSs to ensure a purer sample, as done

in R. Abbott et al. (2023a). This FAR threshold excludes GW190917\_114630 and GW190426\_152155 (R. Abbott et al. 2024), which are consistent with originating from NSBHs but have FARs of  $>0.25 \text{ yr}^{-1}$ . In addition, we exclude certain events whose category is ambiguous from dedicated BBH and NSBH analyses. Specifically, we exclude GW190814 as its source’s secondary mass is lower than the component masses of events classified as BBHs but higher than the inferred NS mass range, leaving its classification ambiguous (R. Abbott et al. 2020c, 2023a; R. Essick et al. 2022; U. Mali & R. Essick 2026). This event is included in Section 4, which considers binary-merger populations across all masses. Hence, the only NS-containing event detected in O4a considered in this paper is GW230529 (A. G. Abac et al. 2024), in addition to the previously reported NSBHs, GW200105\_162426 and GW200115\_042309 (henceforth, GW200105 and GW200115, respectively). The results are presented in Section 5.

### 3.2.3. Exclusion of Non-LVK Catalog Events

In addition to the catalog of event candidates and its analyses conducted by the LVK, independent teams have analyzed the public GW data from O1 through the second half of the third observing run (O3b) using alternative algorithms and have identified additional GW binary-merger event candidates (T. Venumadhav et al. 2019, 2020; S. Olsen et al. 2022; A. H. Nitz et al. 2019, 2020, 2021, 2023; B. Zackay et al. 2019; D. Wadekar et al. 2023; P. Kumar & T. Dent 2024; A. E. Koloniari et al. 2025; A. K. Mehta et al. 2025; T. Mishra et al. 2025). We do not include these additional events in our analyses here due to subtleties with consistently combining sensitivity estimates from these independent catalogs.

### 3.3. Sensitivity of GW Searches

A key ingredient in the estimation of population level properties is the sensitivity of our GW searches  $\xi(\Lambda)$ . The following four search pipelines analyzed detector data for *real* GW signals as well as simulated GW signals, called *injections*: GSTLAL (C. Messick et al. 2017; S. Sachdev et al. 2019; C. Hanna et al. 2020; K. Cannon et al. 2021; B. Ewing et al. 2024; L. Tsukada et al. 2023; S. Sakon et al. 2024; A. Ray et al. 2023b; P. Joshi et al. 2025a, 2025b), MBTA (T. Adams et al. 2016; F. Aubin et al. 2021; N. Andres et al. 2022; C. All  n   et al. 2025), PYCBC (S. A. Usman et al. 2016; A. H. Nitz et al. 2017, 2018; T. Dal Canton et al. 2021), and the cWB analysis (S. Klimenko et al. 2005, 2008, 2016; V. Tiwari et al. 2016; M. Drago et al. 2021; S. Klimenko 2022; T. Mishra et al. 2021, 2022, 2025). Injections were added to data at an artificially higher rate than observed GW signals, and were used to quantify the pipelines’ sensitivities to GW signals (R. Essick et al. 2025; A. G. Abac et al. 2026a). The distribution of injections was chosen to enable efficient and accurate resampling to a wide range of astrophysically plausible populations (R. Essick et al. 2025). For all the analyses in this paper, the detection efficiency  $\xi(\Lambda)$  is estimated using these injections through a Monte Carlo integral (V. Tiwari 2018; W. M. Farr 2019; A. G. Abac et al. 2026a).

### 3.4. Source Properties

Parameter estimation (PE) pipelines use Bayesian inference to estimate the properties of GW events (A. G. Abac et al. 2026a). The hierarchical Bayesian inference framework described in Section 2 requires as input PE samples from individual events. For events detected in O4a, we use samples drawn from the posterior distribution using the NRSUR7DQ4 (V. Varma et al. 2019) waveform approximant if available. If these are not available, e.g., because the signal duration is too long to be analyzed by NRSUR7DQ4, we instead use a mixture of samples from the IMRPHENOMXPHM\_SPINTAYLOR (G. Pratten et al. 2021; M. Colleoni et al. 2025) and SEOBNR5PHM (L. Pompili et al. 2023; A. Ramos-Buades et al. 2023) approximants. These are referred to as MIXED samples in the PE data products. More details about various choices made in the PE procedure can be found in Section 5 of A. G. Abac et al. (2026a) and Section 3 of A. G. Abac et al. (2026b).

For all events detected before O4a, we use the MIXED samples reported in the GWTC-3.0 (R. Abbott et al. 2023b) and GWTC-2.1 (R. Abbott et al. 2024) data releases. One exception is the BNS merger GW170817, for which we use samples obtained with the IMRPHENOMPV2\_NRTIDAL waveform approximant (T. Dietrich et al. 2019) and a prior allowing for large spin magnitudes (B. P. Abbott et al. 2019c). We also reweight these samples to a distance prior that is uniform in comoving volume and source-frame time following the prescription in Appendix C of R. Abbott et al. (2021b).

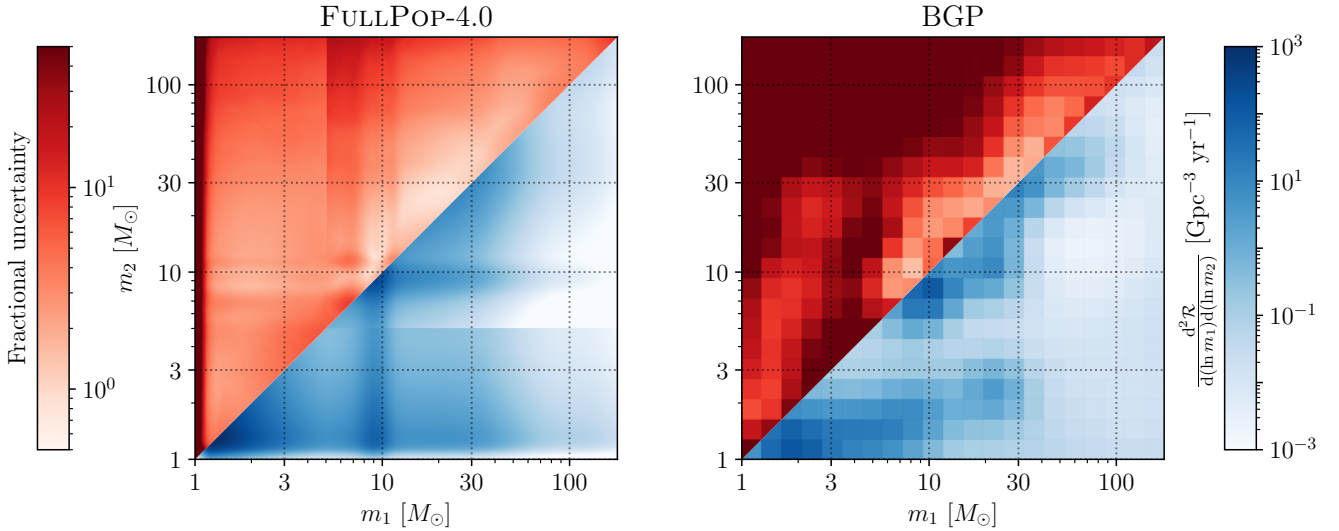
While this work was in its final stages, a normalization error was discovered in the noise-weighted inner product used in the PE likelihood function (C. Talbot et al. 2025b; A. G. Abac et al. 2026a). For events in O4a, we use a version of the PE samples that account for the correct likelihood (C. Talbot et al. 2025b; A. G. Abac et al. 2026a); events earlier to O4a are not expected to be impacted significantly due to this error (see Section 5.10 of A. G. Abac et al. 2026a). Further, for candidates detected during the first three observing runs, we discovered that incorrect priors were used when marginalizing over the uncertainty in the calibration of the LIGO detectors (A. G. Abac et al. 2026a). Preliminary reanalysis indicates that for each candidate the impact of this error in marginalization is small, and we expect the impact on our population analyses to be negligible compared to other sources of systematic error.

## 4. Binary Merger Population across All Masses

We begin our analysis of the astrophysical distribution of merging compact binaries with a joint analysis of all events discussed in Section 3—BNSs, NSBHs, and BBHs—without distinguishing between these different source classes. This allows for a broad look at the complete population, self-consistent measurements of the merger rates in each binary source class, and an analysis of the population at the transition between NSs and BHs. As mentioned in Section 3, we adopt a uniform detection threshold of  $\text{FAR} < 0.25 \text{ yr}^{-1}$  to ensure a high catalog purity of NS systems, where we have fewer detections and so are more sensitive to nonastrophysical false-alarm contaminants.

### 4.1. The Mass Spectrum of Compact Binaries

In Figure 1 we show the joint primary and secondary-mass distributions, inferred using a strongly modeled and a weakly



**Figure 1.** The complete mass spectrum, inferred using the strongly modeled FULLPOP-4.0 and weakly modeled BGP analyses. In the lower triangle of the  $m_1$ – $m_2$  plane (where  $m_1 > m_2$  by definition), we show median merger rate density across primary and secondary masses. At  $m_2 = 5 M_\odot$ , the FULLPOP-4.0 model transitions to an alternative pairing function to allow for NSBHs, hence the discontinuity at  $m_2 = 5 M_\odot$ . In the upper triangle we show the fractional uncertainty in the merger rate reflected across the diagonal. The fractional uncertainty  $\Delta\mathcal{R}/\mathcal{R}$  is the difference of the 95th and 5th percentile values divided by the median merger rate. Both the FULLPOP-4.0 and BGP models show similar broad features: a population of BNSs at primary and secondary masses  $\lesssim 2 M_\odot$ , a population of NSBHs at primary mass  $\sim 9 M_\odot$  and secondary mass  $\lesssim 2 M_\odot$ , and finally the population of BBHs with primary and secondary masses  $\gtrsim 9 M_\odot$ . The uncertainties are the smallest in the  $\sim 9 M_\odot$  and  $\sim 30 M_\odot$  BBH peaks.

modeled approach. Our FULLPOP-4.0 strongly modeled approach is modified from the POWER LAW + DIP + BREAK analysis of the previous GWTC-3.0 catalog (M. Fishbach et al. 2020; A. M. Farah et al. 2022; R. Abbott et al. 2023a; U. Mali & R. Essick 2025); see Appendix B.1 for a model description. Our weakly modeled analysis approximates the  $m_1$ – $m_2$  space with a BGP (I. Mandel et al. 2017; R. Abbott et al. 2023a; A. Ray et al. 2023a, 2025); see Appendix C.2 for further discussion. The FULLPOP-4.0 model uses the default models in Table 1 for the redshift and component spins, and for NS masses ( $m < 2.5 M_\odot$ ) the spin magnitude distribution is truncated over the range  $\chi \in [0, 0.4]$ . The BGP analysis fixes the POWER LAW REDSHIFT evolution to  $\kappa = 3$  (see Appendix B.4), and the spin distribution to be uniform in magnitude (again truncated over  $\chi \in [0, 0.4]$  for NS masses) and isotropic in orientation.

We observe an enhanced merger rate around  $m_1 \sim m_2 \lesssim 2 M_\odot$ , consistent with BNS systems, an additional subpopulation at unequal masses  $m_1 \sim 9 M_\odot$  and  $m_2 \lesssim 2 M_\odot$  consistent with NSBHs, and a third BBH subpopulation at  $m_1, m_2 \gtrsim 9 M_\odot$ . In the upper triangle of Figure 1, we show the fractional uncertainty as a function of mass, a unitless quantity  $\Delta\mathcal{R}/\mathcal{R}$  defined as the 95th–5th percentile uncertainty divided by the median merger rate. The rate is best constrained at equal masses, where the majority of mergers are observed, and in the BBH range  $10$ – $40 M_\odot$ . Due to fewer observations, the uncertainty is larger for BNS and NSBH systems.

In Figure 2, we show the marginalized primary and secondary-mass distributions for our strongly and weakly modeled reconstructions of the merger rate, focusing on the transition between NSs and BHs. The models are consistent within uncertainties, indicating that systematic error from model assumptions are smaller than the statistical uncertainties. The most notable difference between the FULLPOP-4.0 and BGP results is the large uncertainty in the BGP primary-mass distribution relative to the secondary mass. There are significantly more observed CBCs with light secondary masses

$m_2 \lesssim 15 M_\odot$  than primary masses  $m_1 \lesssim 15 M_\odot$  (simply by the definition  $m_2 < m_1$ ), and so the data-driven BGP is more uncertain for small primary masses, while the FULLPOP-4.0 results are more model driven.

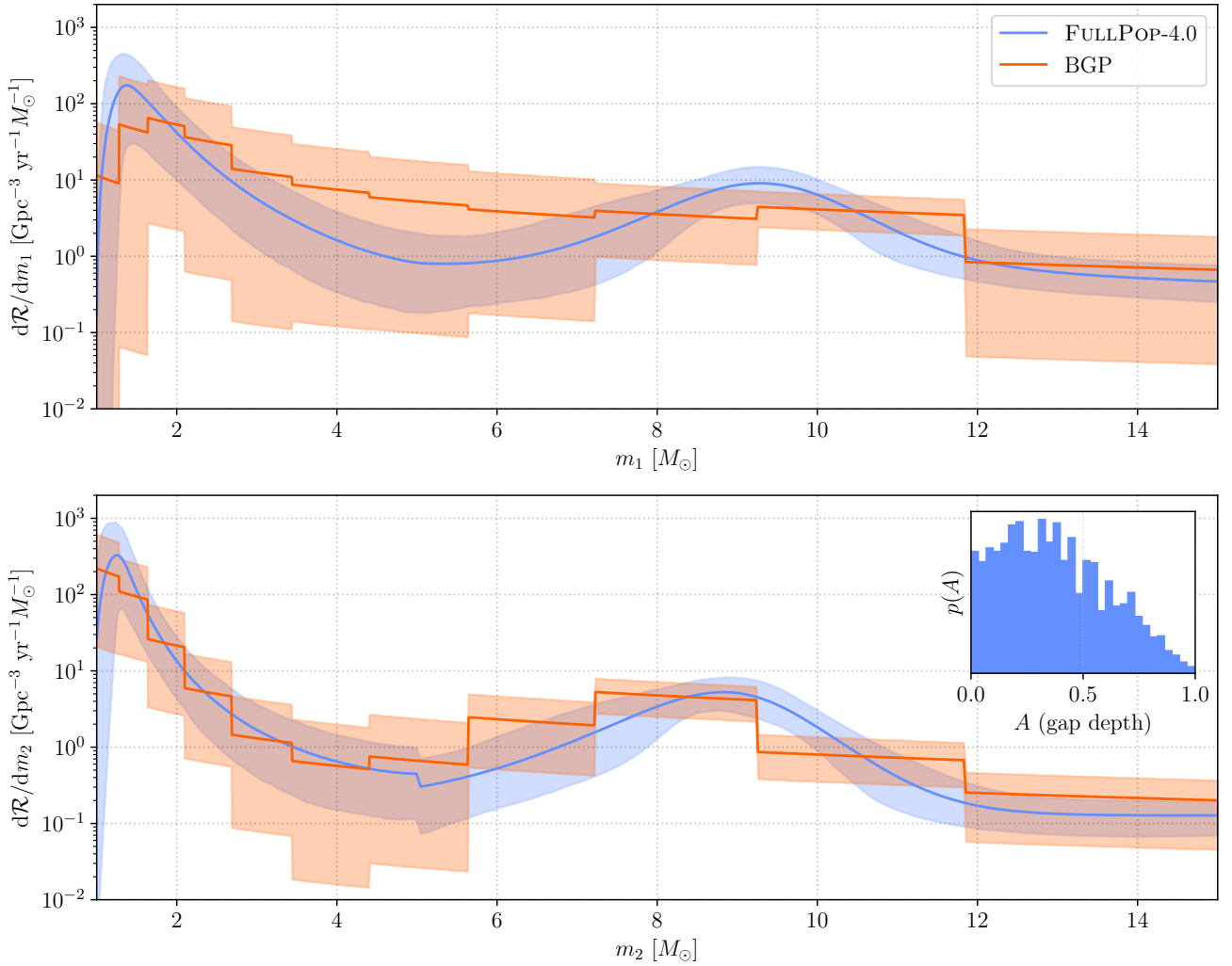
At  $m_2 = 5 M_\odot$ , the FULLPOP-4.0 model adopts an alternative pairing function to more naturally distinguish the pairing behavior of BNS and NSBH systems from that of BBH systems, introducing a discontinuity in the secondary-mass distribution (Figure 2) at the transition point. We discuss the behavior of the population at the transition from NSs to BHs and the astrophysical insights below in Section 4.3.

#### 4.2. Merger Rates

Since we self-consistently include all events in the catalog, our measurements of the binary merger rates are robust to events that straddle different source classes. We calculate the rates of BNS, NSBH, and BBH mergers by assuming any object with mass  $1 M_\odot < m < 2.5 M_\odot$  is an NS, and any object with mass  $m > 2.5 M_\odot$  is a BH. In all models, we assume the rate evolves with redshift in a manner that is uncorrelated with mass (M. Fishbach et al. 2018; R. Abbott et al. 2023a). We quote merger rates in the local Universe, at redshift  $z = 0$ .

Our strongly modeled FULLPOP-4.0 and weakly modeled BGP approaches infer different rates over the  $m_1$ – $m_2$  space, and hence different rates in each binary source class. To marginalize over the systematic modeling uncertainty, we take the union of both 90% credible intervals. The rates thus obtained are  $8.8$ – $250 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for BNS mergers,  $9.3$ – $86 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for NSBH mergers, and  $13$ – $26 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for BBH mergers. In Table 2, we show rates in these classes using different models and within purported mass gaps.

The BNS merger rate measurements may be sensitive to assumptions about NS pairing, and so we also estimate the BNS merger rate assuming a simple, fixed population. We assume a uniform mass distribution between  $1 M_\odot$  and  $2.5 M_\odot$  for the component masses, isotropically distributed spins with



**Figure 2.** A comparison of the merger rate at redshift  $z = 0$ , as a function of component mass for the FULLPOP-4.0 and BGP models. In the upper panel, we show the merger rate as a function of primary mass, marginalized over secondary mass. In the lower panel, we show the merger rate as a function of the secondary mass, marginalized over the primary mass. At  $m_2 = 5 M_\odot$ , the FULLPOP-4.0 model transitions to an alternative pairing function to allow for NSBHs, hence the discontinuity in the secondary mass. The median of the inferred merger rate is shown with a solid line, and the 90% credible interval is shown in the shaded region. The BGP weakly modeled approach has larger uncertainties due to increased flexibility. Both the strongly modeled and weakly modeled approaches find local maxima in the merger rate at  $m_2 \sim 1\text{--}2 M_\odot$  and  $m_2 \sim 6.5\text{--}9 M_\odot$  in the secondary-mass distribution. However, the BGP model does not confidently recover the low mass peaks in the primary-mass distribution. In the inset, we show the FULLPOP-4.0 inferred gap depth parameter  $A$  (see Appendix B.1), where  $A = 1$  (a completely empty gap) is disfavored.

**Table 2**  
Merger Rates in Units of  $\text{Gpc}^{-3} \text{yr}^{-1}$  in Different Mass Ranges, According to the FULLPOP-4.0 and BGP Models

|                    | BNS<br>$m_1 \in [1, 2.5] M_\odot$<br>$m_2 \in [1, 2.5] M_\odot$ | NSBH<br>$m_1 > 2.5 M_\odot$<br>$m_2 \in [1, 2.5] M_\odot$ | BBH<br>$m_1 > 2.5 M_\odot$<br>$m_2 > 2.5 M_\odot$ | NS-Gap<br>$m_1 \in [2.5, 5] M_\odot$<br>$m_2 \in [1, 2.5] M_\odot$ | BH-Gap<br>$m_1 > 2.5 M_\odot$<br>$m_2 \in [2.5, 5] M_\odot$ | Full<br>$m_1 > 1 M_\odot$<br>$m_2 > 1 M_\odot$ |
|--------------------|-----------------------------------------------------------------|-----------------------------------------------------------|---------------------------------------------------|--------------------------------------------------------------------|-------------------------------------------------------------|------------------------------------------------|
| FULLPOP-4.0        | $92^{+157}_{-69}$                                               | $22^{+20}_{-12}$                                          | $18^{+7}_{-5}$                                    | $6.8^{+10.3}_{-4.7}$                                               | $2.4^{+3.3}_{-1.6}$                                         | $130^{+170}_{-80}$                             |
| BGP                | $51^{+118}_{-42}$                                               | $33^{+53}_{-23}$                                          | $20^{+7}_{-5}$                                    | $17^{+48}_{-15}$                                                   | $1.6^{+5.3}_{-1.4}$                                         | $110^{+130}_{-60}$                             |
| Merged             | 8.8–250                                                         | 9.3–86                                                    | 13–26                                             | 1.6–64                                                             | 0.2–7.0                                                     | 51–300                                         |
| SIMPLE UNIFORM BNS | 13–170                                                          | ...                                                       | ...                                               | ...                                                                | ...                                                         | ...                                            |

**Note.** For BNS systems, we also estimate the rate assuming a SIMPLE UNIFORM BNS model. We show rates of BNS, NSBH, and BBH assuming objects with mass  $m \in [1, 2.5] M_\odot$  are NSs and  $m > 2.5 M_\odot$  are BHs. We also show rates within the purported lower-mass gap between astrophysical NSs and BHs, according to these models. In the third row, we show the merged estimates, taking the union of the 90% credible intervals for the FULLPOP-4.0 and BGP models, in order to account for model systematics. We quote merger rates at redshift  $z = 0$ .

uniform spin magnitudes below 0.4, and a merger rate uniform in comoving volume up to  $z = 0.15$ . Under this fiducial model (denoted SIMPLE UNIFORM BNS in Table 2), we infer a BNS merger rate of  $13\text{--}170 \text{ Gpc}^{-3} \text{yr}^{-1}$ .

The estimates in Table 2 are consistent with our previous analysis (R. Abbott et al. 2023a) and the uncertainties on the rate in each source class have generally decreased due to our larger catalog size. Although it is within uncertainties, our

inferred merger rate for BNS systems has notably decreased by a factor of  $\sim 2$  (see Power law+Dip+Break (PDB; pair) and BGP in Table 2 of R. Abbott et al. 2023a). This is a result of the improved detector range and observing time together with the lack of new BNS detections.

#### 4.3. The Neutron Star–Black Hole Transition

Electromagnetic (EM) observations have previously suggested the existence of a mass gap between NSs and BHs (C. D. Bailyn et al. 1998; F. Ozel et al. 2010; W. M. Farr et al. 2011). On the lower end of the gap, nonrotating NS masses are bounded by a physical limit, the Tolman–Oppenheimer–Volkoff (TOV) mass (e.g., V. Kalogera & G. Baym 1996). Astrophysical observations, heavy-ion collision experiments, and modeling of the dense matter equation of state (EoS) at nuclear densities bound  $M_{\text{max,TOV}} \sim 2.2\text{--}2.5 M_{\odot}$  (T. Dietrich et al. 2020; P. Landry et al. 2020; I. Legred et al. 2021; S. Huth et al. 2022; S. Ai et al. 2023; A. J. Dittmann et al. 2024; N. Rutherford et al. 2024; H. Koehn et al. 2025), and studies on the remnant in the BNS merger GW170817 (B. P. Abbott et al. 2017) place limits in the range  $\lesssim 2.3 M_{\odot}$  (B. Margalit & B. D. Metzger 2017; L. Rezzolla et al. 2018; M. Ruiz et al. 2018; B. P. Abbott et al. 2020b; A. Nathanail et al. 2021).

On the upper end of the gap, electromagnetic (EM) observations historically identified a dearth of BHs in the range  $\sim 3\text{--}5 M_{\odot}$  (C. D. Bailyn et al. 1998; F. Ozel et al. 2010; W. M. Farr et al. 2011), hinting at an astrophysical mass gap between NSs and BHs, or perhaps a selection effect obscuring such objects. More recently, observations of noninteracting binary systems (T. A. Thompson et al. 2018; T. Jayasinghe et al. 2021) and radio pulsar surveys (E. D. Barr et al. 2024) suggest the presence of a population of compact objects within the gap. Indeed, the GW events GW190814 (R. Abbott et al. 2020c) and GW230529 (A. G. Abac et al. 2024) are further evidence that the transition between NSs and BHs is populated, albeit sparsely.

With the additional GWTC-4.0 data, the GW picture of the purported lower-mass gap is becoming clearer and structures around the transition from NSs to BHs are emerging. In both our strongly modeled FULLPOP-4.0 and weakly modeled BGP analyses, we find evidence for a prominent pair of peaks at NS masses  $\sim 1.5 M_{\odot}$  and at BH masses  $\sim 9 M_{\odot}$  on each side of the lower-mass gap. A completely empty gap between NSs and BHs is disfavored. We cannot rule out the existence of extremely narrow gaps in the compact object spectrum, though such a feature requires fine tuning of the supernova explosion mechanism, fallback, binary interactions, or other physical processes (e.g., K. Belczynski et al. 2012; C. L. Fryer et al. 2012).

Our FULLPOP-4.0 model detects a peak in the BH merger rate at  $9.09^{+0.376}_{-0.778} M_{\odot}$ . We find that merging NSs represent the global maximum of the compact object mass spectrum at  $1.22^{+0.133}_{-0.143} M_{\odot}$ . At the transition from NSs to BHs, FULLPOP-4.0 allows for an additional suppression in the merger rate, parameterized by a gap depth parameter  $A$ , where  $A = 1$  corresponds to an absolute gap with zero mergers and  $A = 0$  corresponds to no additional suppression. We show the measurement on  $A$  in the inset in Figure 2.  $A$  is consistent with zero, and the lower and upper bounds of the gap (e.g., the maximum NS mass and the minimum BH mass) are not measured away from the prior.

Earlier precursor analyses to FULLPOP-4.0 showed that the merger rate between  $\sim 3\text{--}5 M_{\odot}$  is likely suppressed relative to a power-law continuum (M. Fishbach et al. 2020; R. Abbott et al. 2021a; A. M. Farah et al. 2022), using older datasets. In R. Abbott et al. (2023a), we used a strongly modeled analysis on GWTC-3.0 (compare the PDB model to FULLPOP-4.0) to argue that the transition from NSs to BHs is likely suppressed, but also may be partially filled. FULLPOP-4.0 measures a similar mass spectrum to these previous analyses, but reinterprets the data as evidence for a rise at  $\sim 9 M_{\odot}$ , and no *additional* suppression between the NS and BH peaks (U. Mali & R. Essick 2025 make similar conclusions on GWTC-3.0).

We corroborate our strongly modeled FULLPOP-4.0 conclusions with a weakly modeled BGP approach, and our constraints are improved relative to a similar BGP-based model in R. Abbott et al. (2023a). Unlike the FULLPOP-4.0 model, however, the BGP analysis does not distinguish between peaks, gaps, or a continuum: as a weakly modeled approach, the shape of the population is inferred directly without an associated interpretation.

The BGP model infers a nonzero merger rate between the NS to BH peaks consistent with an underlying continuum and no evidence for a sharp gap. However, the smoothing kernel in the BGP model makes it a priori less sensitive to deep gaps, so we cannot rule them out either. The BGP model also observes NS and BH peaks. We quantify the significance as the fraction of hyperparameter samples where the merger rate density is higher than the merger rate in the neighboring bins. The merger rate maximizes for NSs in the range  $1 M_{\odot} \leq m_2 \leq 2 M_{\odot}$  at 99% credibility and the low-mass BH peak occurs in the secondary mass  $7.5 M_{\odot} \leq m_2 \leq 9 M_{\odot}$  bin at 97% credibility.

As our knowledge improves about the compact object population at the boundary between NSs and BHs, we stand to learn about supernova physics (e.g., A. Burrows & D. Vartanyan 2021) and the formation mechanisms of the heaviest NSs and lightest BHs (A. G. Abac et al. 2024, and references therein). If future catalogs continue to disfavor a completely empty gap, the standard picture of rapid core-collapse supernovae—which features a sharp transition in remnant masses; successful explosions leave NSs with  $m \lesssim 2 M_{\odot}$  and failed explosions promptly collapse to BHs with  $m \gtrsim 5 M_{\odot}$  (e.g., C. L. Fryer & V. Kalogera 2001; C. L. Fryer et al. 2012)—may require modifications to include fallback, slower instability growth, or stochasticity (e.g., C. L. Fryer & V. Kalogera 2001; K. Belczynski et al. 2012; C. L. Fryer et al. 2012; T. Sukhbold et al. 2016; T. Ertl et al. 2019; I. Mandel & B. Müller 2020). Fallback of stellar material can produce black holes from the maximum NS mass to the lightest BH mass ( $\sim 6 M_{\odot}$ ) in the rapid implosion scenario (e.g., T. Ertl et al. 2019), or a slower instability growth timescale could allow the proto-NS to accrete enough mass before the explosion to populate the mass gap (e.g., K. Belczynski et al. 2012; C. L. Fryer et al. 2022; A. Olejak et al. 2022). Another possibility is that stochasticity in the stellar evolution and supernovae smooths out the remnant mass distribution and occupies the lower-mass gap (e.g., I. Mandel & B. Müller 2020; I. Mandel et al. 2020). Alternatively, the gap between NSs and BHs may be populated by a pollution mechanism such as the remnants of BNS or white dwarf collisions, which participate in further hierarchical mergers (HMs; e.g., A. Gupta et al. 2020; C. S. Ye et al. 2020, 2024; E. D. Barr et al. 2024; P. Mahapatra et al. 2025a), or other exotic scenarios like primordial black holes (e.g.,

S. Clesse & J. Garcia-Bellido 2022) or gravitationally lensed events, which could be mistaken for mass gap objects (e.g., M. Bianconi et al. 2023; J. Janquart et al. 2024; A. Farah et al. 2026).

## 5. Population Properties of Mergers Containing Neutron Stars

In O4a, GW230529 (A. G. Abac et al. 2024) is the only NS-containing event identified with a FAR  $< 0.25 \text{ yr}^{-1}$ . We do not include the NSBH candidate GW230518 identified during the ER preceding O4a. Additionally, no coincident EM counterparts were identified for triggers (i.e., preliminary candidate GW signals flagged by the detection pipelines when their ranking statistic exceeded the alert threshold) during O4a based on follow-up efforts conducted by EM telescopes. Thus, conclusions presented in previous papers (R. Abbott et al. 2023a; A. G. Abac et al. 2024) about the population properties of BNS and NSBH mergers remain largely unchanged.

We adopt models and methods consistent with those used in GWTC-3.0 (R. Abbott et al. 2023a). Specifically, we adopt two different models for the NS mass distribution, one in which masses are assumed to be Gaussian distributed, and another in which they are assumed to follow a power law (R. Abbott et al. 2023a). These are referred to as the PEAK model and the POWER model, respectively. We assume that the redshift evolution of the merger rate is fixed and that the spins are distributed following the PE prior (A. G. Abac et al. 2026a). A uniform prior is used for hyperparameters of the population, with the condition  $m_{\min} \leq \mu \leq m_{\max}$  (where  $\mu$  is the mean of the Gaussian bump in the PEAK model), assuming  $m_{\max}$  does not exceed  $M_{\max, \text{TOV}}$  (the maximum permissible NS mass as expected from the TOV limit), as detailed in Appendix B.

When assumed to follow the POWER model, NS masses favor a mass distribution with a power-law slope constrained to  $\alpha = 7.9^{+4.8}_{-5.0}$ . The inference from the PEAK model is broad, with largely unconstrained peak width  $\sigma = 0.65^{+1.2}_{-0.42} M_{\odot}$  and location  $\mu = 1.4^{+0.45}_{-0.24} M_{\odot}$ . While these results may hint at a peak emerging near  $1.4 M_{\odot}$ , it is much broader than the relatively sharp peak in the mass distribution of Galactic NS systems (N. Farrow et al. 2019; K. El-Badry et al. 2024). Our inferred NS mass distribution remains broad, with greater support for high-mass NSs.

As no new NSBHs beyond GW230529 were confidently observed in O4a, the population-level results in A. G. Abac et al. (2024) produced using the NSBHPOP model (S. Biscoveanu et al. 2022b) remain unchanged. Specifically, our inferred minimum BH mass in NSBH systems remains  $3.4^{+1.0}_{-1.2} M_{\odot}$  (A. G. Abac et al. 2024).

## 6. Binary Black Hole Population

In this section, we analyze the astrophysical population of BBHs using data from GW events with a FAR  $< 1 \text{ yr}^{-1}$ . We only include events whose 1% lower limit on both component mass posteriors (under the PE priors) is larger than  $3 M_{\odot}$ . There are 84 events from O4a that meet this criterion in addition to the 69 BBH events from GWTC-3.0, which brings the total number of BBH events passing our FAR threshold to 153. Of the events considered in O4a, only GW230529 does not meet this criterion and is not considered in the analyses below (see Section 3).

### 6.1. Primary Mass

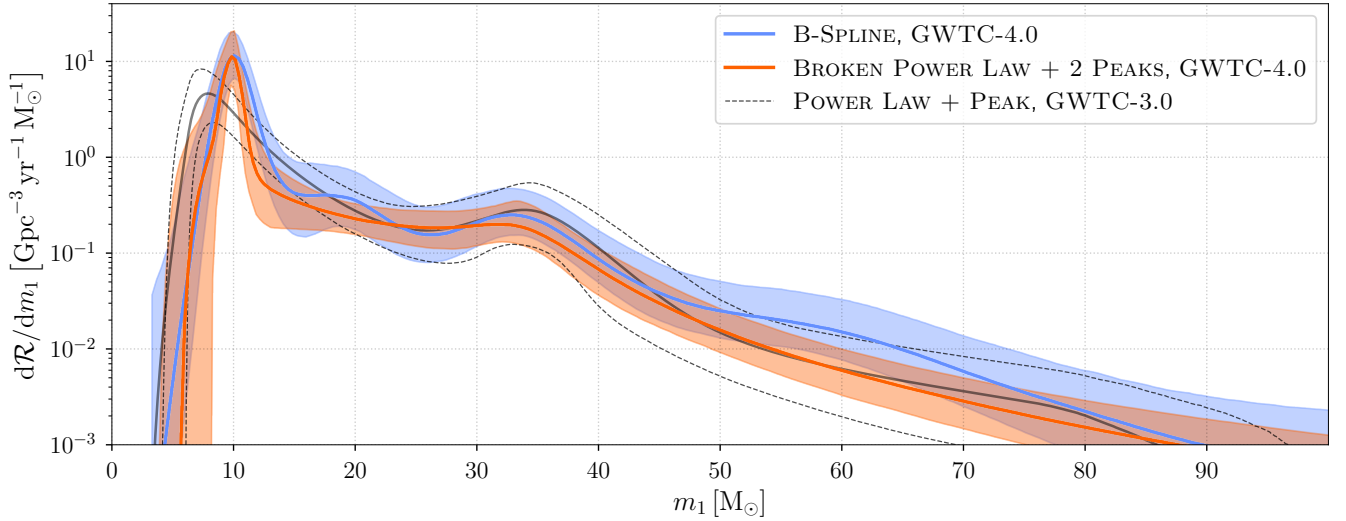
In this section, we illustrate the main findings of the strongly and weakly modeled approaches using results from the BROKEN POWER LAW + 2 PEAKS (see Appendix B.3) and B-SPLINE (see Appendix C.1) models, respectively. We chose the BROKEN POWER LAW + 2 PEAKS model as our fiducial mass model through various considerations in our model comparison study. It was first introduced by T. A. Callister & W. M. Farr (2024) to describe the GWTC-3.0 mass distribution. Results from a selection of other models considered in the model comparison study can be found in Appendix D.1, while models that employ a weakly modeled approach can be found in Appendix D.4, both of which include comparisons to the fiducial BROKEN POWER LAW + 2 PEAKS and B-SPLINE models. The strongly modeled approach employs the default models listed in Table 1 for the other source parameters, namely the POWER LAW REDSHIFT and GAUSSIAN COMPONENT SPINS models.

We identify a global peak at  $\sim 10 M_{\odot}$  and find that it is robust to model variations. A Gaussian-like peak at  $\sim 10 M_{\odot}$  was first identified by V. Tiwari & S. Fairhurst (2021) and B. Edelman et al. (2022) using GWTC-2.0 and later by the weakly modeled approaches in R. Abbott et al. (2023a) using GWTC-3.0. Figure 3 shows the rate  $d\mathcal{R}/dm_1$  as a function of primary mass at  $z = 0.2$  inferred by these models compared to the POWER LAW + PEAK (see Appendix B of R. Abbott et al. 2023a for a description of this model) inference with GWTC-3.0 from R. Abbott et al. (2023a).<sup>328</sup> The low-mass Gaussian component of the BROKEN POWER LAW + 2 PEAKS model infers a global peak in the primary mass spectrum at  $m_1 = 9.8^{+0.3}_{-0.6} M_{\odot}$  relative to the underlying broken power-law continuum. The B-SPLINE model also recovers a global peak at  $m_1 = 10.1^{+0.7}_{-0.7} M_{\odot}$ . Both values are consistent with GWTC-3.0, which inferred a global peak at  $m_1 = 10.2^{+0.3}_{-0.6} M_{\odot}$  by modeling the mass spectrum as a power law modulated by a spline.

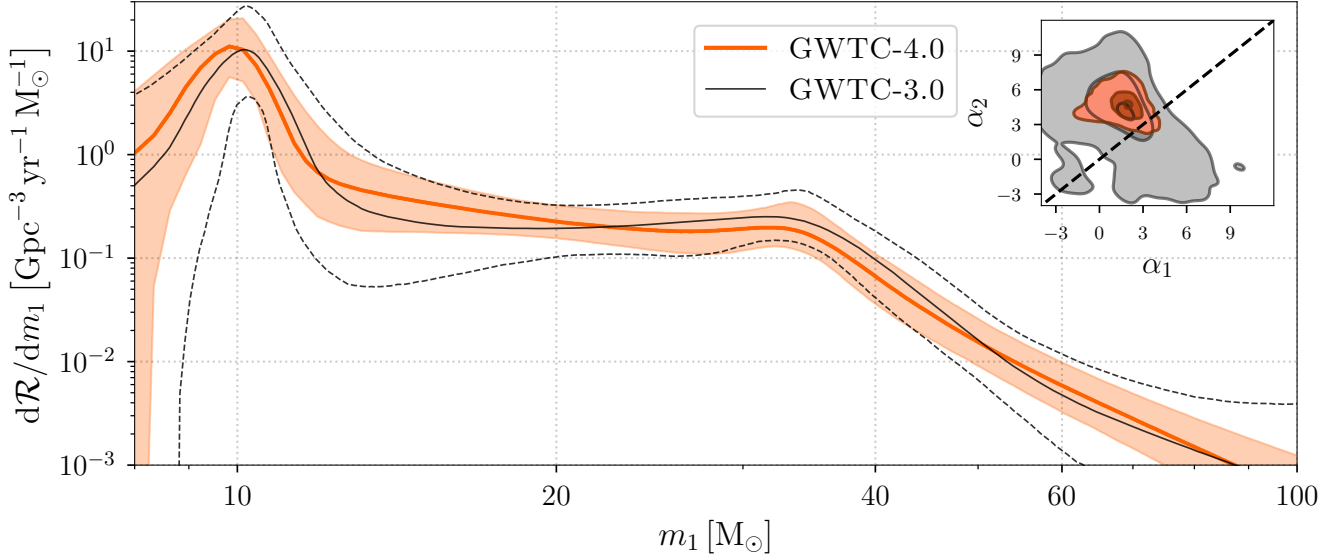
A broken power law is necessary to describe the continuum structure above  $\sim 15 M_{\odot}$  (see Figure 3). Below  $\sim 35 M_{\odot}$ , the continuum of BH masses is well described by a power law with spectral index  $\alpha_1 = 1.8^{+1.3}_{-2.0}$ . Above  $\sim 35 M_{\odot}$ , the continuum steepens, with a spectral index of  $\alpha_2 = 4.7^{+1.7}_{-1.4}$  that is consistent with the POWER LAW + PEAK result from GWTC-3.0 ( $\alpha = 3.5^{+0.6}_{-0.6} M_{\odot}$ ). We find that  $\alpha_2 > \alpha_1$  at 97% credibility. Though this continuum structure was identified by T. A. Callister & W. M. Farr (2024), it was not identified by the strongly modeled approaches in R. Abbott et al. (2023a), in part due to the limited flexibility of models employed in R. Abbott et al. (2023a). To illustrate this, in Figure 4 we present a reanalysis of GWTC-3.0 using the BROKEN POWER LAW + 2 PEAKS model alongside the GWTC-4.0 result, which shows improved constraints across the full mass spectrum.

We identify a feature at  $\sim 35 M_{\odot}$ . Using the strongly modeled approach, we find that this feature is consistent with either (i) an overdensity that peaks at  $m_1 = 32.1^{+3.0}_{-6.8} M_{\odot}$  relative to an underlying broken power law (i.e., the BROKEN POWER LAW + 2 PEAKS result) or (ii) a broken power law with break mass  $m_{\text{break}} = 34.1^{+3.7}_{-3.4} M_{\odot}$  (i.e., a broken power law without a second peak near the break). See Appendix D.1 for a more detailed discussion of this result. The former conclusion is supported by the B-SPLINE model, which

<sup>328</sup> We quote BBH merger rates at  $z = 0.2$  to be consistent with R. Abbott et al. (2023a) and because  $z \sim 0.2$  is where we best constrain the merger rate.



**Figure 3.** Differential merger rate as a function of primary mass (evaluated at  $z = 0.2$ ) of the BROKEN POWER LAW + 2 PEAKS model (orange) and B-SPLINE model (blue) compared to the POWER LAW + PEAK model from GWTC-3.0 (R. Abbott et al. 2023a). The solid lines indicate the posterior medians and the shaded regions show the 90% credible interval of each model. Comparing these results, it is clear that a single power law is a poor description of the the low-mass end of the spectrum.



**Figure 4.** Differential merger rate as a function of primary mass (evaluated at  $z = 0.2$ ) of the BROKEN POWER LAW + 2 PEAKS model inferred with GWTC-4.0 compared to the same model applied to only GWTC-3.0 BBH events. The orange shaded region shows the 90% credible interval for GWTC-4.0 and the solid orange curve shows the posterior median, while the black dashed curves bound the 90% credible region for GWTC-3.0 and the solid black curve shows the posterior median. The inferred distribution is similar between catalogs, which highlights that the low-mass structure identified in GWTC-4.0 was present in GWTC-3.0. The inset figure shows the joint posterior of the broken power-law index parameters  $\alpha_1$  and  $\alpha_2$  for GWTC-3.0 (gray) and GWTC-4.0 (orange), with the contours showing the 5th, 50th, and 95th percentiles. The black dashed curve in the inset indicates where  $\alpha_1 = \alpha_2$ .

exhibits a local peak at  $m_1 = 32.7^{+2.6}_{-4.1} M_\odot$ , consistent with other models that employ a weakly modeled approach in Appendix D.4.

Additional structure may be present in the mass spectrum. A bump near  $\sim 20 M_\odot$  is present in some of the weakly modeled approaches (see Figure 20 in Appendix D.4). We cannot conclude with the strongly modeled approach whether adding a third Gaussian component to the BROKEN POWER LAW + 2 PEAKS model in this region is required by the data or not (as quantified by the log Bayes factor  $\log_{10} \mathcal{B} = -2.20$  between the default model and one including a third peak). This feature was first reported in an analysis of GWTC-2.0 (V. Tiwari & S. Fairhurst 2021) and was present in several analyses of

GWTC-3.0 (R. Abbott et al. 2023a; B. Edelman et al. 2023; V. Tiwari 2023; J. Godfrey et al. 2023). Additionally, the B-SPLINE and other weakly modeled approaches show a rise in the merger rate relative to the BROKEN POWER LAW + 2 PEAKS result in the  $\sim 60 M_\odot$  region, which can be seen in Figures 3 and 20. A previous study of GWTC-3.0 found evidence for a similar feature in this region (I. Magaña Hernandez & A. Palmese 2025).

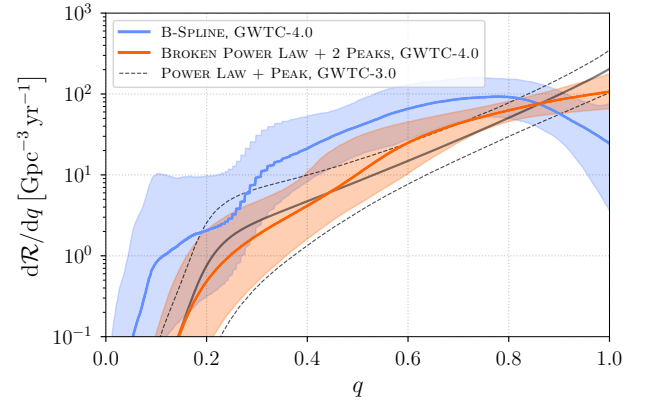
We do not place informative constraints on the individual parameters that govern low-mass smoothing for the BROKEN POWER LAW + 2 PEAKS model. We caution against astrophysically interpreting the BBH primary mass distribution below  $\sim 8 M_\odot$  because of the bias that may be introduced by

removing the probable NS-containing events in the manner described in Section 3. Removing such events is responsible for the discrepancy below  $\sim 8 M_\odot$  between Figures 2 and 3.

GWTC-4.0 includes an exceptionally high-mass BBH, GW231123 (A. G. Abac et al. 2025b), whose inferred component masses lie at the extreme upper end of those in our dataset. To check if GW231123 is an outlier with respect to the mass distribution of BBHs, we construct mock catalogs containing 153 detected events following the inferred population without GW231123 and calculate the distribution of maximum detectable BH masses. The total mass of GW231123 lies at the  $90^{+4}_{-10}$  percentile of this distribution. This shows that while GW231123 lies in the tail of the distribution, its total mass is consistent with the inferred mass spectrum; the degree of consistency is more than was the case with GWTC-3.0 data alone (A. G. Abac et al. 2025b).

The main compact binary formation scenarios (I. Mandel & A. Farmer 2022 and references therein)—isolated binary evolution and dynamical assembly in dense stellar environments—have both been shown to produce populations consistent with current observations (I. Mandel & F. S. Broekgaarden 2022). A peak near  $m_1 \sim 10 M_\odot$  is often predicted by isolated binary evolution models (M. Dominik et al. 2015; N. Giacobbo & M. Mapelli 2018; G. Wiktorowicz et al. 2019; C. J. Neijssel et al. 2019; K. Belczynski et al. 2020), while mass distributions from dynamical formation, such as in young and globular clusters, typically peak above  $10 M_\odot$  (C. L. Rodriguez et al. 2016a; J. Hong et al. 2018; C. L. Rodriguez et al. 2019; F. Antonini & M. Gieles 2020; S. Banerjee 2021). However, predictions from isolated and dynamical formation often overlap and can vary significantly based on the assumptions and methodologies used, making it difficult to conclude the origin of the observed catalog or constrain formation physics based on features in the marginal mass distributions.

A feature that may provide distinguishing power between the isolated and dynamical channels is the existence of an upper mass gap, in the range  $45 M_\odot \lesssim m \lesssim 120 M_\odot$ . Such a dearth would be consistent with the theorized *pair-instability mass gap*, arising from the complete disruption of massive stars due to runaway electron–positron pair production (S. E. Woosley 2017; R. Farmer et al. 2019; M. Mapelli et al. 2020). While the precise locations of the lower and upper edges of the pair-instability mass gap are sensitive to physical assumptions (M. Renzo et al. 2020; L. A. C. van Son et al. 2020; S. E. Woosley & A. Heger 2021; Y. Shen et al. 2023; E. R. J. Winch et al. 2024), the feature tends to be a robust prediction of most stellar evolution models (P. Marchant et al. 2018; P. Marchant & T. Moriya 2020; M. Renzo et al. 2020; S. E. Woosley & A. Heger 2021). The gap may not be completely empty due to overmassive stellar envelope fallback or stellar mergers (U. N. Di Carlo et al. 2019, 2020; K. Kremer et al. 2020; M. Mapelli et al. 2020), hierarchical BBH mergers in clusters or in AGN environments (B. McKernan et al. 2018; F. Antonini et al. 2019; C. L. Rodriguez et al. 2019; Y. Yang et al. 2019; G. Fragione & J. Silk 2020; B. McKernan et al. 2020; M. A. S. Martinez et al. 2020; M. Arca Sedda 2020; B. Liu & D. Lai 2021; M. Mapelli et al. 2021; P. Mahapatra et al. 2021, 2024, 2025b), or even primordial BHs (K. A. Postnov & L. R. Yungelson 2014; S. Bird et al. 2016; S. Clesse & J. Garcia-Bellido 2022). The decrease in the merger rate above  $m_1 \sim 35 M_\odot$  seen in all models and the



**Figure 5.** Differential merger rate as a function of mass ratio (evaluated at  $z = 0.2$ ) of the BROKEN POWER LAW + 2 PEAKS model (orange) and B-SPLINE model (blue). The fiducial POWER LAW + PEAK model from R. Abbott et al. (2023a) is included for comparison. Solid curves indicate posterior medians and the shaded (dashed) regions show 90% credible intervals.

tentative rise near  $m_1 \sim 60 M_\odot$  seen in the weakly modeled approaches may hint toward a polluted mass gap.

## 6.2. Mass–Ratio

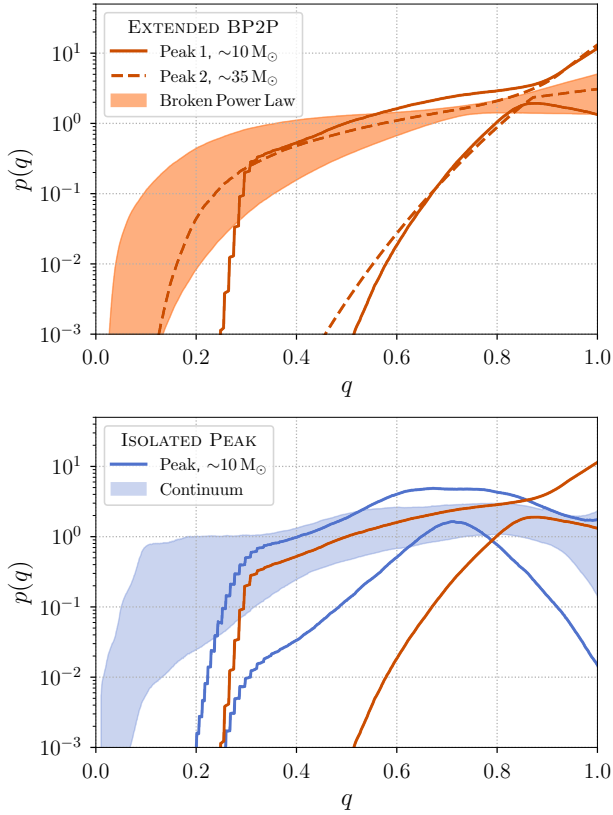
Figure 5 shows the differential merger rate  $d\mathcal{R}/dq$  evaluated at  $z = 0.2$  inferred by the BROKEN POWER LAW + 2 PEAKS and B-SPLINE models compared to the POWER LAW + PEAK result from GWTC-3.0.<sup>329</sup>

We find that the mass-ratio distribution can be described by a power law with an index  $\beta_q = 1.5^{+1.5}_{-1.1}$  that is consistent with GWTC-3.0 ( $\beta_q = 1.1^{+1.7}_{-1.3}$ ) with a reduction in uncertainty. The B-SPLINE model shows a reduced rate above  $q \gtrsim 0.8$  relative to the BROKEN POWER LAW + 2 PEAKS result. More flexible parameterizations in the strongly modeled approach were explored (see also the other weakly modeled approaches in Figure 20, which do peak near unity), but model comparisons were inconclusive. Similarly, in GWTC-3.0, J. Godfrey et al. (2023) inferred a mass-ratio distribution peaked away from unity using a weakly modeled approach, while S. Rinaldi et al. (2025) found equal evidence for two strongly modeled approaches with very distinct behavior above  $q \gtrsim 0.7$ .

Models that incorporate correlations between source parameters have a greater potential to distinguish between formation channels than uncorrelated ones. We next present results from two different models that correlate features of the primary mass spectrum with different mass-ratio distributions.

BHs with masses  $\sim 35 M_\odot$  preferentially merge with other BHs of more equal mass relative to those in the underlying mass continuum. The EXTENDED BROKEN POWER LAW + 2 PEAKS model modifies the BROKEN POWER LAW + 2 PEAKS model by allowing each primary mass mixture component (i.e., the broken power law and two Gaussian components) to be associated with a different power-law-mass-ratio distribution. Figure 6 shows the mass-ratio distribution for each mixture component. Specifically, each component infers a different power-law index  $\beta_q$ , with  $\beta_q^{\text{BP}} = 0.4^{+1.9}_{-1.4}$  for the broken power law,  $\beta_q^{\text{peak1}} = -0.0^{+9.0}_{-7.2}$  for the Gaussian component that captures the  $\sim 10 M_\odot$  peak, and

<sup>329</sup> Models that utilize B-Splines infer the separable distribution  $p(q)$  but the results of such models shown in this section are actually the conditional marginal distribution  $p(q|m_2 > 3M_\odot)$ . See Appendix C.1 for further details.



**Figure 6.** Top panel: the 90% credible regions for the mass-ratio distribution of the  $\sim 10 M_{\odot}$  peak (solid orange curves),  $\sim 35 M_{\odot}$  peak (dashed curves), and continuum (orange shaded region) components of the EXTENDED BROKEN POWER LAW + 2 PEAKS model. Bottom panel: the 90% credible regions for mass-ratio distribution of the  $\sim 10 M_{\odot}$  peak (solid blue curves) and the rest of the mass spectrum (blue shaded region) inferred with the ISOLATED PEAK model. The  $\sim 10 M_{\odot}$  peak mass-ratio distribution from the EXTENDED BROKEN POWER LAW + 2 PEAKS is included for comparison.

$\beta_q^{\text{peak2}} = 6.7^{+5.3}_{-4.7}$  for the second Gaussian component that captures the  $\sim 35 M_{\odot}$  feature. Critically,  $\beta_q^{\text{peak2}} > \beta_q^{\text{BP}}$  at 96.7% credibility. See Appendix D.1 for a more detailed discussion of this result. Other studies of GWTC-3.0 have drawn similar conclusions about the pairing preferences of high mass BHs (e.g., Y.-J. Li et al. 2022; V. Baibhav et al. 2023; J. Sadiq et al. 2024; S. Galadage & A. Lamberts 2025; S. K. Roy et al. 2025).

BHs with masses  $\sim 10 M_{\odot}$  may preferentially merge with lighter BHs. The region bounded by the solid blue curves in the bottom panel of Figure 6 shows the mass-ratio distribution of the  $\sim 10 M_{\odot}$  peak inferred with the ISOLATED PEAK model. This model is a mixture of a Gaussian peak and a B-Spline (continuum) in primary mass, and the mass ratio and spin distributions are inferred separately for each mixture component with B-Splines (see Appendix C for further details). The Gaussian peak is inferred at  $\sim 10 M_{\odot}$  and its mass-ratio distribution exhibits a peak at  $q = 0.71^{+0.12}_{-0.11}$ , a feature that a single power law is unable to reproduce. This could explain the large uncertainty in  $\beta_q^{\text{peak1}}$  from the EXTENDED BROKEN POWER LAW + 2 PEAKS model. The solid blue curve in Figure 6 shows the mass-ratio distribution of masses outside of the  $\sim 10 M_{\odot}$  peak inferred by the B-Spline mixture component. Unlike the full population mass-ratio distribution inferred by the B-SPLINE model in Figure 5, this result does not possess a peak near  $q \sim 0.8$ , indicating that the peak seen in the full

population is due largely to the events around  $\sim 10 M_{\odot}$ . This mass feature was identified in GWTC-3.0 by J. Godfrey et al. (2023).

Most formation channels generally favor equal mass systems. For example, dynamical formation can produce systems with a wide range of mass ratios, but predicted distributions typically peak at unity (C. L. Rodriguez et al. 2016a; S. Tormiamenti et al. 2024). Certain HMs may not necessarily follow this trend, in particular mergers between first generation and second generation BHs have been shown to produce a mass-ratio distribution peaked near  $q \sim 0.5$  (C. L. Rodriguez et al. 2019). Mass transfer during the contact phase of binaries formed via chemically homogeneous evolution (S. E. de Mink & I. Mandel 2016; P. Marchant et al. 2016) leads to a strong preference for equal mass-ratio systems, but this mechanism is thought to be important for binaries with  $m_1 \gtrsim 10 M_{\odot}$  (L. du Buisson et al. 2020; J. Riley et al. 2021; M. Zevin et al. 2021). Mass-ratio reversal within the stable mass transfer channel can lead to a peak in the mass-ratio distribution between  $q \sim 0.6$ – $0.8$  (C. J. Neijssel et al. 2019; L. A. C. van Son et al. 2022b), which is qualitatively consistent with the mass-ratio distribution of the  $\sim 10 M_{\odot}$  inferred with the ISOLATED PEAK model. Stable mass transfer also predicts a peak near  $\sim 10 M_{\odot}$  that is robust to uncertainties in the metallicity-dependent star formation history (L. A. C. van Son et al. 2022a) and other physical uncertainties of the channel (L. A. C. van Son et al. 2022c).

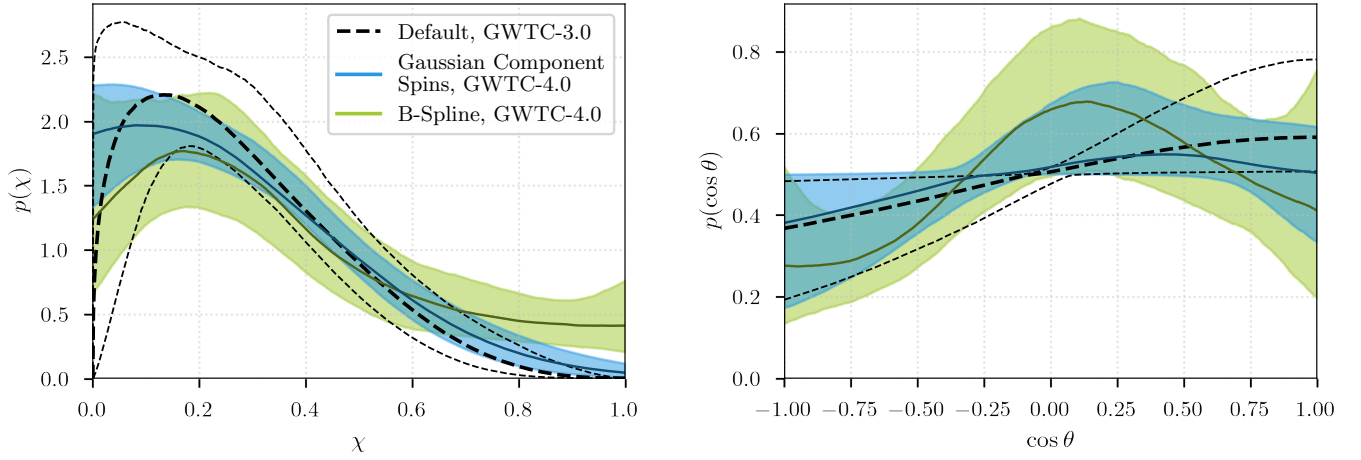
### 6.3. Spin

We next present the spin distribution of the BBH population through O4a. We model spins using two different parameterizations: the magnitudes  $\chi_i$  and tilt angles  $\theta_i$  (Section 6.3.1), and the effective inspiral spin  $\chi_{\text{eff}}$  and effective precessing spin  $\chi_p$  (Section 6.3.2). The effective inspiral spin  $\chi_{\text{eff}}$  is the mass-weighted average of the component spins *aligned* with the binary’s orbital angular momentum (E. Racine 2008; P. Ajith et al. 2011). The effective precessing spin  $\chi_p$  characterizes the degree of relativistic precession caused by spin-orbit misalignment, capturing the effect of the *in-plane* spin components (P. Schmidt et al. 2011, 2012, 2015; D. Gerosa et al. 2021); these are defined in Equations (15) and (16) of A. G. Abac et al. (2025a). More details about spin parameterization are given in Appendix B.5.

Previous analyses of the BBHs observed through O3 found that BH spin vectors tend to be small in magnitude ( $\chi \lesssim 0.3$ ) and preferentially—but not exclusively—lie above the orbital plane ( $\cos \theta > 0$ ; B. P. Abbott et al. 2019a; R. Abbott et al. 2021a, 2023a). The new observations in GWTC-4.0 further support these conclusions and additionally suggest more structure in the component and effective spin distributions, enabled by changes to the models used in previous population analyses: (i) the spin magnitude distribution has support at  $\chi \approx 0$ , (ii) the spin tilt distribution may peak away from perfect alignment with the orbital angular momentum, and (iii) the  $\chi_{\text{eff}}$  distribution is asymmetric about its peak. We elaborate upon these new features in the following subsections.

#### 6.3.1. Spin Magnitudes and Tilts

Spin magnitudes and tilt angles provide insight about BBH formation and evolution (e.g., I. Mandel & A. Farmer 2022; M. Mapelli 2020); we begin with spin magnitudes. If angular



**Figure 7.** Marginal spin magnitude  $\chi$  (left) and cosine tilt angle  $\cos \theta$  (right) distributions under the GAUSSIAN COMPONENT SPINS (blue) and B-SPLINE (green) models. The results from the GWTC-3.0 DEFAULT are shown for comparison (black dashed); note that this model is different from what is used for GWTC-4.0. The GWTC-3.0 analysis employed a Beta distribution for spin magnitudes rather than a truncated normal and fixed the location of the Gaussian component of the spin tilt angle distribution to  $\cos \theta = 1$  rather than letting it vary freely in inference. The solid lines show the median of the inferred distributions from GWTC-4.0, and the shaded regions show their 90% credible regions. The thick dashed lines show the median from GWTC-3.0, while the thin dashed lines show its 90% credible region.

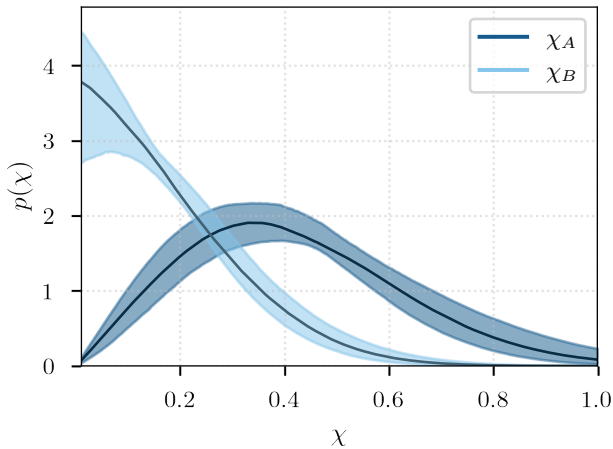
momentum transport in stars is efficient, stellar cores rotate slowly, resulting in small spin magnitudes for isolated BHs (J. Fuller & L. Ma 2019; L. Ma & J. Fuller 2019; J. Fuller et al. 2019). However, binary interactions can significantly influence BH spins through mechanisms such as tides (P. Hut 1981; W. Packet 1981; M. Zaldarriaga et al. 2018; Y. Qin et al. 2018; S. S. Bavera et al. 2020; I. Mandel & T. Fragos 2020) and accretion (P. Hut 1981; W. Packet 1981; E. P. J. van den Heuvel et al. 2017; C. J. Neijssel et al. 2019; N. Steinle & M. Kesden 2021; J. Stegmann & F. Antonini 2021). If a BBH forms from a preexisting isolated stellar binary, tidal interactions can spin up the progenitor of the second-born BH (S. S. Bavera et al. 2020; Y. Qin et al. 2019), yielding spin magnitudes of  $\chi \approx 0.2 - 0.4$  (L. Ma & J. Fuller 2023), although these can be reduced by stellar winds (C. A. Tout & J. E. Pringle 1992). Chemically homogeneous evolution—involving tidally locked, high-mass, low-metallicity, close binaries—may produce even larger spins (I. Mandel & S. E. de Mink 2016; S. E. de Mink & I. Mandel 2016). Alternatively, large spin magnitudes may point toward an HM origin, where one or both BHs are remnants of previous BBH mergers (C. L. Rodriguez et al. 2019; R. C. Zhang et al. 2023; Z. Doctor et al. 2019; C. Kimball et al. 2020; E. Payne et al. 2024; D. Gerosa & M. Fishbach 2021; M. Fishbach et al. 2017; D. Gerosa & E. Berti 2017; M. Mould et al. 2022b; P. Mahapatra et al. 2021, 2025b, 2024), which are predicted to have  $\chi \sim 0.7$  (C. O. Lousto et al. 2010).

With this astrophysical context, we present our measurement of the spin magnitude distribution through O4a. The left column of Figure 7 shows the marginal distributions of  $\chi$  using the strongly modeled approach (GAUSSIAN COMPONENT SPINS; blue) and weakly modeled approach (B-SPLINE; green). The GAUSSIAN COMPONENT SPINS model (Equation (B18)) describes the  $\chi$  population as a truncated Gaussian distribution. This is a departure from the DEFAULT spin model of GWTC-3.0. There, a nonsingular Beta distribution was used (R. Abbott et al. 2023a), which forces  $p(\chi) = 0$  at  $\chi = 0, 1$  and thus cannot measure contributions to the population at near-minimal or near-maximal spins. Allowing for more model flexibility at the  $\chi$  distribution’s boundaries is

crucial, as there exists an ongoing discussion in the literature about whether or not there is an overdensity of BBHs with  $\chi \lesssim 0.01$  (C. Kimball et al. 2020; S. Galadage et al. 2021; T. A. Callister et al. 2022; H. Tong et al. 2022; M. Mould et al. 2022a; A. Hussain et al. 2026). We find that the GAUSSIAN COMPONENT SPINS model is preferred over the DEFAULT spin model of GWTC-3.0 by  $\log_{10} \mathcal{B} = 0.66$ ; additional parametric spin magnitude (and tilt) models are discussed in Appendix D.2. The widening of the 90% credible regions for the  $\chi$  and  $\cos \theta$  distributions at their boundaries under the B-SPLINE model seen in Figure 7 is a prior-driven effect common in spline modeling (e.g., J. Golomb & C. Talbot 2023; B. Edelman et al. 2023).

In GWTC-4.0, we constrain  $p(\chi \approx 0) > 0$  under both the strongly and weakly modeled approaches. At 90% credibility, our recovered spin magnitude distribution peaks between  $\chi = 0.01 - 0.22$ , as measured by the  $\mu_\chi$  location parameter. Broadly, BH spins are inferred to be predominantly non-extremal, with the GAUSSIAN COMPONENT SPINS model finding that 90% of BHs having  $\chi < 0.6$ . The comparative dearth of observed BBHs with large spins disfavors a population dominated by second-generation BHs. However, the precise fraction of systems with large spin magnitudes is model dependent: the GAUSSIAN COMPONENT SPINS and B-SPLINE models only disagree at 90% credibility for  $\chi > 0.83$ . At  $\chi = 0.8, 0.9$ , and  $1.0$ , their  $p(\chi)$  distributions differ at the 85%, 96%, and 98% levels, respectively. While the GAUSSIAN COMPONENT SPINS model approaches  $p(\chi) \sim 0$  at  $\chi = 1$ , the B-SPLINE model infers a larger, nearly flat distribution from  $\chi = 0.6$  to  $1$ . Similar behavior was found in GWTC-3.0 (J. Godfrey et al. 2023), and attributed to a subpopulation with near-uniform spin magnitudes. The discrepancy between our two models may arise from limited flexibility in the strongly modeled approach; a single truncated Gaussian cannot increase the probability at  $\chi \gtrsim 0.8$  without also increasing it at  $\chi \sim 0.2 - 0.5$ . In GWTC-4.0, a handful of events do have preferentially large spin magnitudes, including GW231123, which has primary spin  $\chi_1 > 0.5$  with high confidence (A. G. Abac et al. 2025b).

Under both the GAUSSIAN COMPONENT SPINS and B-SPLINE models, the results presented in Figure 7 assume



**Figure 8.** Larger ( $\chi_A$ , darker blue) and smaller ( $\chi_B$ , lighter blue) spin magnitude distributions, derived from imposing order statistics on the GAUSSIAN COMPONENT SPINS $\chi$  distribution shown in Figure 7. The solid lines show the median of each inferred distribution, and the shaded regions show the 90% credible intervals.

that the spin magnitudes are independently and identically distributed (IID), meaning that the function describing the population distribution is factorizable in terms of  $\chi_1$  and  $\chi_2$ , and the two are described by the same set of hyperparameters. The data prefer identically distributed spin magnitudes over those which are nonidentically distributed, see Table 12. However, mathematically, the primary and secondary spins cannot be IID if the purported correlation between  $q$  and  $\chi_{\text{eff}}$  is true (B. Farr & W. Farr 2025). We probe this correlation in Section 6.5.2, and find support for its existence, albeit with evidence that has diminished since GWTC-3.0. Thus, we interpret the Bayes factor in favor of IID spins as a statement that, under the GAUSSIAN COMPONENT SPINS model, we cannot yet say with statistical certainty that the spins are not identically distributed. This statement is likely driven by the fact that individual-event spin magnitude posterior distributions are typically wide, making  $\chi_1$  and  $\chi_2$  hard to distinguish. In general,  $\chi_1$  and  $\chi_2$  are not expected to be identically distributed in nature; if  $q$  and  $\chi_{\text{eff}}$  are indeed correlated, more informative  $\chi_i$  measurements may eventually reveal their nonidentical nature. Figure 17 in Appendix D.2 presents posteriors on the GAUSSIAN COMPONENT SPINS hyperparameters under the assumption that spin magnitudes (and tilts) are identically versus nonidentically distributed.

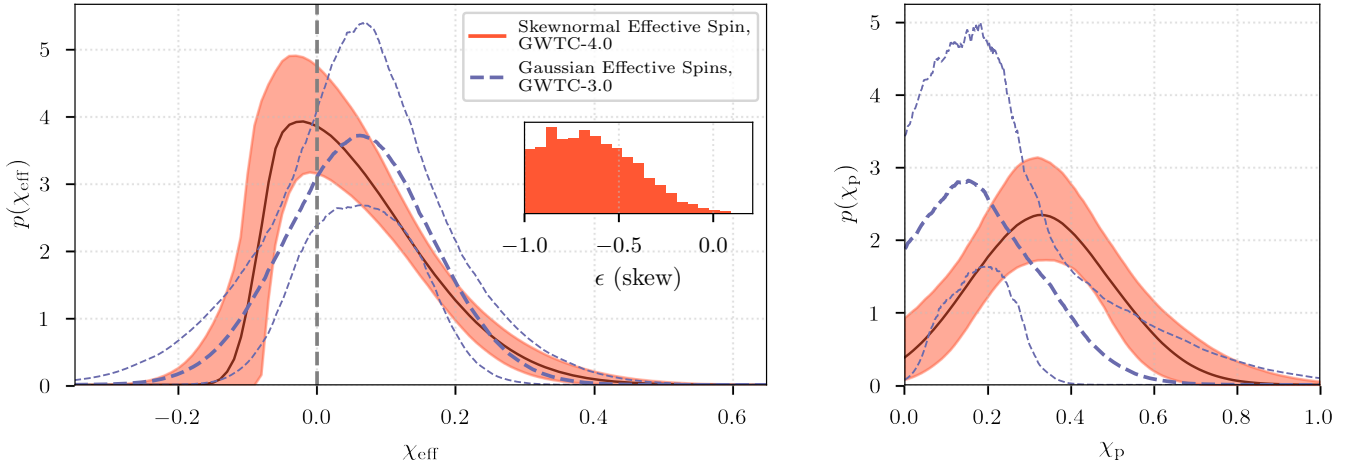
Next, Figure 8 shows the inferred spin magnitude distributions if, rather than sorting by the more versus less massive BH, we instead sort by the BH with the larger (subscript A) and smaller (subscript B) spin magnitudes (S. Biscoveanu et al. 2021). The magnitudes  $\chi_A$  and  $\chi_B$  are derived quantities and are not fit independently: to generate their distributions, we take results from the GAUSSIAN COMPONENT SPINS model and impose order statistics, assuming that  $\chi_A$  is the larger of two draws from the  $p(\chi)$  distribution in the left panel of Figure 7 and  $\chi_B$  is the smaller (R. Abbott et al. 2023a; S. Biscoveanu et al. 2021). This analysis does not assume any sort of pairing function between spins. Spin sorting offers an alternative way to visualize and interpret the spin information from the IID model. The more rapidly spinning component has a wide spin magnitude distribution, with a population predictive distribution (PPD) peaking at  $\chi_A = 0.35$ , and support up to  $\chi_{A,99\%} = 0.92^{+0.04}_{-0.07}$  (value of  $\chi_A$  at which each  $p(\chi_A)$  trace reaches its 99th percentile, serving as a proxy for

the distribution’s maximum). The vanishing probability at  $\chi_A = 0$  is a Jacobian effect of the order statistics. However, if both BHs had  $\chi \approx 0$ , the  $\chi_A$  distribution would be much more strongly peaked at small values (L. Szemraj & S. Biscoveanu 2026), meaning that spin-sorting results on GWTC-4.0 indicate that at least one BH per binary has  $\chi \gtrsim 0$ . The more slowly spinning component, on the other hand, is consistent with a narrower distribution peaking at  $\chi_B = 0$  and only has support up to  $\chi_{B,99\%} = 0.59^{+0.08}_{-0.06}$ . The observation that spin  $\chi_B$  magnitudes are preferentially small could indicate small natal spins for at least one of the two BHs, while the fact that the population is consistent with only one BH per binary having large spin supports the existence of some variety of spin-up mechanism in BBH evolution.

We next turn to the spin tilt distribution. Many authors argue that if BBHs are formed primarily in the isolated binary scenario, large tilt angles are hard to explain without invoking large supernovae kicks and inefficient tides (V. Kalogera 2000; D. Gerosa et al. 2018; N. Steinle & M. Kesden 2021; D. Wysocki et al. 2018; S. Stevenson 2022; T. A. Callister et al. 2021a), although others claim that, depending on the specifics of poorly understood supernovae physics, even small kicks can misalign a binary (V. Baibhav & V. Kalogera 2024; T. M. Tauris 2022). Complete antialignment ( $\cos \theta = -1$ ) is a possible result of mass transfer in the isolated channel (J. Stegmann & F. Antonini 2021). On the other hand, BBHs formed dynamically in stellar clusters are predicted to have isotropically distributed spin orientations, as there is no a priori preferential spin direction in these environments (C. L. Rodriguez et al. 2015, 2016a, 2018; W. M. Farr et al. 2017). However, recent studies indicate that mechanisms could possibly exist for dynamically formed BBHs to have a slight preference for  $\cos \theta > 0$  (A. A. Trani et al. 2021; S. Banerjee et al. 2023; F. Kiroglu et al. 2025), especially for BBHs formed dynamically in the disks of active galactic nuclei (Y.-H. Wang et al. 2021; B. McKernan et al. 2022).

The right-hand column of Figure 7 shows the marginal distribution of the cosine of the tilt angle,  $\cos \theta$ . The  $\cos \theta$  population under the GAUSSIAN COMPONENT SPINS model is a mixture between isotropic and truncated Gaussian subpopulations (Equation (B19)). Following GWTC-3.0 and earlier population analyses, we assume that spin tilt angles are nonindependently but identically distributed (NID) under the GAUSSIAN COMPONENT SPINS model, meaning that while  $\cos \theta_1$  and  $\cos \theta_2$  are described by the same hyperparameters, the population distribution is *not* separable in terms of the two: we require that both BHs in a binary are drawn from the same subpopulation (either the isotropic or the truncated Gaussian). NID tilts are favored by the data over nonidentical distribution, see Table 12. The B-SPLINE model naturally assumes spin tilt angles are IID, as it does not probe separate tilt subpopulations.

The Default model of GWTC-3.0 fixed the location of the Gaussian subpopulation at exact spin-orbit alignment (S. Vitale et al. 2017; C. Talbot & E. Thrane 2017; R. Abbott et al. 2023a), making it a half-Gaussian peaking at  $\cos \theta = 1$ . In GWTC-4.0, the strongly and weakly modeled approaches both find that the spin tilt distribution may peak away from exact spin-orbit alignment. The GAUSSIAN COMPONENT SPINS model finds that the  $\cos \theta$  distribution reaches its maximum between  $-0.51$  and  $0.93$  at 90% credibility; consistently, the B-SPLINE model finds the peak to lie between  $-0.15$  and  $1.0$ . The possibility that the



**Figure 9.** Marginal  $\chi_{\text{eff}}$  (left panel) and  $\chi_p$  (right panel) distributions. The solid lines show the median of each inferred distribution, and the shaded regions show the 90% credible intervals. The GWTC-4.0 results under the SKEW-NORMAL EFFECTIVE SPIN model are shown in red; the GWTC-3.0 results under the GAUSSIAN EFFECTIVE SPINS model are shown in purple (dashed). The histogram inset in the left panel shows the skew parameter  $\epsilon$  for the SKEW-NORMAL EFFECTIVE SPIN model. There is significant preference for a skewed  $\chi_{\text{eff}}$  distribution, indicated by  $\epsilon < 0$  with 99.5% credibility.

tilt angle distribution peaks away from alignment is also found in GWTC-3.0 under various models, which permit such a feature (S. Vitale et al. 2022; B. Edelman et al. 2023; J. Golomb & C. Talbot 2023). It is not impossible, however, for the peak of a  $\cos \theta$  distribution to be inferred away from alignment even when the true underlying population does peak at  $\cos \theta = 1$  (S. Vitale & M. Mould 2025). The inferred peak of the GWTC-4.0  $\cos \theta$  distribution is more strongly constrained away from unity than nearly all of those spuriously found with simulated catalogs of the same size (see Figure 17 with Figure 4 of S. Vitale & M. Mould 2025).

Under both the strongly and weakly modeled approaches, the  $\cos \theta$  distribution shown in Figure 7 has support across a wide range of spin tilts, with a slightly larger fraction of positive  $\cos \theta$  compared to negative. Given this broad support, we next ask the question: what is the lowest spin tilt angle that is absolutely required to fit GWTC-4.0 reasonably? To probe this, we use a model that is similar to the GAUSSIAN COMPONENT SPINS model but with  $p(\cos \theta < t_{\min}) = 0$  for an inferred value  $t_{\min}$ , where  $t \equiv \cos \theta$  (H. Tong et al. 2022; T. A. Callister et al. 2022); see Equation (B20). We find  $t_{\min} = -0.69^{+0.14}_{-0.19}$  at 90% credibility. That the posterior for the minimum required  $\cos \theta$  is inconsistent with  $-1$  but remains confidently negative is a somewhat unexpected astrophysical result. If most BBHs form in isolation, a minimum tilt cutoff is plausible but would be expected to be closer to zero, potentially even positive. Conversely, dynamically formed BBHs should exhibit isotropic tilts extending down to  $\cos \theta = -1$ . Our observed tilt distribution therefore does not preclude either broad scenario of isolated or dynamical formation—or a mixture of both. However, the fact that the inferred minimum required tilt is significantly negative suggests the contribution of a dynamical formation channel to the BBH population. We further discuss the astrophysical interpretation of negative spin tilts and potential subpopulations in Section 6.3.2 in the context of effective spins.

### 6.3.2. Effective Spins

We next turn to the inferred distributions of the effective spins  $\chi_{\text{eff}}$  and  $\chi_p$ . Figure 9 shows the marginal distributions of  $\chi_{\text{eff}}$  (left) and  $\chi_p$  (right) under the SKEW-NORMAL EFFECTIVE

SPIN model (red solid; Equation B29), compared to the GAUSSIAN EFFECTIVE SPINS model result from GWTC-3.0 (purple dashed; Equation B28). The SKEW-NORMAL EFFECTIVE SPIN model (S. Banagiri et al. 2025) differs from the previously used GAUSSIAN EFFECTIVE SPINS in two ways. First, it allows for asymmetry in the  $\chi_{\text{eff}}$  marginal distribution. Second, the marginal  $\chi_p$  distribution is a truncated Gaussian that is not correlated with  $\chi_{\text{eff}}$ . On GWTC-4.0 data, the GAUSSIAN EFFECTIVE SPINS model finds that  $\chi_{\text{eff}}$  and  $\chi_p$  are preferentially uncorrelated, although this conclusion depends on analysis settings; see Figure 19 in Appendix D.3 and the discussion therein.

We find that the  $\chi_{\text{eff}}$  distribution is skewed and asymmetric about zero with more support for positive values. Asymmetry can be directly probed with the  $\epsilon$  skewness parameter of the SKEW-NORMAL EFFECTIVE SPIN model, defined in Equation (B29). We find that the skewness  $\epsilon$  is less than 0 (symmetry) with 99.5% credibility, as can be seen in the inset of the left panel of Figure 9. This corresponds to a wider  $\chi_{\text{eff}}$  distribution to the right of the peak, and a narrower distribution to the left, and is known as *positive skew*. As discussed in Section 6.5.2, asymmetry is also found when allowing for a linear or spline correlation between  $\chi_{\text{eff}}$  and mass ratio. Results for the GWTC-4.0  $\chi_{\text{eff}}$  distribution measured with more models, including the GAUSSIAN EFFECTIVE SPINS model and with the weakly modeled approach are presented in Figures 19 and 21 in Appendix D.

We now discuss BBHs with spin tilts lying below the orbital plane. These interesting probes of dynamical BBH formation have  $\cos \theta < 0$  and thus negative  $\chi_{\text{eff}}$ . In Table 3, we present 90% bounds for three quantities that probe negative  $\chi_{\text{eff}}$  in the population, using both the SKEW-NORMAL EFFECTIVE SPIN and GAUSSIAN EFFECTIVE SPINS models for a straightforward comparison to GWTC-3.0. First, we report the first percentile of  $\chi_{\text{eff}}$  distribution, which serves as a proxy for the distribution’s minimum without necessitating the inclusion of sharp features in the distribution itself (T. A. Callister et al. 2022), constraining it to fall between  $-0.27$  and  $-0.07$ . The GAUSSIAN EFFECTIVE SPINS model finds more extremal minimum spins than the SKEW-NORMAL EFFECTIVE SPIN model, likely due to its required symmetry about its peak; fitting the positive side of the distribution forces a longer

**Table 3**  
Summary of Probes of Spin Misalignment, as Measured by  $\chi_{\text{eff}}$

| Model                                 | $\chi_{\text{eff},1\%}$ | Fraction $\chi_{\text{eff}} < 0$ | HM Fraction            |
|---------------------------------------|-------------------------|----------------------------------|------------------------|
| GAUSSIAN EFFECTIVE SPINS (GWTC-3.0)   | $-0.18^{+0.09}_{-0.12}$ | $0.28^{+0.12}_{-0.13}$           | $< 0.0031$             |
| GAUSSIAN EFFECTIVE SPINS (GWTC-4.0)   | $-0.19^{+0.06}_{-0.07}$ | $0.33^{+0.08}_{-0.1}$            | $< 0.0022$             |
| SKEW-NORMAL EFFECTIVE SPIN (GWTC-4.0) | $-0.11^{+0.04}_{-0.08}$ | $0.32^{+0.09}_{-0.09}$           | $< 1.3 \times 10^{-4}$ |

**Note.** Summary of probes of spin misalignment, as measured by  $\chi_{\text{eff}}$ . We give 90% credible intervals for the  $\chi_{\text{eff}}$  value of the first percentile of the distribution ( $\chi_{\text{eff},1\%}$ ), serving as a proxy for the minimum  $\chi_{\text{eff}}$  and the fraction of  $\chi_{\text{eff}} < 0$ . The HM fraction provides an upper limit to the fraction of BBHs of HM origin, equal to 1/0.16 times fraction of systems with  $\chi_{\text{eff}} < -0.3$  (M. Fishbach et al. 2022; V. Baibhav et al. 2020); we provide its 90% upper limit. Posteriors for these quantities for these and other models are plotted in Figure 21.

tail into the negative region. Second, we report the fraction of the population with negative  $\chi_{\text{eff}}$  to be 0.23–0.41, with the two models finding nearly identical results. Assuming isotropy, an upper bound on the fraction of BBHs formed dynamically in gas-free environments can be placed by doubling the fraction of negative  $\chi_{\text{eff}}$  (Equation (7) of R. Abbott et al. 2021a); we thus find that at most 84% of BBHs form dynamically. Third, we give the 90% upper limit on the fraction of BBHs coming from the HM scenario. The HM fraction is bounded by the consideration that  $\sim 16\%$  of BBHs coming from the HM formation channel will have  $\chi_{\text{eff}} < -0.3$  (V. Baibhav et al. 2020; M. Fishbach et al. 2022). With the SKEW-NORMAL EFFECTIVE SPIN and GAUSSIAN EFFECTIVE SPINS models, we limit this fraction to  $\lesssim 3\%$ . Figure 21 in Appendix D.4 shows posterior distributions on the quantities in Table 3 for the models presented here and those using the weakly modeled approach; with more flexible models, we more generously limit the HM fraction to  $\lesssim 74\%$ .

It is possible that the support for  $\chi_{\text{eff}} < 0$  may be a byproduct of the models fitting for a peak at  $\chi_{\text{eff}} \sim 0$  without having the flexibility for a sharp decline beyond  $\chi_{\text{eff}} < 0$ . This type of sharp feature could occur if component spin magnitudes cluster around  $\chi \sim 0$  but their tilts seldom reach below  $\cos \theta = 0$ . In Section 6.3.1, we address this by directly fitting for the minimum required  $\cos \theta$ , which is found to be confidently negative and corresponds to a fraction  $0.41^{+0.06}_{-0.05}$  of systems with spins laying below the orbital plane. These probes of negative spin indicate that between  $\sim 20$ – $40\%$  the BBH population has spins that are more than  $90^\circ$  misaligned with the orbital angular momentum.

It is unlikely that the entire observed BBH population originates from a single formation channel (M. Zevin et al. 2021; I. Mandel & F. S. Broekgaarden 2022; A. Q. Cheng et al. 2023; S. Afroz & S. Mukherjee 2025; S. Colloms et al. 2025). Features in our spin distributions indeed suggest the presence of multiple subpopulations. A purely random spin channel would produce a symmetric distribution around  $\chi_{\text{eff}} = 0$  (C. L. Rodriguez et al. 2016a, 2016b; W. M. Farr et al. 2017). However, for all models, the observed  $\chi_{\text{eff}}$  distribution is asymmetric about zero, c.f., Figure 21. This asymmetry suggests contribution from a preferentially aligned subpopulation (D. Gerosa et al. 2018; M. Arca Sedda et al. 2023; S. Banagiri et al. 2025). The skew observed in the SKEW-NORMAL EFFECTIVE SPIN, as well as the  $(q, \chi_{\text{eff}})$ LINEAR and  $(q, \chi_{\text{eff}})$ SPLINE models (see Section 6.5.2 and Figure 21) further supports the presence of an aligned component, either as a subdominant subpopulation or a dominant subpopulation with small spin magnitudes. We find a preference for small spin magnitude (Figure 7), perhaps favoring the latter.

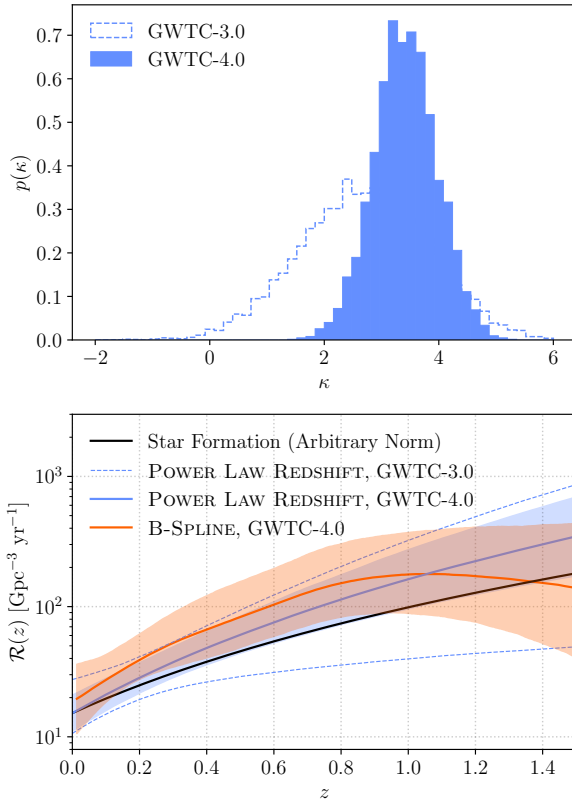
Finally, we discuss the effective precessing spin  $\chi_p$ , which can provide additional insight about spin precession in the population. The right panel of Figure 9 shows the marginal inferred  $\chi_p$  distribution (red). We find that precession exists on a population level, as our models do not support  $(\mu_p, \sigma_p) = (0, 0)$  at high credibility. The GWTC-4.0 results support larger  $\chi_p$  than GWTC-3.0, shown for comparison in Figure 9 (purple dashed). However, different likelihood convergence criteria (Appendix A.1) were used between GWTC-4.0 and GWTC-3.0, meaning these results are not directly comparable. Under the less-stringent GWTC-3.0 convergence criterion, the  $\chi_p$  distribution inferred from GWTC-4.0 data is more consistent with that found in GWTC-3.0, albeit still with less support for low  $\mu_p$  and low  $\sigma_p$ . The inferred  $\chi_p$  distribution is more dependent on analysis settings, specifically the threshold on the variance of the log-likelihood, than other parameters. This is largely because the individual-event prior has no support at  $\chi_p = 0$  making it technically difficult to reweight individual-event posteriors to the population. We discuss the sensitivity of the  $\chi_p$  distribution to analysis settings in detail in Appendix D.3; see Figures 18 and 19.

#### 6.4. Merger Rate and Redshift Evolution

Improvements in the sensitivity of current GW observatories (D. Ganapathy et al. 2023; E. Capote et al. 2025; A. G. Abac et al. 2025a) not only provide more BBH detections, but also observations of increasingly faint sources at higher redshifts. These observations allow us to improve our population-level constraints on the evolution of the merger rate across redshift.

Following R. Abbott et al. (2023a), we repeat the POWER LAW REDSHIFT strongly modeled approach. We assume that the merger rate evolves as  $\mathcal{R}(z) \propto (1+z)^\kappa$ , and we infer the proportionality constant and the power-law index  $\kappa$ . We find that the BBH merger rate at  $z = 0.2$  is  $28^{+8.7}_{-6.7} \text{ Gpc}^{-3} \text{ yr}^{-1}$ , and the power-law exponent is constrained to  $\kappa = 3.4^{+0.92}_{-0.91}$ , which represent consistent and improved constraints over our GWTC-3.0 analysis. We also probe deeper redshifts and infer that 99% of detectable BBHs fall below  $z = 1.54^{+0.08}_{-0.09}$  (see the maximum observable redshift inferred as  $z = 1.1^{+0.2}_{-0.2}$  in M. Fishbach & L. van Son 2023, from GWTC-3.0). We also use the weakly modeled B-SPLINE approach to explore if the data support behavior beyond a power-law evolution, and compare our results in Figure 10. While the results are consistent—indicating that the POWER LAW REDSHIFT model is sufficient—the B-SPLINE approach infers a larger merger rate of  $39^{+23}_{-11} \text{ Gpc}^{-3} \text{ yr}^{-1}$  at  $z = 0.2$ . Our results are nominally consistent with the cosmic star formation rate density, with  $\kappa_{\text{SFR}} = 2.7$  (P. Madau & M. Dickinson 2014).

Our constraints on the merger rate evolution informs our understanding of the BBH progenitor formation rate and the



**Figure 10.** Comparison of redshift models between GWTC-3.0 and GWTC-4.0. Top: posterior on the  $\kappa$  parameter for the POWER LAW REDSHIFT model. GWTC-4.0 shows increased support for positive values. Bottom: median and 90% credible regions for the comoving source frame rate in the POWER LAW REDSHIFT model. We also show a comparison of the POWER LAW REDSHIFT model and the weakly modeled B-SPLINE model and a scaled cosmic star formation rate density (P. Madau & M. Dickinson 2014), which are consistent within uncertainties ( $\kappa_{\text{SFR}} = 2.7$ ).

delay time distribution between formation and merger (S. Vitale et al. 2019; C. L. Rodriguez & A. Loeb 2018; G. Fragione & B. Kocsis 2018; M. Fishbach et al. 2018; V. Baibhav et al. 2019; I. M. Romero-Shaw et al. 2021; F. S. Broekgaarden et al. 2022b; M. Mapelli et al. 2022; M. Fishbach & V. Kalogera 2021; M. Chruslińska 2024; M. Fishbach & G. Fragione 2023; A. P. Boesky et al. 2024). For BBHs formed from isolated binary evolution, the merger rate evolution is typically well approximated as a power law at small redshift, though the value of the power-law index  $\kappa$  is sensitive to the assumed population synthesis parameters (C. J. Neijssel et al. 2019; F. S. Broekgaarden et al. 2022b; M. Gallegos-Garcia et al. 2021; L. M. de Sá et al. 2024). Nevertheless, models typically prefer values around  $\kappa \sim 1$  (M. Dominik et al. 2013; V. Baibhav et al. 2019). BBHs originating from dense star clusters predict local merger rates of  $\mathcal{R} \sim 10 \text{ Gpc}^{-3} \text{ yr}^{-1}$  (M. Arca Sedda et al. 2024) and steeper values of  $\kappa \sim 2$  (F. Antonini & M. Gieles 2020), albeit with large theoretical uncertainties that can account for a similar evolution to the isolated binary evolution predictions. Our observations suggest a steeper evolution, with  $\kappa \sim 2\text{--}4$ . While this does not rule out either class of BBH formation, it may be suggestive of (i) progenitor formation rates that peak at an earlier redshift as compared to the cosmic star formation rate density, e.g., due to a preference for low-metallicity progenitors, and/or (ii) shorter delay times, perhaps with a tail toward long delay times (M. Fishbach & V. Kalogera 2021;

C. Karathanasis et al. 2023; M. Fishbach & L. van Son 2023; K. Turbang et al. 2024; A. Vijaykumar et al. 2024; A. Schiebelbein-Zwack & M. Fishbach 2024).

Models of isolated binary evolution and dense star clusters often predict that the merger rate evolves differently across the mass spectrum (L. A. C. van Son et al. 2022b; M. Mapelli et al. 2022; C. S. Ye & M. Fishbach 2024); however, analyses of the previous catalog have not found evidence for or against differential rate evolution (M. Fishbach et al. 2021; J. Sadiq et al. 2022; L. A. C. van Son et al. 2022b; A. Ray et al. 2023a; J. Heinzel et al. 2025b; J. Sadiq et al. 2025a). We discuss potential mass-redshift correlations in Section 6.5.4.

### 6.5. Population-level Correlations between Parameters

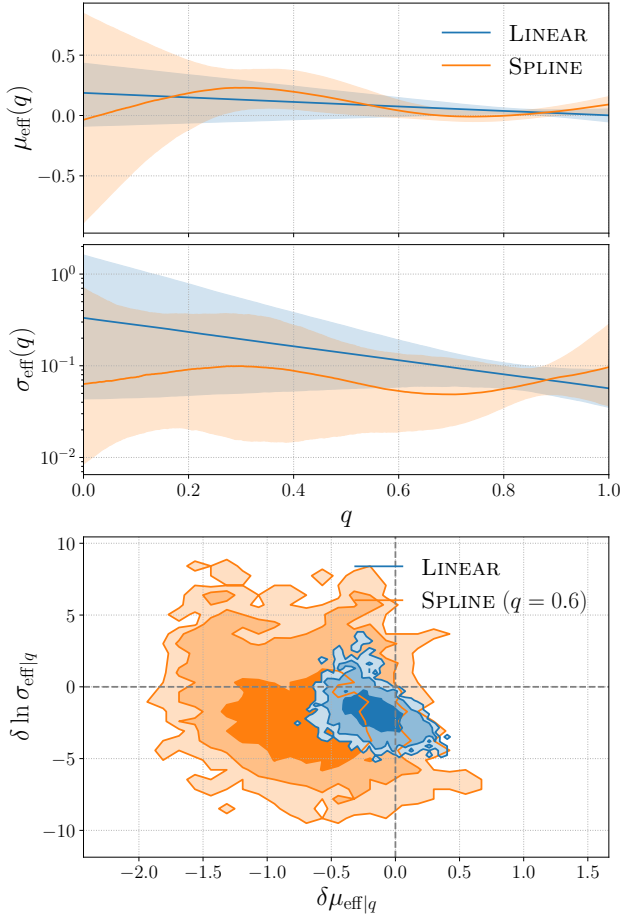
While much can be learned by studying the distributions of individual BBH parameters, we can glean additional information on the population by considering how parameters are correlated with one another across systems. In this subsection, we provide an overview of how parameters in the BBH population appear to be broadly structured in various two-dimensional slices of parameter space, briefly discussing the astrophysical implications of our findings.

#### 6.5.1. Mass Ratio and Spin Correlations

We begin by following up on the purported anticorrelation between BBH mass ratio  $q$  and effective inspiral spin  $\chi_{\text{eff}}$ . Although we find less support for the specific case of anticorrelation between  $q$  and  $\chi_{\text{eff}}$  relative to GWTC-3.0, we find compelling evidence for some correlated structure in  $(q, \chi_{\text{eff}})$ . Namely, larger positive values of  $\chi_{\text{eff}}$  appear to be favored as  $q$  decreases, but it is unclear if this is accompanied by a preference for larger negative values of  $\chi_{\text{eff}}$  as well. The  $(q, \chi_{\text{eff}})$  LINEAR model imposes a linear functional dependence between the BBH mass ratio and the mean and (natural log) width of the  $\chi_{\text{eff}}$  distribution (see Appendix B.7). Fitting this model to GWTC-3.0 data suggests that a linear correlation coefficient of  $\delta\mu_{\text{eff}|q} < 0$  (i.e., the case of a negative  $q$ -dependence on the mean of the  $\chi_{\text{eff}}$  distribution) with 98% credibility (R. Abbott et al. 2023a). Updating this analysis to include data obtained over O4a softens the evidence for an anticorrelation between  $q$  and the mean of the  $\chi_{\text{eff}}$  distribution, with a value of  $\delta\mu_{\text{eff}|q} < 0$  now inferred at 99.4% credibility. However, we now see notable evidence for a linear increase in the log width of the  $\chi_{\text{eff}}$  distribution as mass ratios become more unequal—with  $\delta \ln \sigma_{\text{eff}|q} < 0$  at 91.1% credibility.

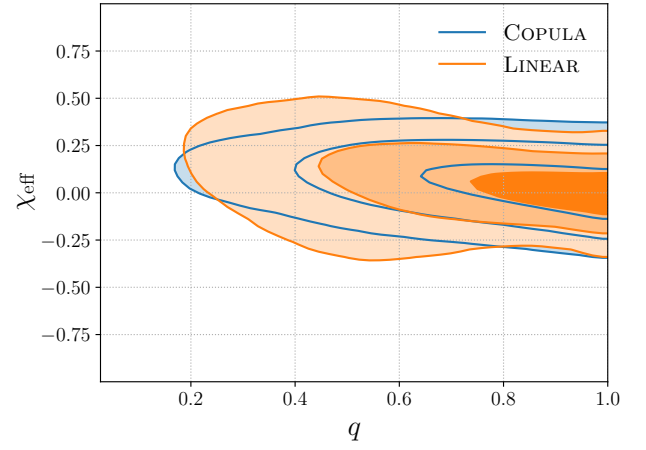
We plot the mass-ratio dependent mean and width of the  $\chi_{\text{eff}}$  distribution inferred using the LINEAR model in Figure 11. In the bottom panel of Figure 11, we include the two-dimensional posterior distribution of  $\delta\mu_{\text{eff}|q}$  and  $\delta \ln \sigma_{\text{eff}|q}$ . Inspecting this plot, we see an anticorrelation in the posterior of the two hyperparameters, where larger negative values of  $\delta\mu_{\text{eff}|q}$  imply values of  $\delta \ln \sigma_{\text{eff}|q}$  closer to zero, and larger negative values of  $\delta \ln \sigma_{\text{eff}|q}$  imply values of  $\delta\mu_{\text{eff}|q}$  closer to zero. The case in which both parameters are zero (no correlation between  $q$  and  $\chi_{\text{eff}}$  of any kind) appears to be ruled out at  $\approx 99\%$  credibility. In practice, this implies that the LINEAR model finds support for larger positive values of  $\chi_{\text{eff}}$  at more unequal mass ratios, but cannot yet conclude whether these are accompanied by larger negative values of  $\chi_{\text{eff}}$  as well.

Next, we probe for more intricate correlations between  $q$  and  $\chi_{\text{eff}}$  using the SPLINE model. Similar to the



**Figure 11.** The inferred peak (top) and width (middle) of the  $\chi_{\text{eff}}$  distribution as a function of mass ratio for the  $(q, \chi_{\text{eff}})$  LINEAR model (blue) and SPLINE model (orange). The shaded regions in these panels give the 90% credible intervals. The bottom panel gives the posterior distribution for the gradient of the  $\chi_{\text{eff}}$  distribution’s peak ( $\delta\mu_{\text{eff}|q}$ ) and natural log width ( $\delta\ln\sigma_{\text{eff}|q}$ ) dependent on mass ratio. From dark to light, the shaded regions represent the 50%, 90%, and 99% credible intervals. Again, blue gives the result of the LINEAR model, while orange shows the result of the SPLINE model sliced through  $q = 0.6$  (the approximate point at which the gradients are largest). It appears that mass ratio and  $\chi_{\text{eff}}$  exhibit some kind of correlation, but the exact nature is unclear.

LINEAR model, the SPLINE model allows for the mean and width of the  $\chi_{\text{eff}}$  distribution to evolve with mass ratio. However, these mass ratio dependencies, rather than being linear, are modeled flexibly with cubic splines (see Appendix B.7 and J. Heinzl et al. 2024). We plot the  $q$ -dependent means and widths inferred from the SPLINE model alongside those from the LINEAR model in Figure 11. Despite fluctuations emerging in the SPLINE model, the two models are, within 90% credible bounds, consistent. The preference for broadening in the  $\chi_{\text{eff}}$  distribution as  $q$  decreases found with the LINEAR model, does not clearly appear in the SPLINE model. In the bottom panel of Figure 11, we also plot the inferred gradient of the  $\chi_{\text{eff}}$  distribution’s mean and (natural log) width relative to mass ratio at  $q = 0.6$  (roughly the value at which covariance appears most pronounced). Here, we see a similar structure to that of the LINEAR model’s ( $\delta\mu_{\text{eff}|q}, \delta\ln\sigma_{\text{eff}|q}$ ) posterior, albeit with much more uncertainty. As a final observation from the SPLINE model in Figure 11, we see that the inferred  $\chi_{\text{eff}}$  distribution at low mass ratios ( $q \lesssim 0.2$ ) grows in uncertainty, roughly recovering the



**Figure 12.** Mass ratio and  $\chi_{\text{eff}}$  PPDs for the COPULA model (blue) and LINEAR model (orange). The contours, from dark to light, mark 50%, 90%, and 99% of the volume. We see a subtle preference for an anticorrelation, although this feature is far less prevalent than it appeared in GWTC-3.0. We also see evidence for a broadening in the distribution as mass ratios become more unequal in the LINEAR model. The COPULA model is not flexible in a way that it can capture a broadening.

prior. This implies that any correlation inferred by the LINEAR model is likely driven by observations with mass ratios  $q \gtrsim 0.2$ . As such, the inferences from this model should be interpreted with caution as  $q \rightarrow 0$ , where the trend is effectively being extrapolated from the more populated  $q \gtrsim 0.2$  region due to a lack of model flexibility.

We now move to the COPULA model, which allows for a correlation between  $q$  and  $\chi_{\text{eff}}$  with a variable strength  $\kappa_{q,\text{eff}}$  (see Appendix B.6). This framework has the added advantage that the level of correlation is decoupled from the shape of the marginal distribution (e.g., C. Adamcewicz & E. Thrane 2022), with less flexibility for covariant structure relative to other correlated population models. Fitting the COPULA model to GWTC-4.0 suggests that  $q$  and  $\chi_{\text{eff}}$  are anticorrelated ( $\kappa_{q,\text{eff}} < 0$ ) with 93.2% credibility. Specifically, we infer  $\kappa_{q,\text{eff}} = -2.04^{+2.25}_{-2.55}$ . C. Adamcewicz et al. (2023) analyzed GWTC-3.0 data with a copula model to find that  $(q, \chi_{\text{eff}})$  are anticorrelated with >99% credibility, suggesting greater evidence for an anticorrelation than is measured here. However, these results are not directly comparable to those presented in this work, due to different modeling assumptions and different convergence criteria in the population likelihood. Qualitatively, we see that the COPULA model and LINEAR model exhibit a subtle anticorrelation in  $(q, \chi_{\text{eff}})$ , as seen in the respective two-dimensional PPDs in Figure 12.

There are a number of potential astrophysical implications if the anticorrelation in  $(q, \chi_{\text{eff}})$  is real. If isolated binaries make up a substantial fraction of the population and undergo tidal spin up, stable mass transfer and the resulting mass ratio reversal of systems (F. S. Broekgaarden et al. 2022a; M. Zevin & S. S. Bavera 2022; A. Olejak et al. 2024) may produce such an anticorrelation in the population. This feature could also be explained by binaries undergoing a common-envelope phase provided common envelope efficiencies are sufficiently high (S. S. Bavera et al. 2021).

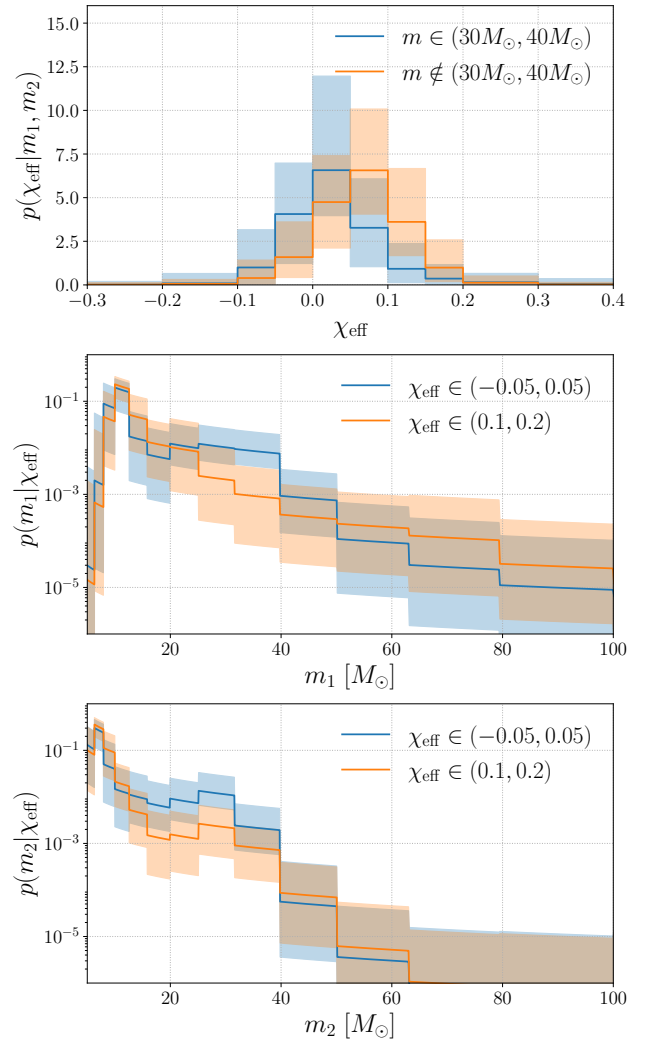
Covariance in  $(q, \chi_{\text{eff}})$  could also be a result of HMs contributing to a considerable fraction of the BBH merger rate (F. Antonini et al. 2025a, 2025b). HMs should exhibit mass ratios that are more unequal and spin magnitudes that are larger than isolated, or first-generation dynamical mergers. If

HMs occur in typical dynamical environments, the spins of the BHs will be isotropically distributed, thus producing a broadening in the  $\chi_{\text{eff}}$  distribution as mass ratios become unequal. Meanwhile, BHs in AGN may have spins preferentially aligned with one another, meaning HMs in these environments can produce a correlation between mass ratios and spins that is asymmetrical about  $\chi_{\text{eff}} = 0$  (B. McKernan et al. 2022; A. Santini et al. 2023). Stronger evidence for unequal mass binaries preferring positive values of  $\chi_{\text{eff}}$  could then indicate that binaries merging in AGN are predominantly coaligned with the rotation of the AGN disk (A. Santini et al. 2023).

### 6.5.2. Mass and Spin Correlations

We find model-dependent evidence for correlations between  $m_1$  and  $\chi_{\text{eff}}$ . Motivated by the feature in the mass distribution around the  $\sim 30 - 40 M_\odot$  range, we use a BGP analysis allowing for correlations in  $m_1$  and  $\chi_{\text{eff}}$  (see Appendix C.2) to see if this feature in the distribution of masses is accompanied by a deviation in the BBH spin distribution. Using GWTC-4.0, these studies find weak evidence that BBH systems with at least one mass in the  $\sim 30 - 40 M_\odot$  peak tend to have spins that are symmetrically distributed about  $\chi_{\text{eff}} = 0$ , while binaries outside of this mass range have spins that are skewed toward positive (aligned) values of  $\chi_{\text{eff}}$ . Quantitatively, this BGP analysis infers that for every merger in the  $\sim 30 - 40 M_\odot$  peak with a negative value of  $\chi_{\text{eff}}$ , there are  $1.9^{+4.8}_{-1.2}$  with a positive value of  $\chi_{\text{eff}}$ . Meanwhile, for every event outside of this mass range with a negative value of  $\chi_{\text{eff}}$ , there are  $1.9^{+4.8}_{-1.2}$  with a positive value of  $\chi_{\text{eff}}$ . We illustrate this result in the top panel of Figure 13. Furthermore, in the BGP analysis the inferred distribution of masses for BBH systems with effective inspiral spins ( $|\chi_{\text{eff}}| \lesssim 0.1$ ) exhibits a preference for a larger proportion of mergers with  $m_1 \sim 30 - 40 M_\odot$ , compared to systems with  $\chi_{\text{eff}} \gtrsim 0.1$ . These distributions, however, remain consistent within 90% credible intervals. This is illustrated in the bottom two panels of Figure 13. These features were also recovered with same analyses applied to GWTC-3.0 data, albeit with less certainty (A. Ray et al. 2025). However, more recent GWTC-3.0 analyses find conflicting evidence, suggesting that the  $\chi_{\text{eff}}$  distribution of  $\approx 30 M_\odot$  BHs is positively skewed (J. Sadiq et al. 2025b; S. K. Roy et al. 2025).

The ISOLATED PEAK model (see also J. Godfrey et al. 2023) fits the data to a model containing multiple mass subpopulations with independent spin distributions. One subpopulation consists of a single peak in the mass distribution (which is inferred to center on  $\sim 10 M_\odot$ ), while other subpopulations are flexibly fit with the B-SPLINE method. Applying these analyses to GWTC-4.0 suggests that BHs within the  $\sim 10 M_\odot$  peak have a spin magnitude distribution consistent (within 90% credible intervals) with the rest of the BBH population. Meanwhile, although there is some overlap in the 90% credible regions of the cosine tilt distributions for both subpopulations, the distribution of tilts for BHs in the  $\sim 10 M_\odot$  peak favors alignment and is inconsistent with isotropy. The distribution of cosine tilts for BHs outside this mass peak appears more symmetrical about  $\cos \theta = 0$  and does not rule out isotropy. Roughly speaking, this corresponds to a distribution of  $\chi_{\text{eff}}$  that may be symmetrical about zero for the BBH population outside of the  $\sim 10 M_\odot$  peak. Inside this mass peak, however, the implied  $\chi_{\text{eff}}$  distribution skews toward positive values.



**Figure 13.** Top: inferred distributions of effective inspiral spin  $\chi_{\text{eff}}$  in the correlated mass–spin BGP analysis. The solid lines give the median, while the shaded regions indicate the 90% credible intervals. In blue, we have the  $\chi_{\text{eff}}$  distribution of BBH systems with at least one mass inside the  $30\text{--}40 M_\odot$  peak range. In orange, we have the  $\chi_{\text{eff}}$  distribution of BBH systems masses outside the  $30\text{--}40 M_\odot$  peak range. While the two distributions are consistent within 90% credible intervals, systems outside the peak range appear to favor a distribution of  $\chi_{\text{eff}}$  skewed toward more positive values. Meanwhile, systems inside the peak range appear to favor a more symmetrical distribution about  $\chi_{\text{eff}} = 0$ . Middle: inferred distributions of primary mass from the correlated mass–spin BGP analysis. Bottom: inferred distributions of secondary mass from the correlated mass–spin BGP analysis. In both mass plots, blue shows the distribution for systems with small spins,  $\chi_{\text{eff}}$  in the range  $(-0.05, 0.05)$ , while orange shows the distribution for systems with larger spins,  $\chi_{\text{eff}}$  in the range  $(0.1, 0.2)$ . Note the preference for a higher proportion of mergers with masses  $\approx 30 - 40 M_\odot$  for low spin systems (blue).

We also model a correlation between primary mass and  $\chi_{\text{eff}}$  using a copula model (see Appendix B.6). Fitting this COPULA model with GWTC-4.0 data, we infer a correlation of  $\kappa_{m_1, \text{eff}} = 0.35^{+1.58}_{-1.41}$  between  $m_1$  and  $\chi_{\text{eff}}$ . Hence, the COPULA analysis finds no evidence for a single, smooth, population-wide correlation between primary mass and  $\chi_{\text{eff}}$ .

Broadly, our analyses of the joint mass and spin distribution recover similar features to recent works that probe for features in GWTC-3.0. First, analyses of GWTC-3.0 do not find evidence for a smoothly correlated distribution in primary mass and  $\chi_{\text{eff}}$  (M. Safarzadeh et al. 2020; S. Biscoveanu et al. 2022a; M. Fishbach et al. 2022; J. Heinzl et al. 2024, 2025b;

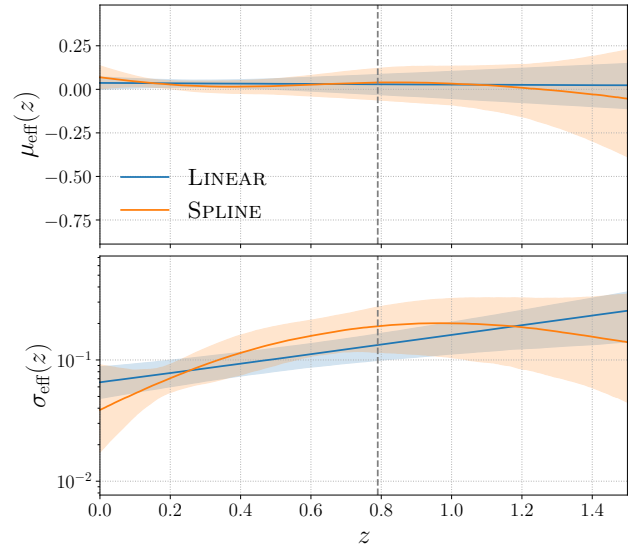
F. Antonini et al. 2025b), as is the case in this work. Meanwhile, a number of analyses find evidence for separate subpopulations in mass and spin consistent with predictions of dynamical and field mergers. More specifically, these works tend to find a subpopulation with lower masses and smaller, mostly aligned spins, and a second subpopulation of heavier binaries with larger, isotropically distributed spins, where the subpopulations transition around  $\sim 40 M_{\odot}$  (Y.-Z. Wang et al. 2022; M. Mould et al. 2022b; J. Godfrey et al. 2023; Y.-J. Li et al. 2024; F. Antonini et al. 2025b; G. Pierra et al. 2024; W.-H. Guo et al. 2024; Y.-J. Li et al. 2025; J. Sadiq et al. 2025b). While the analyses presented in this work do not recover this exact feature (nor do they probe directly for it), the ISOLATED PEAK model’s preference for aligned spins at  $\sim 10 M_{\odot}$  and isotropically distributed spins at higher masses may be related.

### 6.5.3. Redshift and Spin Correlations

We find evidence that the  $\chi_{\text{eff}}$  distribution broadens as redshift increases up to  $z \sim 1$ . We again look for correlations between redshift and  $\chi_{\text{eff}}$  by modeling the mean and width of the  $\chi_{\text{eff}}$  distribution with a linear dependence on redshift (see Appendix B.7). S. Biscoveanu et al. (2022a) employed a LINEAR model for  $(z, \chi_{\text{eff}})$  to analyze GWTC-3.0 data, finding no evidence for redshift dependence in the mean of the  $\chi_{\text{eff}}$  distribution, but suggesting that the  $\chi_{\text{eff}}$  distribution broadens with increasing redshift ( $\delta \ln \sigma_{\text{eff}|z} > 0$  at 98.6% credibility). Updating this analysis to include O4a data, we find more evidence for a broadening in the  $\chi_{\text{eff}}$  distribution with redshift, with  $\delta \ln \sigma_{\text{eff}|z} > 0$  now inferred at 99.4% credibility. The mean and width of the  $\chi_{\text{eff}}$  distribution as functions of redshift are shown in Figure 14.

The SPLINE model, which models the redshift dependence on the mean and width of the  $\chi_{\text{eff}}$  distribution flexibly with cubic splines (see Appendix B.8), is broadly consistent with the LINEAR model. The exception is that the SPLINE model tends to recover the prior beyond a redshift of  $z \gtrsim 1$ . This likely indicates that the LINEAR model is fitting a trend at low redshifts, then extending this trend to redshifts  $z \gtrsim 1$  due to a lack of flexibility. To further illustrate this point, the gray dashed line in Figure 14 indicates the redshift under which 90% of the catalog’s cumulative posterior support is contained. Roughly speaking, this means our inferences above this redshift are informed by only  $\sim 10\%$  of the data. Therefore, while we find evidence that the  $\chi_{\text{eff}}$  distribution broadens as binaries approach  $z \sim 1$ , we are unable to determine if this trend continues at higher redshifts.

We also model a correlation between redshift and  $\chi_{\text{eff}}$  using a copula model, with variable correlation  $\kappa_{z,\text{eff}}$  (see Appendix B.6). In contrast to the above analyses, the COPULA model finds evidence for a positive correlation in  $(z, \chi_{\text{eff}})$ , inferring a value of  $\kappa_{z,\text{eff}} = 4.25^{+2.59}_{-3.01}$  (or  $\kappa_{z,\text{eff}} > 0$  with 96.9% credibility). While the COPULA model lacks the flexibility to fit a broadening directly, the long (albeit shallow) posterior tails reaching into both large-negative and large-positive values for  $\kappa_{z,\text{eff}}$  may relate to the broadening in the  $\chi_{\text{eff}}$  distribution recovered by the LINEAR and SPLINE models (see Appendix D.6). If the  $z$ -dependent broadening and constant mean of the  $\chi_{\text{eff}}$  distribution from the LINEAR and SPLINE models is to be believed, it is unclear why the posterior on  $\kappa_{z,\text{eff}}$  skews toward positive values, rather than being symmetric about zero.



**Figure 14.** The inferred mean (top) and width (bottom) of the  $\chi_{\text{eff}}$  distribution as a function of redshift for the LINEAR model (blue) and the SPLINE model (orange). The shaded regions give the 90% credible intervals. The gray dashed line indicates the redshift under which 90% of the cumulative posterior probability lies across all events in GWTC-4.0. Therefore, inferences above this redshift are dominated by the prior or population model. Note the logarithmic scale on the width (bottom panel). In either model, we find evidence that the width of the effective inspiral spin distribution increases with redshift up to  $z \sim 1$ .

It is unclear what this broadening in the  $\chi_{\text{eff}}$  distribution at greater redshifts might imply astrophysically. Provided BH progenitors experience significant spin up due to tidal torques, smaller orbital separations and periods will result in more efficient spin up of BBH components (M. Zaldarriaga et al. 2018; M. Mapelli 2020; S. S. Bavera et al. 2021, 2022; J. Fuller & W. Lu 2022). Of course, smaller orbital separations correspond to shorter delay times to merger. This means that these systems may contribute more to the merger rate in the earlier Universe (higher  $z$ ), where systems with wider orbits have not had time to merge. Furthermore, given that higher metallicity systems are expected to evolve to longer orbital periods due to experiencing more mass loss during core helium burning (Y. Qin et al. 2018; J. Fuller & W. Lu 2022), one might predict that larger spin magnitudes should be observed in regions of lower metallicity and thus also at higher redshifts. However, the correlation in the LINEAR and SPLINE models is between redshift and the width of the  $\chi_{\text{eff}}$  distribution rather than the mean. This includes an increasing number of systems with both large-positive and large-negative values of  $\chi_{\text{eff}}$ . An increase in systems with large-negative  $\chi_{\text{eff}}$  may be somewhat difficult to square with the above hypothesis, given that tidal spin up is only relevant in isolated systems and that large supernovae kicks are required to misalign the BH spins so significantly (V. Kalogera 2000; D. Wysocki et al. 2018; D. Gerosa et al. 2018; T. A. Callister et al. 2021a; N. Steinle & M. Kesden 2021; S. Stevenson 2022; T. M. Tauris 2022; V. Baibhav & V. Kalogera 2024). On the other hand, if the COPULA results are to be taken at face value, the preference for a positive correlation in  $(z, \chi_{\text{eff}})$  fits more neatly with the aforementioned hypothesis.

Another possibility, following discussion from Section 6.3, is that multiple separate subpopulations of BBH mergers are being observed, where the more dominant (in terms of redshift-dependent merger rate) subpopulation changes at

some nearby redshift. HMs becoming more dominant at higher redshifts, for example, could potentially explain such a broadening in the effective spin distribution. This interpretation would also imply some level of correlation between mass and redshift, which we do not find evidence for below in Section 6.5.4.

As a final caveat, using GWTC-3.0 data, S. Biscoveanu et al. (2022a) fit the BBH population to a model in which the  $\chi_{\text{eff}}$  distribution is linearly dependent on both primary mass and redshift. In doing so, the authors find degeneracies between the  $(m_1, \chi_{\text{eff}})$  and  $(z, \chi_{\text{eff}})$  correlations. While we do not explore correlations beyond two dimensions in this work, we acknowledge that the assumption of independence between other pairs of parameters may have notable effects on our inferences.

#### 6.5.4. Redshift and Mass Correlations

Finally, we consider potential correlations between BBH mass and redshift. We do not find evidence for evolution in the mass distribution with redshift. We emphasize that these inferences are constrained to the nearby Universe, with relatively little data beyond  $z \sim 1$  (19 out of 153 BBH events having posteriors consistent with  $z > 1$  to 90% credibility). We model correlations between primary mass and redshift using a copula with correlation  $\kappa_{m_1, z}$  (see Appendix B.6). Using this COPULA model, we infer a correlation of  $\kappa_{m_1, z} = 1.07^{+2.37}_{-2.46}$ . We also search for correlations between mass and redshift using a BGP analysis that allows for covariance in  $m_1$  and  $z$  (see Appendix C.2). Similarly, this analysis finds that the mass distribution does not show a distinguishable evolution with redshift (see Appendix D.6). This conclusion is mostly in line with studies using GWTC-3.0, which are also unable to infer any correlation between mass and redshift with confidence (M. Fishbach et al. 2021; J. Sadiq et al. 2022; L. A. C. van Son et al. 2022b; C. Karathanasis et al. 2023; A. Ray et al. 2023a; J. Heinzel et al. 2024, 2025b; M. Lalleman et al. 2025; J. Sadiq et al. 2025a). This is with the exception of S. Rinaldi et al. (2024) finding a positive correlation between BBH primary mass and redshift, although a novel method is used to account for selection effects.

## 7. Conclusion

In this paper, we present population-level analyses of events included in the fourth Gravitational-Wave Transient Catalog GWTC-4.0. This dataset more than doubles the number of events analyzed compared to the previous catalog. Our main findings are:

1. Features identified in the third catalog GWTC-3.0 persist, including clear overabundances in the mass distribution at  $1\text{--}2 M_\odot$  and around  $10 M_\odot$ , and a feature near  $35 M_\odot$ . There is no conclusive evidence to either support or refute a suppression of the merger rate between these features.
2. We estimate the merger rates at redshift  $z = 0$  to be  $8.8 - 250 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for binary NSs,  $9.3 - 86 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for NS-black hole binaries, and  $13 - 26 \text{ Gpc}^{-3} \text{ yr}^{-1}$  for binary black holes.
3. The binary black hole primary mass distribution is well described by a broken power law, shallow at low masses and steep at high masses, modulated by overdensities

near  $10 M_\odot$  and  $35 M_\odot$ . A weakly modeled approach finds evidence of overdensity around  $20 M_\odot$ .

4. Black holes in the  $35 M_\odot$  feature tend to pair with companions of similar mass more frequently than lower-mass black holes do.
5. The distribution of effective inspiral spins is asymmetric about  $\chi_{\text{eff}} = 0$  and is skewed toward positive  $\chi_{\text{eff}}$  values. Spin magnitudes span a broad range from 0 to 1, although  $\sim 90\%$  of BHs have  $\chi < 0.6$ .
6. The redshift evolution of the binary black hole merger rate  $\mathcal{R}(z)$  remains consistent with the cosmic star-formation rate density. A merger rate uniform in comoving volume and source-frame time is ruled out.
7. We find that black holes outside the  $30\text{--}40 M_\odot$  range prefer an asymmetric effective inspiral spin distribution skewed toward higher values, while those within this range show no such preference. Compared to GWTC-3.0, we observe stronger evidence that the width of the effective spin distribution increases with redshift and weaker evidence for an anticorrelation between mass ratio and effective spin. No redshift evolution is observed in the mass distribution.
8. The NS mass distribution remains consistent with previous results, favoring a broad distribution of NS masses between  $1 M_\odot$  and  $3 M_\odot$ .

The analysis of this expanded dataset refines the statistical significance of previously reported trends and reveals new features in the population of compact binary mergers. Several of these findings, such as the persistent  $\sim 10 M_\odot$  feature, pose challenges to current models of supernova physics, binary mass transfer, and dynamical formation in dense stellar environments. Future data from the remainder of the fourth observing run O4 will further enhance our understanding and may uncover additional structure in the population.

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use “A. G. Abac et al. (LIGO-Virgo-KAGRA Collaboration), ...” or similar phrasing, depending on journal convention.

## Appendix A Hierarchical Inference Details

### A.1. Likelihood Estimation

The analytic integrals in Equation (2) are not tractable, and so we estimate the integrals using Monte Carlo estimation (V. Tiwari 2018; W. M. Farr 2019; R. Essick & W. Farr 2022; C. Talbot & J. Golomb 2023). For example, the estimator for the likelihood  $\hat{\mathcal{L}}(d_i|\Lambda)$  is

$$\hat{\mathcal{L}}(d_i|\Lambda) \propto \frac{1}{N_{\text{PE}}} \sum_{j=1}^{N_{\text{PE}}} \frac{\pi(\theta_{ij}|\Lambda)}{p(\theta_{ij})}, \quad (\text{A1})$$

where  $\{\theta_{ij}\}_{j=1}^{N_{\text{PE}}}$  are a collection of  $N_{\text{PE}}$  samples from the posterior on the GW parameters of the  $i$ th event  $d_i$ . We divide out by the parameter estimation prior  $p(\theta)$ , and so the Monte Carlo estimator in Equation (A1) converges to the  $i$ th integral inside the product of Equation (2) in the limit of  $N_{\text{PE}} \rightarrow \infty$ .

Similarly, the estimator for the selection efficiency  $\hat{\xi}$  is (V. Tiwari 2018; W. M. Farr 2019; R. Essick & W. Farr 2022)

$$\hat{\xi}(\Lambda) \propto \frac{1}{N_{\text{draw}}} \sum_{j=1}^{N_{\text{found}}} \frac{\pi(\theta_j|\Lambda)}{\pi(\theta_j|\Lambda_{\text{draw}})}, \quad (\text{A2})$$

where  $N_{\text{draw}}$  events with parameters  $\theta_i$  are injected into representative noise from the detectors. The search pipelines then search these synthetically generated data and recover some subset  $N_{\text{found}}$  of the events with the detection statistic exceeding some threshold. In the limit of  $N_{\text{draw}} \rightarrow \infty$ , this approaches the true integral in Equation (3).

Because we only have a finite number of samples from each event and finite  $N_{\text{draw}}$ , we must be careful to account for the intrinsic variance in the estimation of the likelihood. To be sure our Monte Carlo estimators for the likelihood are trustworthy, we study the impact of Monte Carlo uncertainty in every inference we perform. Specifically, we compute the variance in the log-likelihood estimator, which varies across parameter space due to our resampling techniques in Equations (A1) and (A2). Propagating the uncertainty in the log-likelihood along independent degrees of freedom, the variance in the log-likelihood estimator  $\sigma_{\ln \hat{\mathcal{L}}}^2$  in combining Equations (2), (3), and (A1) can be estimated as (e.g., R. Essick & W. Farr 2022)

$$\sigma_{\ln \hat{\mathcal{L}}}^2(\Lambda) = \sum_{i=1}^{N_{\text{det}}} \frac{\sigma_{\hat{\mathcal{L}}_i}^2(\Lambda)}{\hat{\mathcal{L}}_i(\Lambda)^2} + N(\Lambda)^2 \sigma_{\hat{\xi}}^2(\Lambda), \quad (\text{A3})$$

where

$$\sigma_{\hat{\mathcal{L}}_i}^2(\Lambda) = \frac{1}{N_{\text{PE}}} \left[ \frac{1}{N_{\text{PE}} - 1} \times \sum_{j=1}^{N_{\text{PE}}} \left( \frac{\pi(\theta_{ij}|\Lambda)}{p(\theta_{ij})} \right)^2 - \hat{\mathcal{L}}_i(\Lambda)^2 \right] \quad (\text{A4})$$

is the Monte Carlo variance in the single event Monte Carlo integrals of Equation (A1) and

$$\sigma_{\xi}^2(\Lambda) = \frac{1}{N_{\text{draw}}} \left[ \frac{1}{N_{\text{draw}} - 1} \times \sum_{j=1}^{N_{\text{found}}} \left( \frac{\pi(\theta_j|\Lambda)}{p(\theta_j|\Lambda_{\text{draw}})} \right)^2 - \hat{\xi}(\Lambda)^2 \right] \quad (\text{A5})$$

is the variance in the detection efficiency Monte Carlo integral of Equation (A2). When the rate-marginalized likelihood of Equation (4) is used,  $\sigma_{\ln \hat{\mathcal{L}}}^2$  takes a slightly different form

$$\sigma_{\ln \hat{\mathcal{L}}}^2(\Lambda) = \sum_{i=1}^{N_{\text{det}}} \frac{\sigma_{\hat{\mathcal{L}}_i}^2(\Lambda)}{\hat{\mathcal{L}}_i(\Lambda)^2} + N_{\text{det}}^2 \frac{\sigma_{\xi}^2(\Lambda)}{\hat{\xi}(\Lambda)^2}. \quad (\text{A6})$$

It has been shown that GW population inference can be biased when the variance in log-likelihood estimator exceeds 1. Consequently, we adopt a threshold on  $\sigma_{\ln \hat{\mathcal{L}}}^2$  of 1 to manage the bias of the posterior. Above this threshold the likelihood estimate may not be converged, and thus we ignore posterior samples with variances above this chosen threshold. Equation (A3) describes the pointwise variance in the estimation of the log-likelihood. However, for accurate sampling of the posterior we only require the difference of log-likelihoods to be small. A small pointwise log-likelihood variance is *sufficient* for the variance of the difference of log-likelihoods to be small but not *necessary*, rendering our threshold conservative (W. M. Farr 2019; R. Essick & W. Farr 2022). Indeed, for some models, a large region of hyperparameter space is removed by this threshold, limiting the range of potential populations that can be explored; for an example, see Appendix D.3. Improvements to likelihood estimation are an active area of ongoing research (D. Wysocki et al. 2019; Z. Doctor et al. 2019; V. Delfavero et al. 2021; J. Golomb & C. Talbot 2022; M. Mould et al. 2024; A. Hussain et al. 2026; M. Mancarella & D. Gerosa 2025).

### A.2. Sampling Techniques

In each model, we draw samples from the posterior to study the population distributions consistent with the data and the population model. We draw samples using a variety of stochastic sampling algorithms, where the exact approach depends on the model. For most strongly modeled approaches, we use the nested sampler DYNesty (J. S. Speagle 2020) wrapper in BILBY (G. Ashton et al. 2019) and the GWPOPULATION implementation of the hierarchical likelihood (C. Talbot et al. 2025a).

However, our weakly modeled approaches tend to have a large number of hyperparameters and so have a high dimensional posterior. Nested sampling struggles with high dimensional distributions, so we use the Hamiltonian Monte Carlo (HMC) adaptive No-U-Turn Sampler (NUTS) implementation in NUMPYRO (D. Phan et al. 2019; E. Bingham et al. 2019). The NUMPYRO adaptive NUTS requires an autodifferentiable implementation of the likelihood, which we write in JAX (J. Bradbury et al. 2018). This gradient information allows the NUTS algorithm to efficiently explore high dimensional posteriors.

## Appendix B Summary of Models Used in the Strongly Modeled Approach

### B.1. Mass Model for the Full CBC Population

Our strongly modeled FULLPOP-4.0 mass model is based on POWER LAW+DIP (M. Fishbach et al. 2020), BROKEN POWER LAW + DIP (A. M. Farah et al. 2022), and MULTIPDB (U. Mali & R. Essick 2025). It is also similar to the POWER LAW+DIP+BREAK model (R. Abbott et al. 2023a), but in our FULLPOP-4.0 model we now include additional structure. We allow for the possibility of an upper mass gap, as well as separate pairing functions for NS-containing binaries and BBHs. Additionally, we include explicit peaks at low and mid-range BH masses to capture the  $\sim 9\text{--}10 M_{\odot}$  and  $\sim 30\text{--}40 M_{\odot}$  features found by the weakly modeled approaches. As discussed in Section 4, we find that the addition of a low-mass BH peak eliminates the need to explicitly model a gap between NSs and BHs masses.

Our mass model is parameterized as

$$\pi(m_1, m_2|\Lambda) \propto \pi_m(m_1|\Lambda) \pi_m(m_2|\Lambda) \times f(m_1, m_2) \Theta(m_2 < m_1), \quad (\text{B1})$$

where the one-dimensional mass distribution  $\pi_m(m|\Lambda)$  is given by

$$\begin{aligned} \pi_m(m|\Lambda) = & [1 + c_1 \mathcal{N}_{[m_{\text{min}}, m_{\text{max}}]}(m|\mu_1, \sigma_1) + c_2 \mathcal{N}_{[m_{\text{min}}, m_{\text{max}}]}(m|\mu_2, \sigma_2)] \\ & \times n_1(m | m_{\text{NSmax}}, m_{\text{BHmin}}, \eta_{\text{NSmax}}, \eta_{\text{BHmin}}, A) \\ & \times n_2(m | m_{\text{UMGmin}}, m_{\text{UMGmax}}, \eta_{\text{UMGmin}}, \eta_{\text{UMGmax}}, A_2) \\ & \times h(m | m_{\text{NSmin}}, \eta_{\text{NSmin}}) l(m | m_{\text{BHmax}}, \eta_{\text{BHmax}}) \\ & \times \begin{cases} m^{\alpha_1} & \text{if } m < m_{\text{NSmax}} \\ m^{\alpha_{\text{dip}}} m_{\text{NSmax}}^{\alpha_1 - \alpha_{\text{dip}}} & \text{if } m_{\text{NSmax}} \leq m < m_{\text{BHmin}} \\ m^{\alpha_2} m_{\text{NSmax}}^{\alpha_1 - \alpha_{\text{dip}}} m_{\text{BHmin}}^{\alpha_{\text{dip}} - \alpha_2} & \text{if } m \geq m_{\text{BHmin}} \end{cases} \end{aligned} \quad (\text{B2})$$

This  $\pi_m(m|\Lambda)$  represents a universal mass function to describe the primary and secondary mass distributions. Note that the marginal mass distribution is different from the universal mass distribution due to the pairing formalism.  $\mathcal{N}_{[a,b]}(\mu, \sigma)$  represents a truncated normal distribution over  $[a, b]$  with location and width parameters  $\mu$  and  $\sigma$ . The high-pass, low-pass, and notch functions are defined as follows:

$$l(m|m_{\text{BHmax}}, \eta_{\text{BHmax}}) = \left[ 1 + \left( \frac{m}{m_{\text{BHmax}}} \right)^{\eta_{\text{BHmax}}} \right]^{-1}, \quad (\text{B3})$$

$$h(m|m_{\text{NSmin}}, \eta_{\text{NSmin}}) = 1 - l(m|m_{\text{NSmin}}, \eta_{\text{NSmin}}), \quad (\text{B4})$$

$$\begin{aligned} n_1(m|m_{\text{NSmax}}, m_{\text{BHmin}}, \eta_{\text{NSmax}}, \eta_{\text{BHmin}}, A) \\ = 1 - A l(m|m_{\text{NSmax}}, \eta_{\text{NSmax}}) h(m|m_{\text{BHmin}}, \eta_{\text{BHmin}}), \end{aligned} \quad (\text{B5})$$

$$\begin{aligned} n_2(m|m_{\text{UMGmin}}, m_{\text{UMGmax}}, \eta_{\text{UMGmin}}, \eta_{\text{UMGmax}}, A_2) \\ = 1 - A_2 l(m|m_{\text{UMGmin}}, \eta_{\text{UMGmin}}) \\ h(m|m_{\text{UMGmax}}, \eta_{\text{UMGmax}}). \end{aligned} \quad (\text{B6})$$

The pairing function

$$f(m_1, m_2|\beta_{\text{BH}}, \beta_{\text{NS}}) = \begin{cases} \left( \frac{m_2}{m_1} \right)^{\beta_1} & \text{if } m_2 < 5 M_{\odot} \\ \left( \frac{m_2}{m_1} \right)^{\beta_2} & \text{if } m_2 > 5 M_{\odot} \end{cases} \quad (\text{B7})$$

controls how much merging binaries favor/disfavor equal masses. We allow for alternative pairing for binaries with very

**Table 4**  
Summary of FULLPOP-4.0 Model Parameters and Priors

| Category         | Parameter                | Unit      | Description                                                   | Prior        |
|------------------|--------------------------|-----------|---------------------------------------------------------------|--------------|
| Pairing Function | $\beta_1$                | ...       | Spectral index below $5 M_\odot$                              | $U(-2, 3)$   |
|                  | $\beta_2$                | ...       | Spectral index above $5 M_\odot$                              | $U(-2, 7)$   |
| Broken Power Law | $\alpha_1$               | ...       | Power law below $m_{\text{NS max}}$                           | $U(-10, 2)$  |
|                  | $\alpha_{\text{dip}}$    | ...       | Power law between $m_{\text{NS max}}$ and $m_{\text{BH min}}$ | $U(-3, 2)$   |
|                  | $\alpha_2$               | ...       | Power law above $m_{\text{BH min}}$                           | $U(-3, 2)$   |
|                  | $m_{\text{brk}}$         | $M_\odot$ | Break point between $\alpha_1$ and $\alpha_2$                 | 5            |
| Highpass Filter  | $m_{\text{NS min}}$      | $M_\odot$ | Low-mass roll off                                             | $U(1, 1.4)$  |
|                  | $\eta_{\text{min}}$      | ...       | Sharpness at $m_{\text{NS min}}$                              | 50           |
| Lowpass Filter   | $m_{\text{BH max}}$      | $M_\odot$ | High-mass roll off                                            | $U(60, 200)$ |
|                  | $\eta_{\text{max}}$      | ...       | Sharpness at $m_{\text{BH max}}$                              | $U(-4, 12)$  |
| Low-mass Notch   | $m_{\text{NS max}}$      | $M_\odot$ | Lower notch edge                                              | $U(1.4, 5)$  |
|                  | $\eta_1^{\text{low}}$    | ...       | Sharpness at $m_{\text{NS max}}$                              | 50           |
|                  | $m_{\text{BH min}}$      | $M_\odot$ | Upper notch edge                                              | $U(5, 9)$    |
|                  | $\eta_1^{\text{high}}$   | ...       | Sharpness at $m_{\text{BH min}}$                              | 50           |
|                  | $A_1$                    | ...       | Notch depth                                                   | 0            |
| High-mass Notch  | $m_{\text{UMGmin}}$      | $M_\odot$ | Lower notch edge                                              | $U(30, 90)$  |
|                  | $\eta_2^{\text{low}}$    | ...       | Sharpness at $m_{\text{UMGmin}}$                              | 30           |
|                  | $m_{\text{UMGmax}}$      | $M_\odot$ | Upper notch edge                                              | $U(60, 150)$ |
|                  | $\eta_2^{\text{high}}$   | ...       | Sharpness at $m_{\text{UMGmax}}$                              | 30           |
|                  | $A_2$                    | ...       | Depth of high-mass notch                                      | $U(0, 1)$    |
| Low-mass Peak    | $\mu_2^{\text{peak}}$    | $M_\odot$ | Peak location                                                 | $U(6, 12)$   |
|                  | $\sigma_2^{\text{peak}}$ | $M_\odot$ | Peak width                                                    | $U(0, 5)$    |
|                  | $c_2$                    | ...       | Peak height                                                   | $U(0, 500)$  |
| High-mass Peak   | $\mu_1^{\text{peak}}$    | $M_\odot$ | Peak location                                                 | $U(17, 50)$  |
|                  | $\sigma_1^{\text{peak}}$ | $M_\odot$ | Peak width                                                    | $U(4, 20)$   |
|                  | $c_1$                    | ...       | Peak height                                                   | $U(0, 1000)$ |

**Note.**  $U(x, y)$  denotes a uniform prior between  $x$  and  $y$ .

light secondary masses (NSBHs or BBH with the secondary component in the lower-mass gap, e.g., GW190814; R. Abbott et al. 2020c). We show the priors and describe the parameters of the FULLPOP-4.0 model in Table 4.

### B.2. Neutron Star Mass Models

Following previous work (P. Landry & J. S. Read 2021; R. Abbott et al. 2023a), the mass distribution of NS-containing events is modeled as

$$\pi(m_1, m_2|\Lambda) \propto \begin{cases} \pi(m_1|\Lambda) \pi(m_2|\Lambda) & \text{if BNS,} \\ U(3 M_\odot, 60 M_\odot) \pi(m_2|\Lambda) & \text{if NSBH.} \end{cases} \quad (\text{B8})$$

To model  $\pi(m|\Lambda)$ , we use either of the following models

### 1. POWER model:

$$\pi(m|\Lambda) \propto \begin{cases} m^\alpha & \text{if } m_{\text{min}} \leq m \leq m_{\text{max}}, \\ 0 & \text{otherwise.} \end{cases} \quad (\text{B9})$$

### 2. PEAK model:

$$\pi(m|\Lambda) \propto \begin{cases} \exp\left[-\frac{(m-\mu)^2}{2\sigma^2}\right] & \text{if } m_{\text{min}} \leq m \leq m_{\text{max}}, \\ 0 & \text{otherwise.} \end{cases} \quad (\text{B10})$$

See Table 5 for a description of the parameters used in the model and the corresponding prior ranges.

### B.3. Binary Black Hole Mass Models

**BROKEN POWER LAW + 2 PEAKS:** the fiducial BBH mass model is a mixture between a broken power law and two left-truncated Gaussian peaks, with low-mass tapering applied to the full distribution. The broken power law is given by

$$p_{\text{BP}}(m_1|\alpha_1, \alpha_2, m_{\text{break}}, m_{1,\text{low}}, m_{\text{high}}) = \frac{1}{N} \begin{cases} \left(\frac{m_1}{m_{\text{break}}}\right)^{-\alpha_1} & m_{1,\text{low}} \leq m_1 < m_{\text{break}} \\ \left(\frac{m_1}{m_{\text{break}}}\right)^{-\alpha_2} & m_{\text{break}} \leq m_1 < m_{\text{high}}, \end{cases} \quad (\text{B11})$$

where  $\alpha_1$  and  $\alpha_2$  are the power-law indices, the transition between the low-mass and high-mass power law occurs at  $m_{\text{break}}$ , and the normalization constant is

$$N = m_{\text{break}} \left[ \frac{1 - \left(\frac{m_{1,\text{low}}}{m_{\text{break}}}\right)^{1-\alpha_1}}{1 - \alpha_1} + \frac{\left(\frac{m_{1,\text{high}}}{m_{\text{break}}}\right)^{1-\alpha_2} - 1}{1 - \alpha_2} \right]. \quad (\text{B12})$$

The full mixture distribution  $\pi(m_1|\Lambda)$  is

$$\begin{aligned} \pi(m_1|\Lambda) \propto & [\lambda_0 p_{\text{BP}}(m_1|\alpha_1, \alpha_2, m_{\text{break}}, m_{1,\text{low}}, m_{\text{high}}) \\ & + \lambda_1 \mathcal{N}_l(m_1|\mu_1, \sigma_1, \text{low} = m_{1,\text{low}}) \\ & + (1 - \lambda_0 - \lambda_1) \mathcal{N}_l(m_1|\mu_2, \sigma_2, \text{low} = m_{1,\text{low}})] \\ & \times S(m_1|m_{1,\text{low}}, \delta_{m,1}), \end{aligned} \quad (\text{B13})$$

where  $\mathcal{N}_l$  is a left-truncated normal distribution. The Planck tapering function  $S$  ensures a smooth turn-on of the distribution in the range  $(m_{1,\text{low}}, m_{1,\text{low}} + \delta_{m,1})$  and is given by

$$S(m|m_{\text{low}}, \delta_m) = \begin{cases} 0 & m < m_{\text{low}}, \\ [1 + f(m - m_{\text{low}}, \delta_m)]^{-1} & m_{\text{low}} \leq m < m_{\text{low}} + \delta_m, \\ 1 & m_{\text{low}} + \delta_m \leq m, \end{cases} \quad (\text{B14})$$

**Table 5**  
Summary of POWER and PEAK NS Mass Model Parameters

| Parameter  | Unit        | Description                                                         | Prior           |
|------------|-------------|---------------------------------------------------------------------|-----------------|
| $\alpha$   | ...         | Spectral index for the power law in the POWER NS mass distribution. | $U(-15, 5)$     |
| $m_{\min}$ | $M_{\odot}$ | Minimum mass of the NS mass distribution.                           | $U(1.0, 1.5)$   |
| $m_{\max}$ | $M_{\odot}$ | Maximum mass of the NS mass distribution.                           | $U(1.5, 3.0)$   |
| $\mu$      | $M_{\odot}$ | Location of the Gaussian peak in the PEAK NS mass distribution.     | $U(1.0, 3.0)$   |
| $\sigma$   | $M_{\odot}$ | Width of the Gaussian peak in the PEAK NS mass distribution.        | $U(0.01, 2.00)$ |

**Note.**  $U(x, y)$  denotes a uniform prior between  $x$  and  $y$ .

**Table 6**  
Summary of BROKEN POWER LAW + 2 PEAKS Model Parameters and Priors

| Parameter              | Description                                                                                    | Prior                            |
|------------------------|------------------------------------------------------------------------------------------------|----------------------------------|
| $\alpha_1$             | Spectral index of first primary mass power law                                                 | $U(-4, 12)$                      |
| $\alpha_2$             | Spectral index of second primary mass power law                                                | $U(-4, 12)$                      |
| $m_{\text{break}}$     | Power-law break location                                                                       | $U(20, 50)$                      |
| $\mu_1$                | Location of the first peak                                                                     | $U(5, 20)$                       |
| $\sigma_1$             | Width of the first peak                                                                        | $U(0, 10)$                       |
| $\mu_2$                | Location of the second peak                                                                    | $U(25, 60)$                      |
| $\sigma_2$             | Width of the second peak                                                                       | $U(0, 10)$                       |
| $m_{1,\text{low}}$     | Lower edge of taper function                                                                   | $U(3, 10)$                       |
| $\delta_{m,1}$         | Mass range of low-mass tapering                                                                | $U(0, 10)$                       |
| $\lambda_0, \lambda_1$ | Mixing fractions between power law and peaks                                                   | $\text{Dir}(\alpha = (1, 1, 1))$ |
| $m_{\text{high}}$      | Maximum mass for distribution, which is pinned to $m_{\text{high}} = 300 M_{\odot}$ by default | $\delta(m_{\text{high}} - 300)$  |
| $\beta_q$              | Spectral index of mass ratio power law                                                         | $U(-2, 7)$                       |
| $m_{2,\text{low}}$     | Lower edge of taper function in $m_2$                                                          | $U(3, m_{1,\text{low}})$         |
| $\delta_{m,2}$         | Mass range of low-mass tapering in $m_2$                                                       | $U(0, 10)$                       |

**Note.** The priors for the EXTENDED BROKEN POWER LAW + 2 PEAKS model are the same except for the  $\beta_q$  parameters, which assume a prior of  $U(-10, 13)$ .

with

$$f(m', \delta_m) = \exp\left(\frac{\delta_m}{m'} + \frac{\delta_m}{m' - \delta_m}\right).$$

We model the mass ratio as a power law with index  $\beta_q$  and low-mass tapering applied to secondary mass  $m_2$ , conditioned on primary mass  $m_1$ ,

$$p_{\text{PL}}(q|m_1, \beta_q, m_{2,\text{low}}, \delta_{m,2}) \propto q^{\beta_q} S(m_1 q | m_{2,\text{low}}, \delta_{m,2}), \quad (\text{B15})$$

with the same tapering function defined above. We numerically normalize the mass ratio distribution as a function of primary mass, and interpolate the normalization to arbitrary primary masses with a log-uniform grid across primary mass. We define  $m_2 \lesssim m_1$ , and therefore must enforce  $m_{2,\text{low}} \lesssim m_{1,\text{low}}$ , which we enforce by the conditional priors described in Table 6, alongside the rest of the mass model priors.

**EXTENDED BROKEN POWER LAW + 2 PEAKS:** this model incorporates correlations between the primary mass and mass ratio, by allowing each primary mass mixture component in the BROKEN POWER LAW + 2 PEAKS to be associated with a separate power-law mass ratio model. In terms of the functions

**Table 7**  
Summary of POWER LAW REDSHIFT Model Parameter and Prior

| Parameter | Description                                       | Prior        |
|-----------|---------------------------------------------------|--------------|
| $\kappa$  | Power-law index on comoving merger rate evolution | $U(-10, 10)$ |

defined above, the model is expressed as

$$\begin{aligned} \pi(m_1, q|\mathbf{A}) \propto & [\lambda_0 p_{\text{BP}}(m_1|\alpha_1, \alpha_2, m_{\text{break}}, m_{1,\text{low}}, m_{\text{high}}) \\ & \times p_{\text{PL}}(q|m_1, \beta_q^{\text{BP}}, m_{2,\text{low}}^{\text{BP}}, \delta_{m,2}^{\text{BP}}) \\ & + \lambda_1 \mathcal{N}_l(m_1|\mu_1, \sigma_1, \text{low} = m_{1,\text{low}}) \\ & \times p_{\text{PL}}(q|m_1, \beta_q^{\text{peak1}}, m_{2,\text{low}}^{\text{peak1}}, \delta_{m,2}^{\text{peak1}}) \\ & + (1 - \lambda_0 - \lambda_1) \mathcal{N}_l(m_1|\mu_2, \sigma_2, \text{low} = m_{1,\text{low}}) \\ & \times p_{\text{PL}}(q|m_1, \beta_q^{\text{peak2}}, m_{2,\text{low}}^{\text{peak2}}, \delta_{m,2}^{\text{peak2}})] \\ & \times S(m_1|m_{1,\text{low}}, \delta_{m,1}), \end{aligned} \quad (\text{B16})$$

where the superscripts (BP, peak1, and peak2) denote the different mass ratio hyperparameters ( $\beta_q, m_{2,\text{low}}, \delta_{m,2}$ ) for the broken power-law, first Gaussian, and second Gaussian components. The priors on these hyperparameters are the same as those used in the BROKEN POWER LAW + 2 PEAKS model, listed in Table 6, except for the power-law index parameters  $\beta_q$ , which assume  $U(-10, 13)$ .

#### B.4. POWER LAW REDSHIFT Model

We model redshift evolution by the comoving merger rate density (Equation 5). In particular, we use the model

$$\pi(z|\kappa) \propto \frac{1}{1+z} \frac{dV_c}{dz} (1+z)^\kappa, \quad (\text{B17})$$

where the prefactor converts from a rate density in comoving volume and source frame time to detector frame time and redshift. In other words, the comoving rate density scales as  $\mathcal{R} \propto (1+z)^\kappa$ . We use a prior on  $\kappa$  as specified in Table 7.

#### B.5. Spin Models

BBH spins can be parameterized in several ways that are useful for GW data analysis. Here, we use dimensionless spin magnitudes for the BHs  $\chi_1$  and  $\chi_2$ , and cosine tilt angles  $\cos\theta_1$  and  $\cos\theta_2$ , as well as the effective spin parameters  $\chi_{\text{eff}}$  (E. Racine 2008; P. Ajith et al. 2011; T. Damour 2001) and  $\chi_p$  (P. Schmidt et al. 2011, 2012, 2015). The effective inspiral spin  $\chi_{\text{eff}}$  is used because it is typically the most precisely measured BBH spin parameter, due to its lower-order

appearance post-Newtonian expansions (K. G. Arun et al. 2009). Other parameterizations of spin precession exist (e.g., S. Fairhurst et al. 2020; D. Gerosa et al. 2021; L. M. Thomas et al. 2021) but for reasons of convention, we only work with the typical parameterization given in Equation (16) of A. G. Abac et al. (2025a). When modeling the effective spins, we use the analytic per-event parameter-estimation prior on  $\chi_{\text{eff}}$ ,  $\chi_p$ , and  $q$  (M. Iwaya et al. 2025) in the calculation of the hierarchical likelihood (Equation 2). For all models presented in this work, we assume that azimuthal angles  $\phi_i$  are distributed uniformly between 0 and  $2\pi$ —the same as their parameter estimation prior—due to their typically uninformative individual-event posteriors. See Table 3 of A. G. Abac et al. (2025a) for more information about spin parameters.

We report results with spin vectors defined at the reference frequencies used for inference on each signal (A. G. Abac et al. 2026a). The effective spin  $\chi_{\text{eff}}$  is approximately conserved throughout the inspiral (E. Racine 2008; D. Gerosa et al. 2015), so its population distribution should be unaffected by the choice of reference frequency. While the effective precessing spin  $\chi_p$  and the spin angles are dependent on reference frequency, they are comparatively weakly constrained by the data. Additionally, their parameter estimation priors are invariant under time evolution, meaning measurements are robust against different reference frequencies. At the current number of events and because of model dependence while measuring tilt distributions, we do not expect significant differences between the inferred tilt or  $\chi_p$  distributions at different reference frequencies (M. Mould & D. Gerosa 2022). Our approach is consistent with past LVK analyses, where evolved spins have not been used (B. P. Abbott et al. 2019a; R. Abbott et al. 2021a, 2023a).

### B.5.1. Component Spin Models

GAUSSIAN COMPONENT SPINS: we model the spin magnitudes ( $\chi_i$ ) as a truncated Gaussian distribution between 0 and 1, assuming they are identically and independently distributed:

$$\pi(\chi_i | \mu_\chi, \sigma_\chi) = \mathcal{N}_{[0,1]}(\chi_i | \mu_\chi, \sigma_\chi) \mathcal{N}_{[0,1]}(\chi_i | \mu_\chi, \sigma_\chi). \quad (\text{B18})$$

$$\begin{aligned} \pi(\cos \theta_i | \mu_t, \sigma_t, \zeta, t_{\min}) \\ = \begin{cases} \zeta \mathcal{N}_{[t_{\min}, 1]}(\cos \theta_i | \mu_t, \sigma_t) \mathcal{N}_{[t_{\min}, 1]}(\cos \theta_i | \mu_t, \sigma_t) + \frac{1 - \zeta}{(1 - t_{\min})^2} & \cos \theta_i > t_{\min}, \\ 0 & \cos \theta_i \leq t_{\min}. \end{cases} \end{aligned} \quad (\text{B20})$$

This choice attempts to rectify shortcomings of the nonsingular Beta distribution used to model the spin magnitudes in previous work (B. P. Abbott et al. 2019a; R. Abbott et al. 2021a, 2023a); see Equation (B21) below. The nonsingular Beta distribution is forced to go to  $\pi(\chi) = 0$  at  $\chi = 0, 1$ , which crucially does not allow for measurements of contributions to the population at  $\chi = 0$  or  $\chi = 1$ , even though nontrivial contributions may exist (T. A. Callister et al. 2022; S. Galadage et al. 2021; A. Hussain et al. 2026). Allowing the Beta distribution to be singular would add limited

**Table 8**  
Summary of GAUSSIAN COMPONENT SPINS Model Parameters for Spin Magnitudes (Equation B18) and Tilt Angles (Equation B19, B20)

| Parameter     | Description                                                          | Prior       |
|---------------|----------------------------------------------------------------------|-------------|
| $\mu_\chi$    | Location of the $\chi$ distribution                                  | U(0, 1)     |
| $\sigma_\chi$ | Width of the $\chi$ distribution                                     | U(0.005, 1) |
| $\mu_t$       | Location of the Gaussian component of the $\cos \theta$ distribution | U(−1, 1)    |
| $\sigma_t$    | Width of the Gaussian component of the $\cos \theta$ distribution    | U(0.01, 4)  |
| $\zeta$       | Fraction in the Gaussian component of the $\cos \theta$ distribution | U(0, 1)     |
| $t_{\min}$    | Minimum of the $\cos \theta$ distribution                            | U(−1, 1)    |

**Note.** U stands for a uniform prior.

additional model flexibility, only adding the option for  $\pi(\chi) = \infty$  at the  $\chi = 0, 1$ , but not anywhere in between 0 and  $\infty$ . Thus, we opt for the truncated Gaussian model, which can take on a continuous range of values at  $\chi$ 's boundaries.

We model the distribution of the cosine spin tilt angle ( $\cos \theta_i$ ) as a mixture between a Gaussian distribution truncated on  $-1$  to  $1$  and an isotropic distribution, assuming they are identically but *not* independently distributed:

$$\begin{aligned} \pi(\cos \theta_i | \mu_t, \sigma_t, \zeta) = \zeta \mathcal{N}_{[-1, 1]}(\cos \theta_i | \mu_t, \sigma_t) \\ \times \mathcal{N}_{[-1, 1]}(\cos \theta_i | \mu_t, \sigma_t) + \frac{1 - \zeta}{4}. \end{aligned} \quad (\text{B19})$$

We here allow for the location of the Gaussian subpopulation to vary, following S. Vitale et al. (2022), rather than fixing it at  $\mu_t = 1$  as was done in previous work (B. P. Abbott et al. 2019a; R. Abbott et al. 2021a, 2023a). Priors on the GAUSSIAN COMPONENT SPINS hyperparameters are given in Table 8.

MINIMUM TILT MODEL: for the spin tilts, we also use a model in which  $t_{\min}$  (where  $t \equiv \cos \theta$ ), a hard lower truncation of  $\pi(\cos \theta)$ , is informed by the data. In this case the population distribution becomes

Equation (B19) is the same as Equation (B20) with  $t_{\min} = -1$ . The prior on  $t_{\min}$  and other hyperparameters are given in Table 8.

BETA DISTRIBUTION SPIN MAGNITUDE: in Appendix D.2, we compare the GAUSSIAN COMPONENT SPINS model to alternatives. For the spin magnitudes, these are the Constrained and Unconstrained Beta Distributions, which both follow the form:

$$\pi(\chi_i | \alpha, \beta) \propto \chi_i^{\alpha-1} (1 - \chi_i)^{\beta-1}. \quad (\text{B21})$$

The Constrained Beta was the DEFAULT model for GWTC-3.0 (R. Abbott et al. 2023a) and requires the shape parameters  $\alpha, \beta > 1$ , which forces  $\pi(\chi_i = 0, 1) = 0$  (D. Wysocki et al. 2019; R. Abbott et al. 2021a). The Unconstrained Beta relaxes this constraint on the the shape parameters. If  $0 < \alpha, \beta < 1$ , the Beta distribution becomes singular, meaning  $\pi(\chi_i = 0, 1) = \infty$ . Following R. Abbott et al. (2023a), we sample the mean and standard deviation of the Beta distribution, rather than  $\alpha$  and  $\beta$ , and use the same priors for  $\mu_\chi$  and  $\sigma_\chi$  as given in Table 8 for the GAUSSIAN COMPONENT SPINS model. For the Constrained Beta case, we additionally impose the cut  $\alpha, \beta > 1$ . The relationship between  $\{\mu_\chi, \sigma_\chi\}$  and  $\{\alpha, \beta\}$  is given in Equation (5) of B. P. Abbott et al. (2019a).

### B.5.2. Identical Versus Nonidentically Distributed Spin Magnitudes and Tilts

In Appendix D.2, we investigate whether or not the primary and secondary spins are identically distributed, assuming the GAUSSIAN COMPONENT SPINS model. *Identical* distribution means that the two distributions share the same set of hyperparameters, while *nonidentical* means that each is described by different hyperparameters. Spin magnitudes are also *independently* distributed, meaning that  $\pi(\chi_1, \chi_2)$  is separable in terms of  $\chi_1$  and  $\chi_2$ . The acronym IID means they are independently and identically distributed, while IND means independently and nonidentically distributed:

$$\begin{aligned} \chi_i \text{ IID} &\Rightarrow \pi(\chi_{1,2} | \mu_\chi, \sigma_\chi) \\ &= \mathcal{N}_{[0,1]}(\chi_1 | \mu_\chi, \sigma_\chi) \\ &\quad \times \mathcal{N}_{[0,1]}(\chi_2 | \mu_\chi, \sigma_\chi), \end{aligned} \quad (\text{B22})$$

$$\begin{aligned} \chi_i \text{ IND} &\Rightarrow \pi(\chi_{1,2} | \mu_{\chi,1}, \sigma_{\chi,1}, \mu_{\chi,2}, \sigma_{\chi,2}) \\ &= \mathcal{N}_{[0,1]}(\chi_1 | \mu_{\chi,1}, \sigma_{\chi,1}) \mathcal{N}_{[0,1]}(\chi_2 | \mu_{\chi,2}, \sigma_{\chi,2}). \end{aligned} \quad (\text{B23})$$

The tilt angles, on the other hand, are *nonindependently* distributed, meaning that  $\pi(\cos \theta_1, \cos \theta_2)$  is not separable. The acronym NID means they are nonindependently but identically distributed, while NND means nonindependently and nonidentically distributed:

$$\begin{aligned} \cos \theta_i \text{ NID} &\Rightarrow \pi(\cos \theta_{1,2} | \zeta, \mu_t, \sigma_t) = \zeta \mathcal{N}_{[-1,1]}(\cos \theta_1 | \mu_t, \sigma_t) \\ &\quad \times \mathcal{N}_{[-1,1]}(\cos \theta_2 | \mu_t, \sigma_t) + \frac{1 - \zeta}{4}, \end{aligned} \quad (\text{B24})$$

$$\begin{aligned} \cos \theta_i \text{ NND} &\Rightarrow \pi(\cos \theta_{1,2} | \zeta, \mu_{t,1}, \sigma_{t,1}, \mu_{t,2}, \sigma_{t,2}) = \zeta \\ &\quad \times \mathcal{N}_{[-1,1]}(\cos \theta_1 | \mu_{t,1}, \sigma_{t,1}) \mathcal{N}_{[-1,1]} \\ &\quad \times (\cos \theta_2 | \mu_{t,2}, \sigma_{t,2}) + \frac{1 - \zeta}{4}. \end{aligned} \quad (\text{B25})$$

For the nonidentically distributed cases, each component's hyperparameters have the same priors as those listed in Table 8 for the identically distributed case. Table 12 gives Bayes factors between different combinations of IID/IND spin magnitudes and NID/NND spin tilts; see the associated discussion in Appendix D.2.

**Table 9**  
Summary of GAUSSIAN EFFECTIVE SPINS (Equation B28) and SKEW-NORMAL EFFECTIVE SPIN (Equation B29) Spin Parameters

| Parameter             | Description                                                    | Prior G            | Prior SN        |
|-----------------------|----------------------------------------------------------------|--------------------|-----------------|
| $\mu_{\text{eff}}$    | Location of the $\chi_{\text{eff}}$ distribution               | U(−1, 1)           | U(−1, 1)        |
| $\sigma_{\text{eff}}$ | Width of the $\chi_{\text{eff}}$ distribution                  | U(0.05, 1)         | LU<br>(0.01, 4) |
| $\mu_p$               | Location of the $\chi_p$ distribution                          | U(0.05, 1)         | U(0.01, 1)      |
| $\sigma_p$            | Width of the $\chi_p$ distribution                             | U(0.07, 1)         | LU<br>(0.01, 1) |
| $\rho$                | Degree of correlation between $\chi_{\text{eff}}$ and $\chi_p$ | U<br>(−0.75, 0.75) | N/A             |
| $\epsilon$            | Skew of the $\chi_{\text{eff}}$ distribution                   | N/A                | U(−1, 1)        |

**Note.** The first column of priors (**G**) gives those used for the GAUSSIAN EFFECTIVE SPINS results and the second column (**SN**) is SKEW-NORMAL EFFECTIVE SPIN. U stands for a uniform prior; LU for log-uniform.

### B.5.3. Effective Spin Models

GAUSSIAN EFFECTIVE SPINS: we here assume that the distribution of  $\chi_{\text{eff}}$  and  $\chi_p$  across the BBH population is a bivariate truncated Gaussian (S. Miller et al. 2020; J. Roulet & M. Zaldarriaga 2019) characterized by the location and width of the  $\chi_{\text{eff}}$  and  $\chi_p$  distributions and the covariance between them:

$$\pi(\chi_{\text{eff}}, \chi_p | \boldsymbol{\mu}, \boldsymbol{\Sigma}) \propto \mathcal{N}(\chi_{\text{eff}}, \chi_p | \boldsymbol{\mu}, \boldsymbol{\Sigma}), \quad (\text{B26})$$

where  $\boldsymbol{\mu} = (\mu_{\text{eff}}, \mu_p)$  and

$$\boldsymbol{\Sigma} = \begin{pmatrix} \sigma_{\text{eff}}^2 & \rho \sigma_{\text{eff}} \sigma_p \\ \rho \sigma_{\text{eff}} \sigma_p & \sigma_p^2 \end{pmatrix}. \quad (\text{B27})$$

This expands to:

$$\begin{aligned} \pi(\chi_{\text{eff}}, \chi_p | \boldsymbol{\mu}, \boldsymbol{\Sigma}) \propto \exp \left[ -\frac{1}{2(1 - \rho^2)} \left( \frac{(\chi_{\text{eff}} - \mu_{\text{eff}})^2}{\sigma_{\text{eff}}^2} \right. \right. \\ \left. \left. - \frac{2\rho(\chi_{\text{eff}} - \mu_{\text{eff}})(\chi_p - \mu_p)}{\sigma_{\text{eff}} \sigma_p} + \frac{(\chi_p - \mu_p)^2}{\sigma_p^2} \right) \right]. \end{aligned} \quad (\text{B28})$$

The bivariate Gaussian is truncated over the range  $\chi_{\text{eff}} \in [-1, 1]$ ,  $\chi_p \in [0, 1]$  and is normalized numerically. Priors on the hyperparameters are given in Table 9.

SKEW-NORMAL EFFECTIVE SPIN: to account for observational evidence that the  $\chi_{\text{eff}}$  distribution is not symmetric (T. A. Callister et al. 2021b; C. Adamcewicz & E. Thrane 2022; S. Banagiri et al. 2025), we additionally model  $\chi_{\text{eff}}$  as a skewed, truncated Gaussian distribution:

$$\begin{aligned} \pi(\chi_{\text{eff}} | \mu_{\text{eff}}, \sigma_{\text{eff}}, \epsilon) \\ \propto \begin{cases} (1 + \epsilon) \mathcal{N}_{[-1,1]}(\chi_{\text{eff}} | \mu_{\text{eff}}, \sigma_{\text{eff}}(1 + \epsilon)) & \chi_{\text{eff}} \leq \mu_{\text{eff}}, \\ (1 - \epsilon) \mathcal{N}_{[-1,1]}(\chi_{\text{eff}} | \mu_{\text{eff}}, \sigma_{\text{eff}}(1 - \epsilon)) & \chi_{\text{eff}} \geq \mu_{\text{eff}}. \end{cases} \end{aligned} \quad (\text{B29})$$

This model includes a parameter  $\epsilon$  that describes the skew of the distribution, such that  $\epsilon > 0$  characterizes a distribution with more support for  $\chi_{\text{eff}} < \mu_{\text{eff}}$ , while  $\epsilon < 0$  has more support when  $\chi_{\text{eff}} > \mu_{\text{eff}}$ . The SKEW-NORMAL EFFECTIVE SPIN distribution reduces to a standard, symmetric Gaussian in the case that  $\epsilon = 0$ . We here model  $\chi_p$  as a truncated normal distribution and infer its location and width. Priors on the hyperparameters are given in Table 9.

### B.6. Copula Correlation Models

Copulas allow for a variable correlation between two parameters  $x$  and  $y$ , while keeping the marginal distributions for the respective parameters fixed. This is done using the fact that the cumulative distribution function (CDF) of any randomly distributed variable is itself a uniformly distributed variable between 0 and 1, in order to model the CDFs of  $x$  and  $y$  with a correlated two-dimensional uniform distribution. This correlated two-dimensional uniform distribution, known as a copula density function, is dependent on a (hyper)parameter  $\kappa_{x,y}$ , which determines the level (or strength) of the correlation. A coordinate transformation (which is determined by the chosen marginal distributions for  $x$  and  $y$ ) can then be applied to provide a correlated two-dimensional model in the desired coordinates. Conveniently, the Jacobian for this transformation turns out to be the product of the chosen marginal distributions, meaning the two-dimensional population model can be written as

$$\pi_{xy}(x, y|\mathbf{A}, \kappa_{x,y}) = \pi_c(u(x|\mathbf{A}), v(y|\mathbf{A})|\kappa_{x,y}) \times \pi_x(x|\mathbf{A})\pi_y(y|\mathbf{A}). \quad (\text{B30})$$

Here,  $\mathbf{A}$  are the set of hyperparameters governing the marginal distributions  $\pi_x$  and  $\pi_y$ , while  $\pi_c$  denotes the chosen copula density function. Finally,

$$u(x|\mathbf{A}) = \int_{x_{\min}}^x dx' \pi_x(x'|\mathbf{A}), \quad (\text{B31})$$

and

$$v(y|\mathbf{A}) = \int_{y_{\min}}^y dy' \pi_y(y'|\mathbf{A}), \quad (\text{B32})$$

which we refer to as  $u$  and  $v$  for the sake of brevity, are the CDFs of  $x$  and  $y$ , respectively.

The COPULA models all assume the same marginal distributions and copula density functions, but differ in which pairs of parameters they correlate (i.e., which parameters  $u$  and  $v$  are functions of in the above notation). Namely, the mass distribution is assumed to follow the default BROKEN POWER LAW + 2 PEAKS model, redshift follows the default power-law redshift model, and  $\chi_{\text{eff}}$  and  $\chi_p$  are Gaussian distributed, but uncorrelated (i.e., they follow the GAUSSIAN EFFECTIVE SPINS model with  $\rho = 0$ ). We assume a Frank copula density function

$$\pi_c(u, v|\kappa_{x,y}) = \frac{-\kappa_{x,y} e^{-\kappa_{x,y}(u+v)} (e^{-\kappa_{x,y}} - 1)}{(e^{-\kappa_{x,y}} - e^{-\kappa_{x,y}u} - e^{-\kappa_{x,y}v} + e^{-\kappa_{x,y}(u+v)})^2}, \quad (\text{B33})$$

where  $\kappa_{x,y} \in (-\infty, \infty)$ . Positive values of  $\kappa_{x,y}$  imply a correlation, while negative values of  $\kappa_{x,y}$  imply an anticorrelation. The Frank copula density function is not defined at  $\kappa_{x,y} = 0$ , but becomes uncorrelated as  $\kappa_{x,y} \rightarrow 0$  from above and below, so we assume  $\pi_c(u, v|\kappa_{x,y} = 0) = 1$  (technically, making this a piece-wise function). The Frank copula density function is chosen as it allows for positive and negative correlations that are symmetric about  $\kappa_{x,y} = 0$ , and gives rise to correlated distributions that we believe appear physically reasonable (C. Adamcewicz & E. Thrane 2022; C. Adamcewicz et al. 2023). The prior on  $\kappa_{x,y}$  (which is the same for all copula model variations), is given in Table 10.

**Table 10**

Summary of Parameters Exclusive to the COPULA, LINEAR, and SPLINE Correlated Models, Along with Their Priors

| Parameter                          | Description                                                                | Prior        |
|------------------------------------|----------------------------------------------------------------------------|--------------|
| $\kappa_{x,y}$                     | Level of correlation between parameters $x$ and $y$ inferred with a copula | $U(-20, 20)$ |
| $\mu_{\text{eff} q}$               | $q = 1$ intercept in linear $\mu_{\text{eff}}(q)$                          | $U(-1, 1)$   |
| $\delta\mu_{\text{eff} q}$         | Gradient in linear $\mu_{\text{eff}}(q)$                                   | $U(-2, 2)$   |
| $\ln \sigma_{\text{eff} q}$        | $q = 1$ intercept in linear $\ln \sigma_{\text{eff}}(z)$                   | $U(-5, 0)$   |
| $\delta \ln \sigma_{\text{eff} q}$ | Gradient in linear $\ln \sigma_{\text{eff}}(q)$                            | $U(-12, 4)$  |
| $\mu_{\text{eff} z}$               | $z = 0$ intercept in linear $\mu_{\text{eff}}(z)$                          | $U(-1, 1)$   |
| $\delta\mu_{\text{eff} z}$         | Gradient in linear $\mu_{\text{eff}}(z)$                                   | $U(-1, 1)$   |
| $\ln \sigma_{\text{eff} z}$        | $z = 0$ intercept in linear $\ln \sigma_{\text{eff}}(z)$                   | $U(-5, 0)$   |
| $\delta \ln \sigma_{\text{eff} z}$ | Gradient in linear $\ln \sigma_{\text{eff}}(z)$                            | $U(-3, 5)$   |
| $\mu_{\text{eff} q}^i$             | $i^{\text{th}}$ node in spline $\mu_{\text{eff}}(q)$                       | $U(-1, 1)$   |
| $\ln \sigma_{\text{eff} q}^i$      | $i^{\text{th}}$ node in spline $\ln \sigma_{\text{eff}}(q)$                | $U(-5, 0)$   |
| $\mu_{\text{eff} z}^i$             | $i^{\text{th}}$ node in spline $\mu_{\text{eff}}(z)$                       | $U(-1, 1)$   |
| $\ln \sigma_{\text{eff} z}^i$      | $i^{\text{th}}$ node in spline $\ln \sigma_{\text{eff}}(z)$                | $U(-5, 0)$   |

**Note.** There are four variations of the COPULA model in which  $(x, y) = (q, \chi_{\text{eff}}), (m_1, \chi_{\text{eff}}), (z, \chi_{\text{eff}})$ , and finally,  $(m_1, z)$ . Within the spline models, we use four nodes  $i$ .

Copulas are advantageous as they allow for a potential correlation to be quantified by a single variable  $\kappa_{x,y}$ , that otherwise has no influence on the distribution of the population. However, relative to the linear and spline models explored below, they suffer from a lack of flexibility when it comes to covariance. There are a limited number of copula density functions available, all of which introduce a correlation in a unique, but rigid way (e.g. C. Adamcewicz & E. Thrane 2022; C. Adamcewicz et al. 2023). Furthermore, known two-dimensional copulas depend on a single parameter  $\kappa_{x,y}$ , and cannot infer, for example, a separable broadening and correlation with the mean of a distribution simultaneously. As a result, using copulas to probe for more complex structure in two dimensions (assuming fixed marginal distributions), requires model comparison between a number of different copula density functions (e.g., C. Adamcewicz et al. 2023).

### B.7. Linear Correlation Models

The  $(q, \chi_{\text{eff}})$  and  $(z, \chi_{\text{eff}})$  LINEAR models begin by assuming that  $\chi_{\text{eff}}$  is Gaussian distributed for any given value of mass ratio  $q$  and redshift  $z$ , respectively. As the two models are otherwise identical, for the remainder of this section, we substitute  $x$  for  $q$  and  $z$ . This parameter-dependent Gaussian distribution for  $\chi_{\text{eff}}$ ,  $\pi(\chi_{\text{eff}}|x)$ , is truncated at unphysical values of  $|\chi_{\text{eff}}| \geq 1$ . From here, the mean and (natural log) width of the  $\chi_{\text{eff}}$  distribution are allowed to evolve with the chosen variable  $x$  linearly:

$$\mu_{\text{eff}}(x) = \mu_{\text{eff}|x} + \delta\mu_{\text{eff}|x}x, \quad (\text{B34})$$

and

$$\ln \sigma_{\text{eff}}(x) = \ln \sigma_{\text{eff}|x} + \delta \ln \sigma_{\text{eff}|x_0}x. \quad (\text{B35})$$

Here,  $\mu_{\text{eff}|x}$ ,  $\delta\mu_{\text{eff}|x}$ ,  $\ln \sigma_{\text{eff}|x}$ , and  $\delta \ln \sigma_{\text{eff}|x_0}$  are all hyperparameters fit to the data, where  $\delta\mu_{\text{eff}|x}$  and  $\delta \ln \sigma_{\text{eff}|x_0}$  quantify the strength of the correlation between  $x$  and the mean and width

of the  $\chi_{\text{eff}}$  distribution, respectively. The priors for these parameters are given in Table 10. Meanwhile, masses follow the default BROKEN POWER LAW + 2 PEAKS model and redshift is distributed according to the default power-law redshift model.

These models (in the style of those presented in M. Safarzadeh et al. 2020; T. A. Callister et al. 2021b; S. Biscoveanu et al. 2022a), therefore allow us to infer separable trends in the mean and width of the  $\chi_{\text{eff}}$  distribution with another parameter. The inferred correlations should be interpreted with care as, unlike the copula models defined in Section B.6, the correlation hyperparameters here will also affect the shape of the marginal  $\chi_{\text{eff}}$  distribution. As such, it can be difficult to be certain whether an inferred correlation is entirely due to a trend between  $\chi_{\text{eff}}$  and another parameter, or is in part due to a better fit to the marginal  $\chi_{\text{eff}}$  distribution (C. Adamcewicz & E. Thrane 2022).

### B.8. Spline Correlation Models

The SPLINE models (J. Heinzel et al. 2024) are similar to the LINEAR models defined in Section B.7. The key difference is that the SPLINE models more flexibly model the parameter-dependent mean  $\mu_{\text{eff}}(x)$  and (natural log) width  $\ln \sigma_{\text{eff}}(x)$  of the  $\chi_{\text{eff}}$  distribution as cubic splines dependent on  $x$ . Each spline has four nodes  $\mu_{\text{eff}}^i$  and  $\ln \sigma_{\text{eff}}^i$  that are placed uniformly in  $\log_{10} x$ , and are inferred from the data. The priors for these nodes are given in Table 10.

## Appendix C

### Summary of Models Used in the Weakly Modeled Approach

We describe weakly modeled approaches—B-SPLINE, BGP, AR, FM—used in this work. Results in the main text make use of B-SPLINE and BGP models. BGP was chosen since it was the only model capable of modeling the full mass spectrum, while B-SPLINE was chosen for most BBH analyses for its ease of description and flexibility, as it simultaneously models all parameters with B-Splines. See Appendix D.4 for comparison of these weakly modeled approaches.

#### C.1. B-SPLINE Models

**B-SPLINE:** The B-SPLINE model (B. Edelman et al. 2023) simultaneously fits all population parameters with Basis-splines (B-splines). A  $k^{\text{th}}$  order B-spline of variable  $x$  consists of a linear combination of  $n$  basis functions  $\{B_{k,n}(x)\}$ , each of which are degree  $k - 1$  piecewise polynomials joined at a set of  $m$  locations called knots  $\{x_m\}$ . The number of basis functions  $n$  defined across any range of  $x$  values is determined solely by the order of the spline  $k$  and the total number of knots  $m$  as  $n = k + m$ . This forms a basis that spans the space of possible interpolants between the knots  $\{x_m\}$ . Given a vector of coefficients  $\alpha$ , any function  $f$  can then be approximated as

$$\tilde{f}(x) = \sum_{i=1}^n B_{k,i}(x) \alpha_i. \quad (\text{C1})$$

In the case of this work,  $f$  is a probability distribution  $p(\theta|\alpha_\theta)$  for a population-level parameter  $\theta$ , where the B-spline coefficients  $\alpha_\theta$  are the hyperparameters of the distribution that are inferred during parameter estimation.

Given an adequate number of knots, a B-spline is highly flexible and therefore capable of identifying sharp features that

could be present in the data. This does, however, naturally make the B-SPLINE model prone to overfitting. To combat this, we include a smoothing prior  $\pi_{\text{BS}}$  that penalizes large differences between neighboring coefficients. The prior is defined as

$$p(\alpha|\tau) = \exp\left(-\frac{1}{2}\tau\alpha^T\mathbf{D}_r^T\mathbf{D}_r\alpha\right), \quad (\text{C2})$$

where  $D_r$  is the  $r$ -order difference matrix with shape  $(n - r) \times n$  and  $\tau$  is a scalar that controls the level of smoothing. Ideally,  $\tau$  is also inferred during parameter estimation. We found that  $\tau$  consistently railed against prior boundaries, which meant that the limits imposed on the likelihood uncertainty was the main driver of smoothness. We therefore fix  $\tau$  to a reasonable value (roughly between 5 – 10) for each population distribution. With a sufficient number of bases, typically  $n \sim 30 - 40$ , this penalty prior will prevent the B-spline from overfitting the data while the large number of bases will provide enough flexibility to fit sharp features.

The mass and spin distributions are modeled as B-splines, and the redshift distribution is modeled as a power law modulated by a B-spline (B. Edelman et al. 2023), with all components inferred simultaneously. One of the weakly modeled approaches used in previous analyses (R. Abbott et al. 2023a) was the POWERLAW + SPLINE model. This model assumed that the primary BBH mass followed a power-law distribution with moderate deviations controlled by a cubic spline. The B-SPLINE model does not assume an underlying shape for the primary mass distribution, instead allowing for full model flexibility.

The B-SPLINE model infers the separable components of the mass distributions,  $p(m_1)$  and  $p(q)$ , wherein the primary mass is defined over the range  $3 - 300 M_\odot$  and the mass ratio is defined over the range  $0.03 - 1$ . Unlike the BROKEN POWER LAW + 2 PEAKS model, a minimum secondary mass is not enforced during parameter estimation. To provide a more direct comparison to the strongly modeled approach, the B-SPLINE mass distributions shown in Section 6.1 are not the separable components  $p(m_1)$  or  $p(q)$  but instead the marginal distributions conditioned on  $m_2 > 3 M_\odot$ , that is,  $p(q|m_2 > 3 M_\odot) = \int p(q)p(m_1)\Theta(m_1q - 3)dm_1$ . We include the separable distributions along with the conditional marginal distributions in the mass ratio plot in Figure 20 to illustrate how this assumption affects the shape of the mass ratio distribution.

**ISOLATED PEAK:** this model is defined by two subpopulations (J. Godfrey et al. 2023). One assumes a primary mass distribution described by a log-Gaussian peak while the other infers the mass distribution with a B-spline. Mass ratio, spin magnitude, and spin tilt distributions are inferred separately for each subpopulation, also using B-splines. The redshift distribution is the same for each subpopulation and is inferred with a power law modulated by a B-spline.

#### C.2. Binned Gaussian Process (BGP) Model

In previous population analyses (R. Abbott et al. 2023a), we used the BGP model to study the joint distribution of primary and secondary masses. Here, we extend it to model the joint distributions of mass, spin, and redshift. The BGP approach models the rate of BBH, BNS, and NSBH mergers as a piecewise constant function over a set of fixed bins across the

one-, two-, or three-dimensional joint space. The comoving merger rate density in each bin is a hyperparameter of the model. In addition, the BGP model couples the logarithm of the rate density in each bin with a Gaussian process covariance, assuming an exponential quadratic kernel (also known as a radial basis function kernel). The exponential quadratic kernel has a hyper-hyperparameter length scale  $\lambda$  for each parameter in the joint space.

The covariance between two bins is proportional to the exponential of the negative squared distance between the bin centers, in units of the length scales along each parameter. In addition, there is one more hyper-hyperparameter  $\sigma$ , which acts as an overall multiplicative scaling of the covariance matrix (A. Ray et al. 2023a). The BGP approach directly infers the rate density in each bin, as well as the hyper-hyperparameters of the covariance kernel. The prior on the parameter  $\sigma$  is a half-normal with width 1, and the length scale priors were tuned to the mean and variation in the set of distances between the bin centers.

We used 22 bins spaced uniformly in log-mass for the mass BGP models, and 15 bins spaced uniformly between  $\chi_{\text{eff}} \in [-0.7, 0.7]$  for the effective spin BGP models.

The BGP approach has the advantage of being able to model nontrivial correlations in the population of compact binaries. However, it assumes an arbitrary binning scheme, which reduces the resolution of the constraints and leads to unphysical discontinuities at the boundary between bins. Furthermore, measurements of the rate density in some bins may be driven by the a priori assumption of a Gaussian covariance, and not the data. This can also cause smoothing near sharp features, e.g., near the  $m_1 = m_2$  boundary.

### C.3. Autoregressive Process (AR) Model

The AR model (T. A. Callister & W. M. Farr 2024) is a highly flexible model for one-dimensional marginal merger rate densities. The Monte Carlo integrals for estimating the likelihood in Equation (2) involve a large set of parameter estimation samples (Equation (A1)) and found injections for the selection efficiency (Equation (A2)). The merger rate density at each sample is its own hyperparameter, which is directly inferred from the data. Without any further assumptions, such a model is severely underconstrained and will converge on the maximum likelihood functional distribution (E. Payne & E. Thrane 2023). In order to a priori favor smoother distributions, this finite list of samples is ordered along the dimension of interest like, for example, their primary mass. The marginal merger rate density is then assumed to be an autoregressive Gaussian random walk in log-space. There are two hyper-hyperparameters,  $\sigma_{\text{AR}}$  and  $\tau_{\text{AR}}$ , that control the scale of variability and the autocorrelation length along the Gaussian random walk, respectively. These hyper-hyperparameters have half-normal and log-normal priors, respectively, tuned to the scale of the data: see Appendix B in T. A. Callister & W. M. Farr (2024) for details. These hyper-hyperparameters are jointly inferred along with the logarithmic merger rate density at each sample.

The AR model is particularly well-suited to distributions with sharp features and nontrivial evolution, complementing the BGP approach. However, the AR model used here cannot model correlations in the population. Furthermore, as in the BGP approach, the inferred merger rate may extrapolate based off nearby constraints in regions of little information. When

evaluating uncertainties in the AR model, one should consider the impact of the AR smoothing prior. In particular, lower bounds on the merger rate in some regions may not be an accurate lower bound on the true distribution.

Like the B-SPLINE model, the AR model does not enforce a minimum secondary mass through a mass-dependent mass ratio.

### C.4. Flexible Mixtures (FM) Model

The FM model (V. Tiwari 2021) is a flexible mixture model framework for modeling the BBH population. FM models the population as a Gaussian mixture model in chirp mass and aligned spins, and a power law in mass ratio and redshift (V. Tiwari 2022). Furthermore, FM is able to model correlations between parameters in the population, and additionally has a variable model dimension, sampling the transdimensional posterior using a reversible-jump MCMC method. For the analyses presented here, FM uses 11 mixture components.

## Appendix D Result Validation Studies

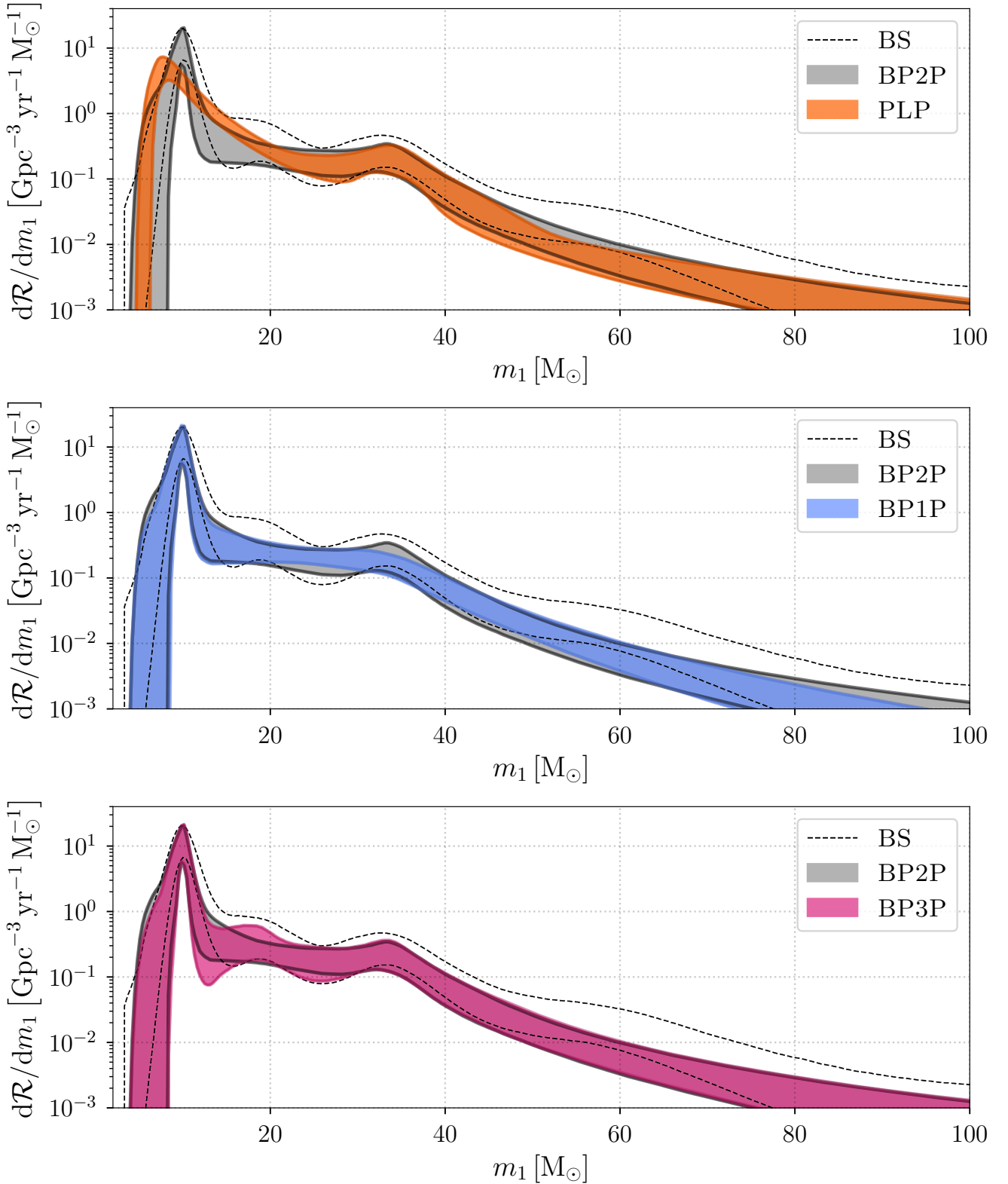
In the following subappendices, we describe various methods used to select and validate the data, models, and approaches presented in the main text. In Appendix D.1 and Appendix D.2 we discuss the process for selecting the fiducial mass and spin models, respectively, under the strongly modeled approach and present results from other models that were under consideration. Appendix D.3 describes how the specific convergence cut biases the inferred effective spin distribution. In Appendix D.4, we compare various types of methods for the weakly modeled approach, which were presented in Appendix C. Appendix D.5 gives compact object merger rates when subthreshold triggers are considered, i.e., using a lower FAR threshold. Finally, Appendix D.6 provides supplementary results for population-level correlations between masses, spins, and redshifts.

### D.1. Model Comparison Study: Mass

The fiducial mass model is a strongly modeled approach that is intended to provide a minimal but accurate description of the data with a parameterization that is more readily interpretable than the weakly modeled approaches. Table 11 shows the Bayes factors between models with a different number of features and our fiducial model BROKEN POWER LAW + 2 PEAKS. We also compare to our previous fiducial model from R. Abbott et al. (2023a), the POWER LAW + PEAK model. In Figure 15, we see that POWER LAW + PEAK infers the peak component at  $35M_{\odot}$ , as in R. Abbott et al. (2023a), but a broken power law plus 1 peak (BP1P) model infers the peak component at  $10M_{\odot}$  and the power law break at  $35M_{\odot}$ .

**Table 11**  
Bayes Factor Comparison of Selected Models from the Mass Model Comparison Study

| Model                       | Abbreviation | $\log_{10} \mathcal{B}$ |
|-----------------------------|--------------|-------------------------|
| BROKEN POWER LAW + 2 PEAKS* | BP2P         | 0                       |
| BROKEN POWER LAW + 1 PEAK   | BP1P         | 0.14                    |
| BROKEN POWER LAW + 3 PEAKS  | BP3P         | -0.20                   |
| POWER LAW + PEAK            | PP           | -2.20                   |

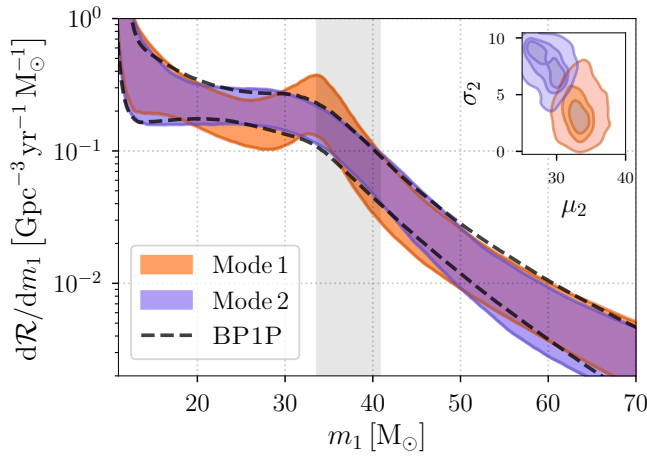


**Figure 15.** Inferred mass distributions of various strongly modeled approaches compared to the fiducial mass model BROKEN POWER LAW + 2 PEAKS (gray shaded) and the B-SPLINE model (black dashed). The fiducial model from GWTC-3.0, POWER LAW + PEAK, is shown in orange, a broken power law with a single peak in blue, and a broken power law with three peaks in pink.

In Table 11, we see that all models that include a broken power law are strongly favored over the POWER LAW + PEAK model.

However, among models with a broken power law, the Bayes factors do not show strong support for one model over another. Bayes factors are a useful model comparison metric

when they are decisive (e.g., requiring a broken power law); however, minor preferences should not be taken too seriously:  $\log_{10}$  Bayes factors less than  $\sim 0.5$  should be considered ambiguous (H. Jeffreys 1939). In addition, for the set of hierarchical models we consider here, the priors are neither



**Figure 16.** Differential merger rate as a function of primary mass (evaluated at  $z = 0.2$ ) of the two different modes recovered by the BROKEN POWER LAW + 2 PEAKS model. The orange shaded region shows the 90% credible interval for the dominant mode (65% of posterior), reflecting a distinct peak at  $35 M_{\odot}$ , and the purple shaded region shows the 90% credible interval for the subdominant mode (35% of posterior), reflecting a broken power-law morphology without a distinct  $35 M_{\odot}$  peak. The black dashed lines show the 90% credible bounds of the BROKEN POWER LAW + 1 PEAK model for comparison. The inset figure shows the joint posterior of the peak mean  $\mu_2$  and width  $\sigma_2$  for each mode. The vertical gray shaded region indicates the 90% credible interval of the sum  $\mu_2 + \sigma_2$ , which is consistent between both modes.

physically motivated nor can they be made consistent between models. Bayes factors are prior-dependent, which means the value of the Bayes factor itself is subjective. Additionally, since they are calculated using nested sampling, there is a Monte Carlo error of  $\approx 0.1$  on the  $\log_{10}$  Bayes factors. Therefore, among the models not decisively ruled out by Bayes factors, we select the most interpretable extension of the POWER LAW + PEAK model that probes features shared among all of the weakly modeled approaches shown in Figure 20. The BROKEN POWER LAW + 2 PEAKS model best fit these criteria.

In GWTC-3.0, the POWER LAW + PEAK model identified an overdensity in the merger rate at  $m_1 = 35^{+1.7}_{-2.9} M_{\odot}$  relative to a global power law. Evidence for this feature first appeared in B. P. Abbott et al. (2019a) and was strengthened in R. Abbott et al. (2021a) and R. Abbott et al. (2023a). As mentioned in Section 6.1, this feature at  $35 M_{\odot}$  may be an overdensity relative to an underlying mass continuum or could mark the onset of a decline in the merger rate. In addition to the Bayes factor comparison shown in Table 11, this ambiguity is also present in the BROKEN POWER LAW + 2 PEAKS posterior, which includes two posterior modes (identified with a k-means clustering algorithm) that correspond to two different morphologies, shown in Figure 16. The dominant mode is correlated with a narrower ( $\sigma_2 = 3.3^{+3.0}_{-2.2} M_{\odot}$ ) peak at  $\mu_2 = 33^{+3.0}_{-2.3} M_{\odot}$  and accounts for 65% of the posterior volume, while the subdominant mode is correlated with a wider ( $\sigma_2 = 7.7^{+2.1}_{-2.7} M_{\odot}$ ) peak at  $\mu_2 = 29^{+2.8}_{-3.2} M_{\odot}$  and accounts for 35% of the posterior volume. This latter mode has a morphology nearly identical to the inferred BP1P distribution (see Figure 16). The inflection point of the Gaussian,  $\mu_2 + \sigma_2 = 36^{+4.0}_{-3.1} M_{\odot}$ , is consistent between both modes, which indicates that the right half of the Gaussian must fall below the power law to match the declining rate in this region (the gray vertical shaded region in Figure 16).

The power-law indices,  $\alpha_1$  and  $\alpha_2$ , are not correlated with the two modes present in the BP2P posterior, though the

measured slope of the mass distribution between  $18 - 19 M_{\odot}$  is not equivalent to  $\alpha_1$  in the subdominant mode. In this mode, the slope (calculated by finite difference) is  $0.84^{+1.4}_{-1.7}$ , which includes more support for negative values compared to the inferred power-law index,  $\alpha_1 = 1.9^{+1.4}_{-1.9}$ . We infer the power-law break location at  $m_{\text{break}} = 35^{+13}_{-13} M_{\odot}$ . The BP1P model, which does not include a second Gaussian component, measures the break location much more precisely at  $m_{\text{break}} = 34.1^{+3.7}_{-3.4} M_{\odot}$ . The uncertainty in the BP2P power-law break is due to the presence of the second Gaussian component, which likely obscures the break most of the time. Because the peak is narrower in the dominant BP2P mode, one might expect the break location to be better constrained in this mode; however, this is not the case. The break location does not appear to be correlated with either mode.

EXTENDED BROKEN POWER LAW + 2 PEAKS also possesses the two modes seen in BROKEN POWER LAW + 2 PEAKS, but with some key differences. Like BROKEN POWER LAW + 2 PEAKS, the two modes are distinguished by the inferred location of the second Gaussian component. The dominant mode in EXTENDED BROKEN POWER LAW + 2 PEAKS places the second Gaussian component at  $\sim 35 M_{\odot}$ . Unlike BROKEN POWER LAW + 2 PEAKS, this mode accounts for 91.6% of the posterior. Additionally, the correlation between primary mass and mass ratio allowed by EXTENDED BROKEN POWER LAW + 2 PEAKS breaks the degeneracy in the inferred power-law break location seen in the two modes of BROKEN POWER LAW + 2 PEAKS. The power-law break location is uninformed in the dominant mode (because it is obscured by the second Gaussian component), but is measured near  $\sim 35 M_{\odot}$  in the subdominant mode. The mass ratio power-law index of the second Gaussian component in the dominant mode is  $\beta_q^{\text{peak2}} = 6.7^{+5.3}_{-4.7}$ , which is what we report in the main text (Section 6.1). In contrast, the subdominant mode measures  $\beta_q^{\text{peak2}}$  as being strictly negative, and as in BROKEN POWER LAW + 2 PEAKS, prefers the location of the second Gaussian component to be less than  $30 M_{\odot}$ . The mass ratio power-law index of the continuum mass component,  $\beta_q^{\text{BP}}$  is strictly positive in this mode. Given these findings, the second Gaussian mass component in the dominant mode and the continuum mass component in the subdominant mode of EXTENDED BROKEN POWER LAW + 2 PEAKS appear to be describing the same feature, which is that  $\sim 35 M_{\odot}$  BHs are more likely to pair with other BHs of equal mass relative to the rest of the continuum. This result is most clearly described by the dominant mode, which is why (in addition to it accounting for 91.6% of the posterior) we quote the dominant mode results in the main text.

## D.2. Model Comparison Study: Spin Magnitudes and Tilt Angles

We consider two additional spin magnitude models beyond the GAUSSIAN COMPONENT SPINS model from Section 6.3.1: the Constrained Beta and Unconstrained Beta models, both defined by Equation (B21). We also consider one additional spin tilt model, the Isotropic + Aligned Gaussian, which fixes  $\mu_t = 1$  in the GAUSSIAN COMPONENT SPINS model and served as the DEFAULT in GWTC-3.0 (C. Talbot & E. Thrane 2017; R. Abbott et al. 2023a). The first five rows of Table 12 give the log Bayes factors between these models. Within the GAUSSIAN COMPONENT SPINS model, we also test whether the primary and secondary spins are identically and independently

**Table 12**  
Comparison of Different Parametric Models for Spin Magnitudes  $\chi_i$  and Tilt Angles  $\cos \theta_i$

| $\chi_i$ Model       |     | $\cos \theta_i$ Model          |     | $\log_{10} \mathcal{B}$ |
|----------------------|-----|--------------------------------|-----|-------------------------|
| Truncated Gaussian * | IID | Isotropic + Truncated Gaussian | NID | 0.0                     |
| Constrained Beta     | IID | Isotropic + Aligned Gaussian   | NID | -0.66                   |
| Constrained Beta     | IID | Isotropic + Truncated Gaussian | NID | -0.64                   |
| Unconstrained Beta   | IID | Isotropic + Truncated Gaussian | NID | -0.98                   |
| Truncated Gaussian   | IID | Isotropic + Aligned Gaussian   | NID | -0.08                   |
| Truncated Gaussian   | IND | Isotropic + Truncated Gaussian | NID | -1.09                   |
| Truncated Gaussian   | IID | Isotropic + Truncated Gaussian | NND | -0.17                   |
| Truncated Gaussian   | IND | Isotropic + Truncated Gaussian | NND | -0.91                   |

**Note.** The first row is the Default model for GWTC-4.0 (GAUSSIAN COMPONENT SPINS), while the second is the Default that was used for GWTC-3.0 and earlier (B. P. Abbott et al. 2019a; R. Abbott et al. 2021a, 2023a; C. Talbot & E. Thrane 2017). The third through final are other models explored. All log Bayes factors ( $\log_{10} \mathcal{B}$ ) are with respect to the first row.

distributed (see Appendix B.5.2), with log Bayes factors given in the bottom three rows of Table 12. The GAUSSIAN COMPONENT SPINS model with IID spin magnitudes and NID spin tilts performs the best, and is adopted as the default component spin model in the main text.

Figure 17 shows posteriors for the magnitude and tilt hyperparameters assuming that  $\chi_i$  and  $\cos \theta_i$  are both identically distributed (gray) versus both nonidentically distributed (blue and red). The primary and secondary spins have consistent hyperparameter distributions. Assuming identical distribution makes the hyperparameters more-precisely constrained—yielding tighter 90% bands on the resultant population distributions—but does not affect the overall shape of the distributions. The only difference of note is that  $\chi_2$  has less support for a small  $\mu_\chi$  than  $\chi_1$ , potentially hinting at more highly spinning secondary BHs on a population level.

### D.3. Dependence of the Effective Spin Distribution on the Likelihood Variance Cut

We next investigate the effect of the likelihood variance threshold (see Appendix A.1) on our strongly modeled effective spin results. To ensure that posteriors generated using Monte Carlo estimation are trustworthy, i.e., the likelihood estimate is converged, we enforce that all hyperparameter samples yield a log-likelihood variance  $\sigma_{\ln}^2 < 1$  for all analyses presented in the main text (C. Talbot & J. Golomb 2023). In GWTC-3.0, however, a different quantity was used to assess the Monte Carlo uncertainty: the effective number of independent samples,  $N_{\text{eff}}$  (W. M. Farr 2019). It was there imposed that  $N_{\text{eff}}$  be greater than  $4N_{\text{events}}$  for the sensitivity injections used in Equation (3) and greater than 10 for every event in the catalog of CBCs. This  $N_{\text{eff}}$  cut is generally less stringent than the approach taken for GWTC-4.0. The  $\chi_p$  distribution is sensitive to which method is used to cut out samples.

For the most direct comparison to GWTC-3.0, we here use the GAUSSIAN EFFECTIVE SPINS model. Figure 18 shows the posteriors for the GAUSSIAN EFFECTIVE SPINS parameters where the  $\sigma_{\ln}^2$  (purple) versus  $N_{\text{eff}}$  (green) cuts are done on the GWTC-4.0 results. The LVK GWTC-3.0 results (with the  $N_{\text{eff}}$  cut) are shown in comparison (black). Figure 19 shows the resultant marginal and joint  $\chi_{\text{eff}}-\chi_p$  population distributions. There are three main differences between the results with the two cuts on GWTC-4.0 data:

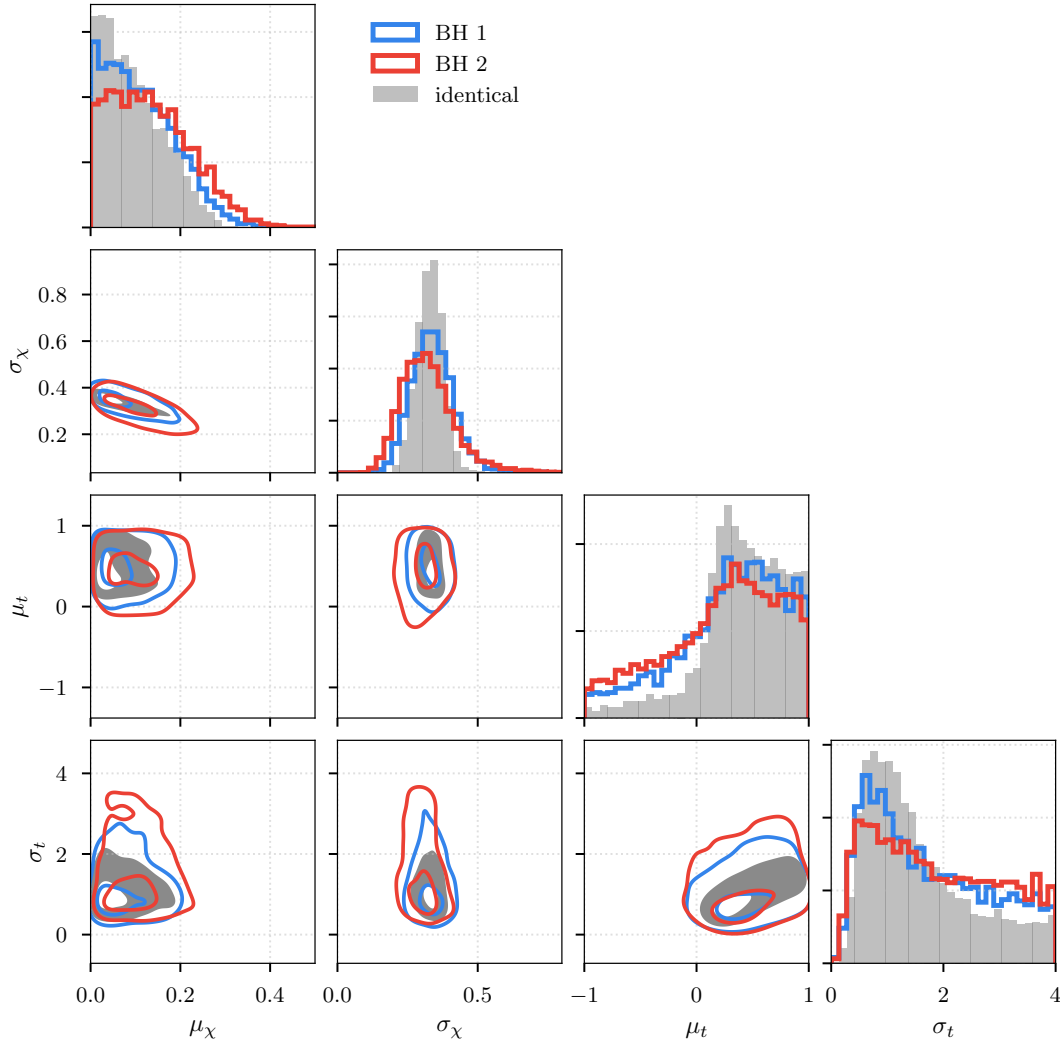
1. The  $\sigma_{\ln}^2$  cut yields a  $\mu_p$  posterior, which is constrained away from zero, while the the  $N_{\text{eff}}$  cut does not.
2. The  $N_{\text{eff}}$  cut allows for wider  $\chi_p$  distributions (larger  $\sigma_p$ ) than the  $\sigma_{\ln}^2$  cut.
3. Under the  $N_{\text{eff}}$  cut,  $\chi_{\text{eff}}$  and  $\chi_p$  are preferentially positively correlated, while under the  $\sigma_{\ln}^2$  cut we remain agnostic, with preference for small-to-zero correlation.

Thus, the claims that the  $\chi_p$  distribution does not peak at zero and that the data prefer  $\chi_{\text{eff}}$  and  $\chi_p$  being uncorrelated at the population level, are not necessarily astrophysical in origin. Rather, they are driven by regions of the parameter space that our events and sensitivity injections allow us reliably probe with Monte Carlo likelihood estimators.

The particular sensitivity of the  $\chi_p$  distribution to these cuts can be at least partly attributed to the use of a uniform and isotropic spin prior in GWTC-4.0 parameter estimation, which induces a  $\chi_p$  prior that goes to 0 at  $\chi_p = 0, 1$ . Thus, Equation (2) is prone to yield a small  $N_{\text{eff}}$  and/or large  $\sigma_{\ln}^2$  when  $\chi_p$  is near-minimal or near-maximal. Using alternative spin priors in parameter estimation could aid in getting more effective samples at small  $\chi_p$ , improving our ability to probe the presence or absence of negligibly precessing BHs at the population level. The Monte Carlo uncertainty from working with a finite number of samples to estimate the likelihood will only grow more problematic as the number of observed CBCs increases (C. Talbot & J. Golomb 2023); development of mitigation techniques is an area of active research (e.g., D. Gerosa et al. 2020; S. Rinaldi & W. Del Pozzo 2021; C. Talbot & E. Thrane 2022; T. A. Callister et al. 2022; C. Talbot & J. Golomb 2023; K. Leyde et al. 2024; A. Hussain et al. 2026; T. A. Callister et al. 2024; A. Lorenzo-Medina & T. Dent 2025; M. Mancarella & D. Gerosa 2025).

### D.4. Comparison of Weakly Modeled Approach Results

**Mass distributions:** we supplement the strongly modeled approach with various weakly modeled approaches. Figure 20 (top panel) shows the inferred primary mass distribution using the B-SPLINE, AR, Flexible Mixtures, and BGP models compared to the fiducial BROKEN POWER LAW + 2 PEAKS model. All models agree within their 90% credible regions, though the Flexible Mixtures model is the only model that does not exhibit a prominent peak at  $\sim 10M_\odot$ . The Flexible Mixtures model does not directly infer the primary mass, but

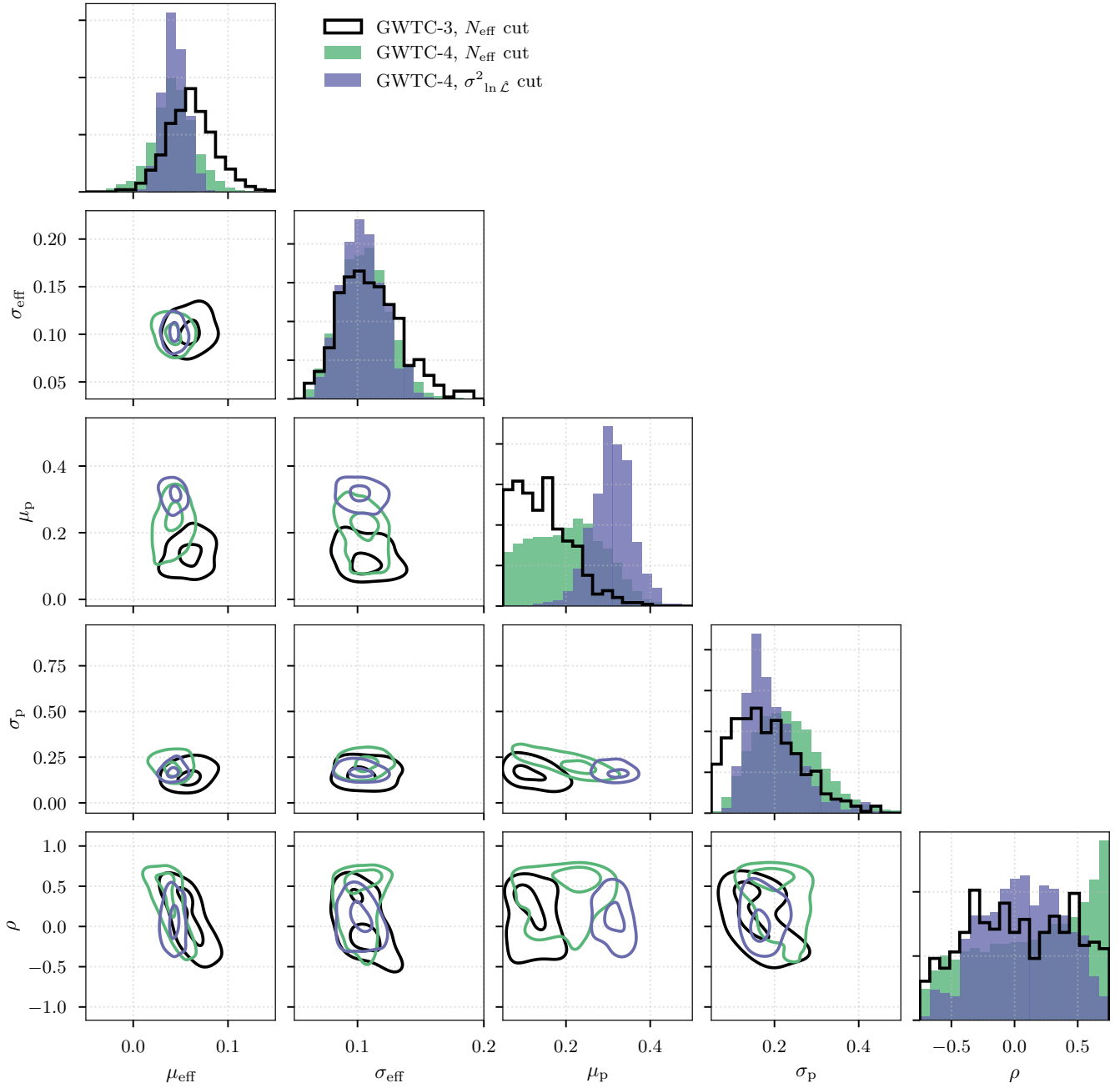


**Figure 17.** Distribution of GAUSSIAN COMPONENT SPINS hyperparameters for the primary BH (blue) and secondary BH (red) when neither magnitudes nor tilts are assumed identical (last row of Table 12), compared to when they are both assumed identical (gray, first row of Table 12). The contours of the two-dimensional distributions mark the 50th and 90th percentiles.

instead it models the chirp mass as a Gaussian mixture model and the mass ratio with a power law. The primary mass distribution shown in Figure 20 is then derived from these two distributions. The discrepancy between this model and the other weakly modeled approaches could be due to model misspecification, i.e., assuming the mass ratio distribution follows a power law for all primary masses. The fact that the discrepancy exists primarily in the  $\sim 10M_{\odot}$  region supports the ISOLATED PEAK result in Section 6.2, which suggests the  $\sim 10M_{\odot}$  peak disfavors equal mass mergers (i.e., is inconsistent with a power law in mass ratio) compared to higher mass BBHs. The mass ratio distributions inferred by the B-SPLINE, AR, and Flexible Mixtures is shown Figure 20 (bottom panel). The 90% credible regions are consistent between each model. The B-SPLINE model infers a peak away from  $q = 1$ , which is not present in the AR or Flexible Mixtures results. This may be due to the B-SPLINE model's greater flexibility compared to the AR and Flexible Mixtures models, as it infers all parameters simultaneously with B-Splines. The AR model assumes an autoregressive process only in primary mass and mass ratio, while other parameters are inferred with the fiducial models listed in Table 1. As noted in Appendix C.1, the figure includes the marginal distributions

conditioned on  $m_2 > 3M_{\odot}$  from the B-SPLINE and AR models in addition to the fully separable components (dashed lines). The two distributions are essentially identical above  $q \sim 0.4$ , below which the marginal distribution falls off sharply. This implies that the behavior of the strongly modeled approach below  $q \sim 0.4$  is primarily due to the prior assumption of a minimum mass cutoff, and not due to information inferred about the shape of the distribution in that regime.

*Effective spin distributions:* in addition to the SKEW-NORMAL EFFECTIVE SPIN model and various correlation models presented for  $\chi_{\text{eff}}$  in the main text (Figures 9 and 12), we use the weakly modeled approach for a consistency check and find the distributions shown in the top panel of Figure 21. We plot the  $\chi_{\text{eff}}$  distribution directly inferred with a binned Gaussian process (BGP; blue) as well as that reconstructed from the spin magnitude and tilt B-SPLINE model results (green), and compare them to the SKEW-NORMAL EFFECTIVE SPIN (red-orange), GAUSSIAN EFFECTIVE SPINS (purple), and  $(q, \chi_{\text{eff}})$  SPLINE (maroon) results from the main text. The two approaches paint the same qualitative picture: the  $\chi_{\text{eff}}$  distribution peaks at small values. However, there is variation between the weakly modeled approach and strongly modeled approach; the weakly modeled distributions are wider than the



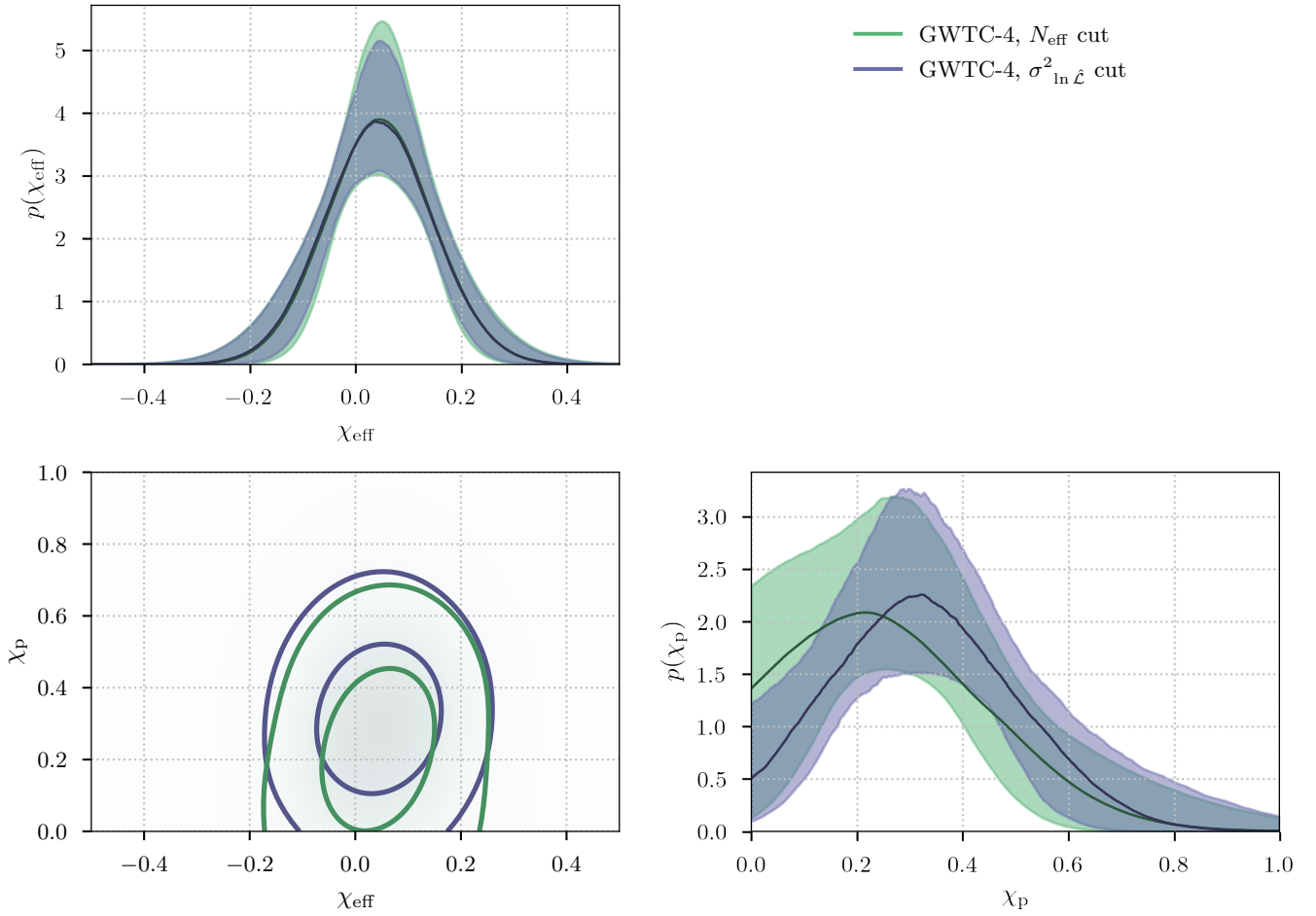
**Figure 18.** Posterior for the GAUSSIAN EFFECTIVE SPINS model hyperparameters, as defined in Table 9, for GWTC-4.0 under two methods of cutting out samples that may lead to an unconverged likelihood. Posteriors excluding samples with a substantially large log-likelihood variance ( $\sigma_{\text{ln } \mathcal{L}}^2$  cut) are shown in purple; those excluding samples with a substantially small number of effective samples ( $N_{\text{eff}}$  cut) are in green. In black are the GWTC-3.0 results with the  $N_{\text{eff}}$  cut for comparison. The  $\chi_{\text{eff}}$  hyperparameters are not affected by the cuts, while the  $\chi_p$  and joint-distribution hyperparameters are. The contours of the two-dimensional distributions mark the 50th and 90th percentiles.

strongly modeled distributions. In Figure 21, we additionally plot posteriors distributions on statistics derived from each  $\chi_{\text{eff}}$  distribution (c.f., Table 3), with results summarized as follows:

1. *First percentile of the  $\chi_{\text{eff}}$  distribution ( $\chi_{\text{eff},1\%}$ ):* the three strongly modeled distributions find consistent first-percentiles, around  $\sim 0.2$ , while the weakly modeled find that the  $\chi_{\text{eff}}$  distribution extends to lower values. In the case of the BGP, the first-percentile distribution rails against the minimum allowed value of  $-0.7$ .
2. *Fraction of BBHs with negative  $\chi_{\text{eff}}$ :* All models yield consistent posteriors with one another and find that the

fraction of BBHs with negative  $\chi_{\text{eff}}$  is greater than zero and less than  $\sim 0.8$ . The BGP posterior on this fraction is the widest, and the B-SPLINE posterior peaks at a higher values than the near-identical strongly modeled posteriors.

3. *HM fraction:* the HM fraction is a heuristic for the upper limit of the fraction of BBHs coming from HMs; it is calculated as  $1/0.16$  times the fraction of BBHs with  $\chi_{\text{eff}} < -0.3$ , based on the fact that  $\sim 16\%$  of HMs are theorized to have  $\chi_{\text{eff}} < -0.3$  (M. Fishbach et al. 2022; V. Baibhav et al. 2020). The different models yield a range of 90% upper limits for the HM fraction. With the



**Figure 19.** Marginal and joint  $\chi_{\text{eff}}$  and  $\chi_p$  distributions under the GAUSSIAN EFFECTIVE SPINS model using two methods of cutting out hyperparameter samples that may lead to an unconverged likelihood (see Figure 18). The marginal distributions show the median (solid line) and 90% credible interval on the probability density for each population distribution (shaded). The joint distribution is the PPD with contours marking the 50th and 90th quantiles.

three parametric models, we consistently find the HM fraction to be small at  $\lesssim 8\%$ . The two more flexible nonparametric models, on the other hand, find support up to larger values of 27% (B-SPLINE) or 74% (BGP).

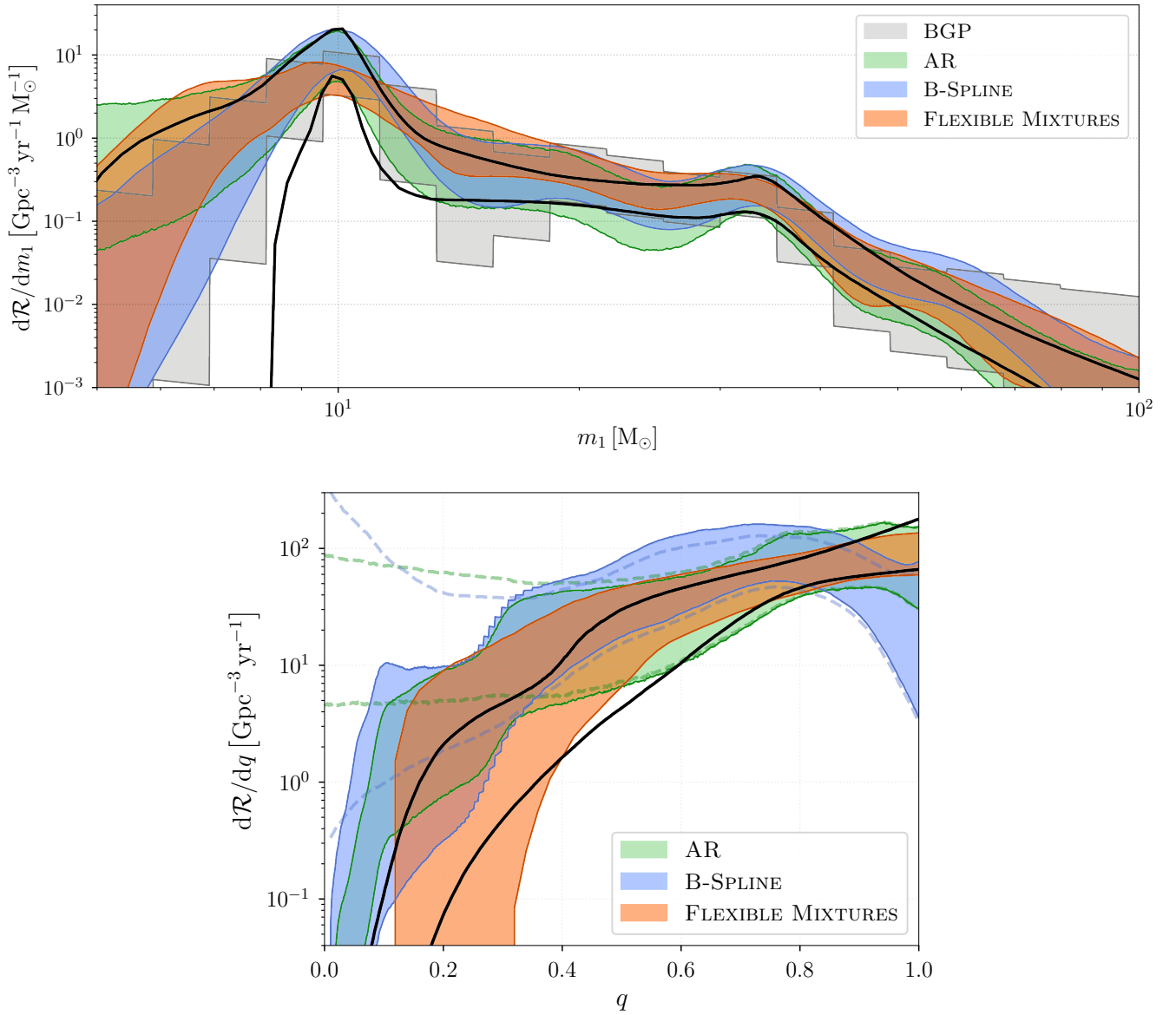
4. *Skew of the  $\chi_{\text{eff}}$  distribution about its peak:* each model finds fairly different values of the skew, which is here defined as the difference between the fraction of  $\chi_{\text{eff}} > \chi_0$  and  $\chi_{\text{eff}} < \chi_0$ , where  $\chi_0$  is the value of  $\chi_{\text{eff}}$  at which the distribution peaks (S. Banagiri et al. 2025, Equation (5)). By design, the GAUSSIAN EFFECTIVE SPINS model will always have a skew of  $\sim 0$ : truncated normal distributions are approximately symmetric about their peak if the truncation occurs substantially far from the distribution’s bulk, which is here the case. All other models find a preference for positive skew, meaning that the distribution has more support for  $\chi_{\text{eff}}$  above its peak than below. This is the most pronounced for the SKEW-NORMAL EFFECTIVE SPIN, which is entirely inconsistent with a skew of 0.

#### D.5. Merger Rates Including Subthreshold Triggers

Search pipelines compute signal-to-noise ratios (SNRs) of detector data to identify portions of data with above-threshold SNRs, i.e., “triggers”, which may contain GW events (A. G. Abac et al. 2026a). Based on pipeline-specific ranking statistics, triggers

are assigned significances quantified by FARs. In the main text, merger rates were calculated from population analyses that only used triggers surpassing a fixed-significance FAR threshold, which was motivated to introduce minimal contamination from noise events. By design, the list of triggers included in those analyses is threshold-dependent. Here, we explore the merger rates by including subthreshold triggers (W. M. Farr et al. 2015; S. J. Kapadia et al. 2020), which ensures that the inferred rates are free of biases due to arbitrary significance thresholds and mitigates loss of information from excluding subthreshold GW candidates. Specifically, we consider the full set of available triggers from a matched-filtering search, GSTLAL (C. Messick et al. 2017; S. Sachdev et al. 2019; C. Hanna et al. 2020; K. Cannon et al. 2021; B. Ewing et al. 2024; L. Tsukada et al. 2023; S. Sakon et al. 2024; A. Ray et al. 2023b; P. Joshi et al. 2025a, 2025b).

The method used by GSTLAL to self-consistently classify triggers and compute  $p_{\text{astro}}$  (B. P. Abbott et al. 2019b; S. J. Kapadia et al. 2020; A. Ray et al. 2023b; R. Abbott et al. 2023b, 2024; A. G. Abac et al. 2026a, 2026b) values provides the rate densities described here for BNSs, NSBHs, and BBHs (S. J. Kapadia et al. 2020; A. G. Abac et al. 2026a). The approach is a simplified version of the methods described in Appendix C 3 of R. Abbott et al. (2023a), as well as the discovery of GW200105 and GW200115 (R. Abbott et al. 2021c) and GW230529 (A. G. Abac et al. 2024). The simplification involves fixing the mass distribution to the

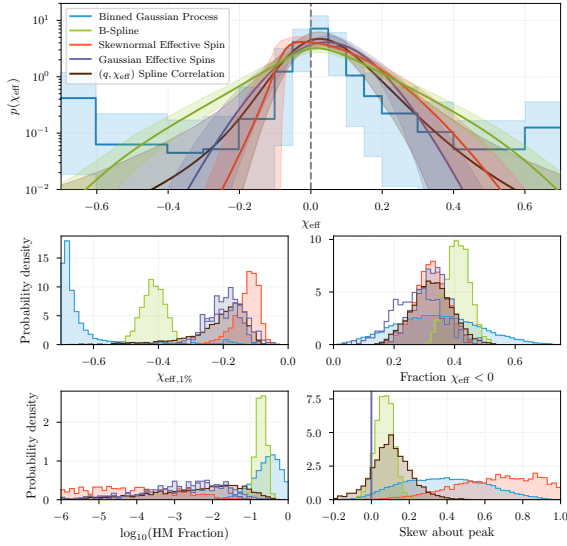


**Figure 20.** (Top) Primary mass distributions using the weakly modeled approaches outlined in Appendix C. The BROKEN POWER LAW + 2 PEAKS result is shown in black for comparison. All distributions show rates evaluated at  $z = 0.2$ , except for BGP, which shows the rate evaluated on the  $z = 0.1 - 0.25$  bin. Note that Flexible Mixtures does not infer primary mass directly, but instead derives it from the chirp mass Gaussian mixture model and the mass ratio as a power-law distribution. The lack of substructure in the Flexible Mixtures mass distribution relative to the other models is likely due to model misspecification from assuming a power-law mass ratio model. (Bottom) Mass ratio distributions using the weakly modeled approaches outlined in Appendix C. The BROKEN POWER LAW + 2 PEAKS result is shown in black for comparison. Flexible Mixtures models the chirp mass as a Gaussian mixture model and the mass ratio as a power law. For the B-SPLINE and AR models, the separable distribution  $p(q)$  is shown by dashed lines and the conditional marginal distribution  $p(q|m_2 > 3M_\odot) = \int p(q)p(m_1)\Theta(m_1q - 3)dm_1$  is shown by the shaded regions, highlighting that the low-mass ratio truncation seen in the strongly modeled approach is largely a prior effect.

Salpeter model (E. E. Salpeter 1955) as opposed to marginalizing over population uncertainties inferred by the above-threshold event analyses explored in the main text. We do not expect the marginalization over population uncertainties to have a significant impact on the inferred merger rates, given the uncertainty ranges. When we apply the simpler model to GWTC-3.0 (R. Abbott et al. 2023a), the estimated rates are comparable to those derived when marginalizing over the inferred population. For effective inspiral spins of each trigger, we use a uniform distribution. Consistent with how searches categorize triggers and compute  $\langle VT \rangle$  (A. G. Abac et al. 2026a), we set the boundary between NSs and BHs to be  $3 M_\odot$ . For triggers categorized as BNS or NSBH, we set the bounds of the spins corresponding to an NS to  $\pm 0.4$ . These bounds are

consistent with what the analyses in the main text adopt (see Section 3.2 and 5).

Using the fixed population distribution and the Poisson mixture model of S. J. Kapadia et al. (2020), we infer the merger rate densities of the different source categories (BNS, NSBH, and BBH) from the full list of available GSTLAL triggers with  $FAR < 1 \text{ hr}^{-1}$ . This is done while self-consistently accounting for the possibility that some of these triggers are likely noise artifacts. We construct the posterior of astrophysical counts of BNS, NSBH, and BBH events by utilizing mass-based binning template weights (A. Ray et al. 2023b). We estimate the time-volume sensitivity (V. Tiwari 2018; A. G. Abac et al. 2026a)  $\langle VT \rangle$  for each event category  $\alpha$  ( $\alpha = \text{BNS, NSBH, BBH}$ ), using injections (R. Essick et al. 2025), and their



**Figure 21.** First row: marginal  $\chi_{\text{eff}}$  distributions with BGP (blue) and B-SPLINE (green) models, as compared to the SKEW-NORMAL EFFECTIVE SPIN (red-orange), GAUSSIAN EFFECTIVE SPINS (purple), and  $(q, \chi_{\text{eff}})$  SPLINE (maroon) models. The PPD (average) is shown with a dark line, and the 90% confidence intervals are shaded. Second and third rows: posteriors on the first percentile of the  $\chi_{\text{eff}}$  distribution (upper left), the fraction of  $\chi_{\text{eff}} < 0$  (upper right), HM fraction (lower left), and the skew (lower right). See Section 6.3.2 for a discussion of these quantities. Colors correspond to the top panel; purple dashed is GWTC-3.0 with the GAUSSIAN EFFECTIVE SPINS model for comparison.

contributions to the counts posterior (S. J. Kapadia et al. 2020). Finally, we compute the rates posterior from marginalized counts posterior and the estimated  $\langle VT \rangle$  (B. P. Abbott et al. 2019b; R. Abbott et al. 2021a, 2023a; A. G. Abac et al. 2026b):

$$p(R_\alpha) = p(\Lambda_{1\alpha} | \mathbf{x}) \langle VT \rangle_{\text{O1-O4a}, \alpha}. \quad (\text{D1})$$

Here,  $p(\Lambda_{1\alpha} | \mathbf{x})$  is the marginalized counts posterior where  $\Lambda_{1\alpha}$  is the astrophysical count for event category  $\alpha$  and  $\Lambda_{1\alpha} = R_\alpha \langle VT \rangle_{\text{O1-O4a}, \alpha}$ . Here, O1-O4a indicates that data from O1 throughout O4a are used. The vector  $\mathbf{x}$  represents the set of triggers using in this analysis, where each  $x_i$  consists of the ranking statistics information, SNR, and an identifier for the template associated with the trigger.

A Jeffreys prior,  $\propto N^{-1/2}$ , is imposed on the astrophysical counts for BBHs to construct their posterior from the mixed Poisson likelihood and compute the merger rate. The merger rate of BBHs is computed to be  $13.1 - 17.3 \text{ Gpc}^{-3} \text{ yr}^{-1}$ . This is consistent with the BBH merger rate provided in the analyses presented in the main text, and the rate has been further narrowed compared to the results of R. Abbott et al. (2023a) while still being consistent within uncertainties. A uniform prior is used for NSBHs and BNSs, as the number of detected events containing an NS is small. We compute the NSBH merger rates to be  $22.2 - 143 \text{ Gpc}^{-3} \text{ yr}^{-1}$ , which is

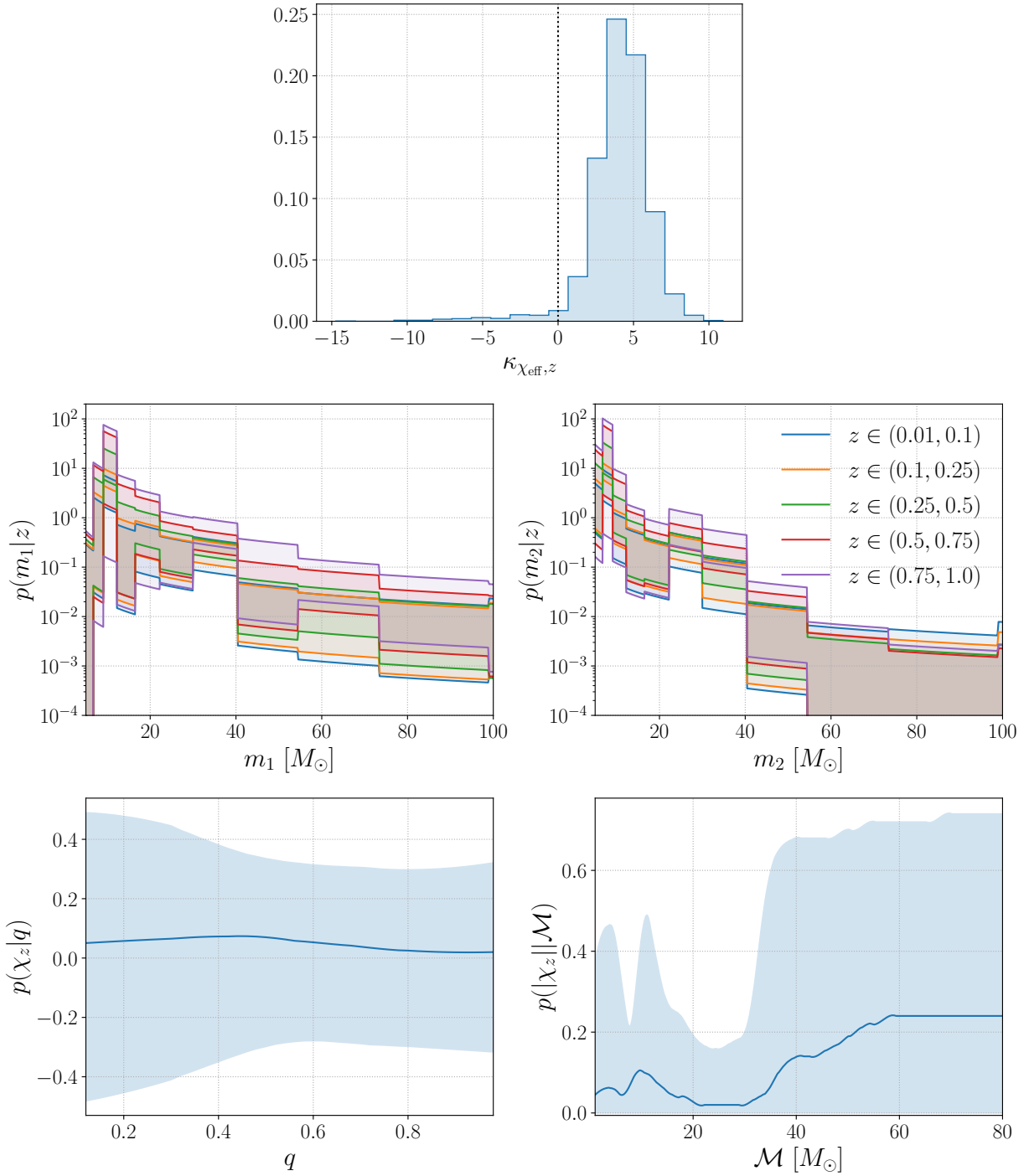
consistent with the NSBH merger rate presented in main text. Similarly to the rate for BBHs, the rate of NSBHs is consistent with the rate obtained from the analyses of GWTC-3.0 but has been further narrowed. The BNS merger rate is calculated to be  $30.9 - 361 \text{ Gpc}^{-3} \text{ yr}^{-1}$ , which is consistent with the BNS merger rate presented in the main text and has been narrowed down compared to the rate obtained from the analyses of GWTC-3.0.

#### D.6. Supplementary Results: BBH Correlations

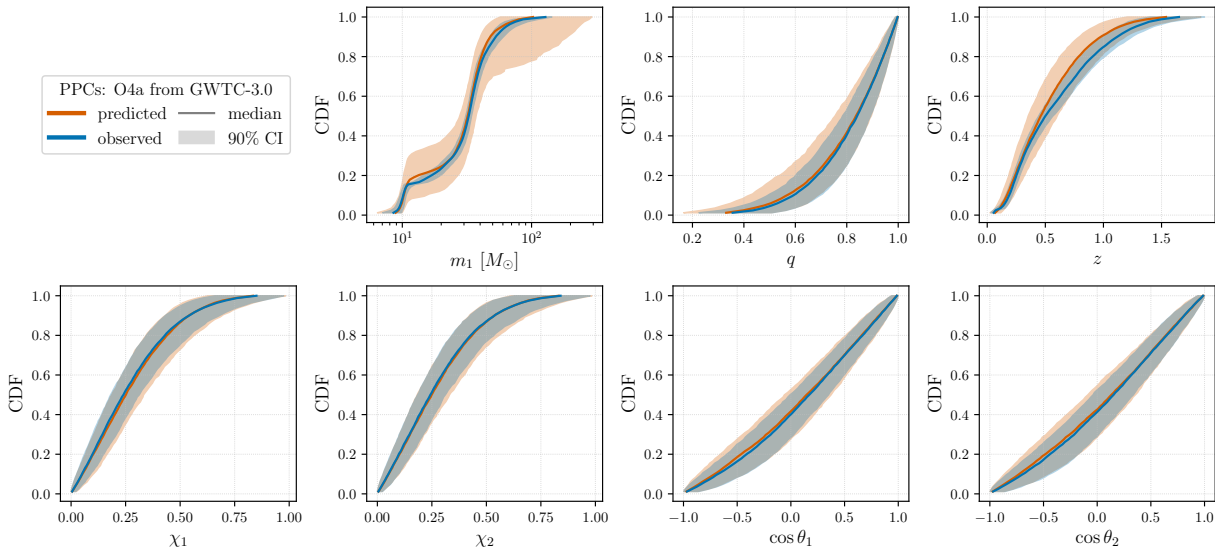
Here, we supplement the correlated BBH population results presented in Section 6.5 with additional results and figures. In the top panel of Figure 22, we plot the posterior distribution for the level of correlation  $\kappa_{\chi_{\text{eff}}, z}$  inferred in the COPULA model for  $(z, \chi_{\text{eff}})$ . Note the peak at positive values and long tail into negative values. The middle panels show the inferred mass distributions, using a mass-redshift correlated BGP analysis, binned by redshift. We see that both the primary and secondary mass distributions appear to be broadly consistent across redshifts up to  $z = 1$ . Finally, we investigate mass and spin correlations with the data-driven FM analyses. In the bottom panels of Figure 22, we plot the inferred distribution of orbital aligned spin  $\chi_z$  as a function of both chirp mass and mass ratio, obtained with the FM analysis. We see that the results have a large degree of uncertainty and are broadly consistent with findings explored here and in Section 6.5.

#### D.7. Posterior Predictive Checks

Posterior predictive checks (PPCs) are model validation tools that check for consistency between model predictions and observed data (A. Gelman et al. 1996; M. J. Bayarri & M. E. Castellanos 2008). To check if our default BROKEN POWER LAW + 2 PEAKS model can predict held-out data, we fit this model to GWTC-3.0 data and check for its ability to predict O4a observations. For each sample from the GWTC-3.0 hyperposterior, we draw a mock catalog of 84 detected events (i.e., the number of BBHs detected in O4a passing  $FAR < 1 \text{ yr}^{-1}$ ) by reweighing the injection set used for sensitivity estimates. We plot the cumulative density function (CDF) of these mock detected events, whose spread corresponds to uncertainty in the inferred population parameters. To build the observed CDFs, we repeat the same procedure with PE samples for each event reweighed to the hyperposterior, retaining one sample at random. Readers are directed to, e.g., I. M. Romero-Shaw et al. (2022) and S. J. Miller et al. (2026) for a more detailed description of PPC methodology. We find that the observed and predicted CDFs agree in Figure 23, indicating that the the population distribution inferred with the the BROKEN POWER LAW + 2 PEAKS model on GWTC-3.0 data is a good description of the new O4a data.



**Figure 22.** Top: posterior distributions for the level of correlation between redshift and effective inspiral spin  $\kappa_{\chi_{\text{eff}},z}$  inferred using the COPULA model. The vertical black dashed line in each plot indicates a value of  $\kappa_{\chi_{\text{eff}},z}$ , at which no correlation is implied. Middle: inferred distributions of primary mass (left) and secondary mass (right) in the redshift and spin correlated BGP analysis. The solid lines bound the 90% credible intervals for each redshift bin. We can see that all redshift bins from  $z = 0.01$  to  $z = 1$  are consistent within 90% credibility. Bottom: correlated mass and spin PPDs from the FM model. Solid lines give the medians, while the shaded regions encompass 90% of the PPD volume. The left panel gives the inferred distribution of aligned spin  $\chi_z$  given mass ratio. We do not see any evidence for or against a correlation. The right panel gives the inferred distribution of the aligned spin magnitude  $|\chi_z|$  as a function of chirp mass. We see that the uncertainty is very large, with a notable drop in the  $\sim 20 - 30 M_\odot$  region. For reference, this region very roughly corresponds to the  $30 M_\odot$  peak observed in the component mass distributions (a  $30 M_\odot + 30 M_\odot$  BBH has a chirp mass of  $\mathcal{M} \approx 26 M_\odot$ ). Following the mass- and spin-correlated BGP results then, it is unsurprising that the FM results prefer a local minimum in aligned spin magnitude in this region.



**Figure 23.** Posterior predictive checks for the BROKEN POWER LAW + 2 PEAKS model. The orange CDFs denote predictions of O4a observations from the BROKEN POWER LAW + 2 PEAKS model fit to GWTC-3.0 data, whereas the blue CDFs denote O4a observations. The predicted and observed curves match within their 90% credible regions, indicating that the BROKEN POWER LAW + 2 PEAKS model performs well at describing held-out data.

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